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# CS380: Computer Graphics

# Ray Tracing

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**Course URL:**  
<http://sglab.kaist.ac.kr/~sungeui/CG/>

**KAIST**



# Class Objectives

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- **Understand overall algorithm of recursive ray tracing**
  - Ray generations
  - Intersection tests
  - Basic sampling methods

# Various Visibility Algorithm

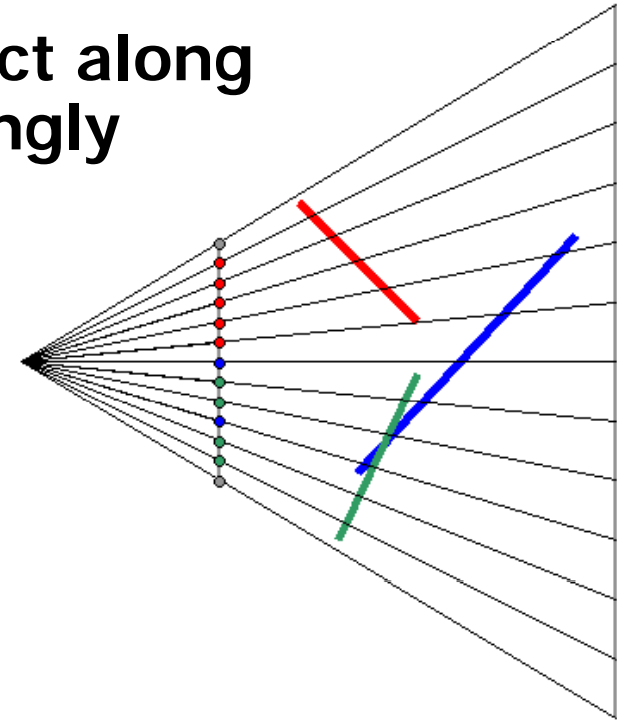
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- Z-buffer
- Scan-line algorithm
- Ray casting, etc.

# Ray Casting

- For each pixel, find closest object along the ray and shade pixel accordingly
- Advantages
  - Conceptually simple
  - Can take advantage of spatial coherence in scene
  - Can be extended to handle global illumination effects
- Disadvantages
  - Renderer must have access to entire retained model
  - Hard to map to special-purpose hardware

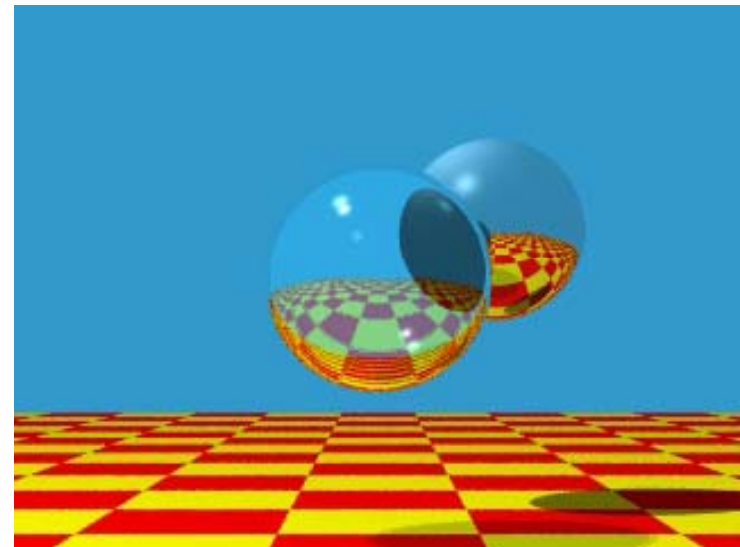


# Recursive Ray Casting

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- Ray casting generally dismissed early on because of aforementioned problems
- Gained popularity in when Turner Whitted (1980) showed this image
  - *Show recursive* ray casting could be used for global illumination effects



# Ray Casting and Ray Tracing

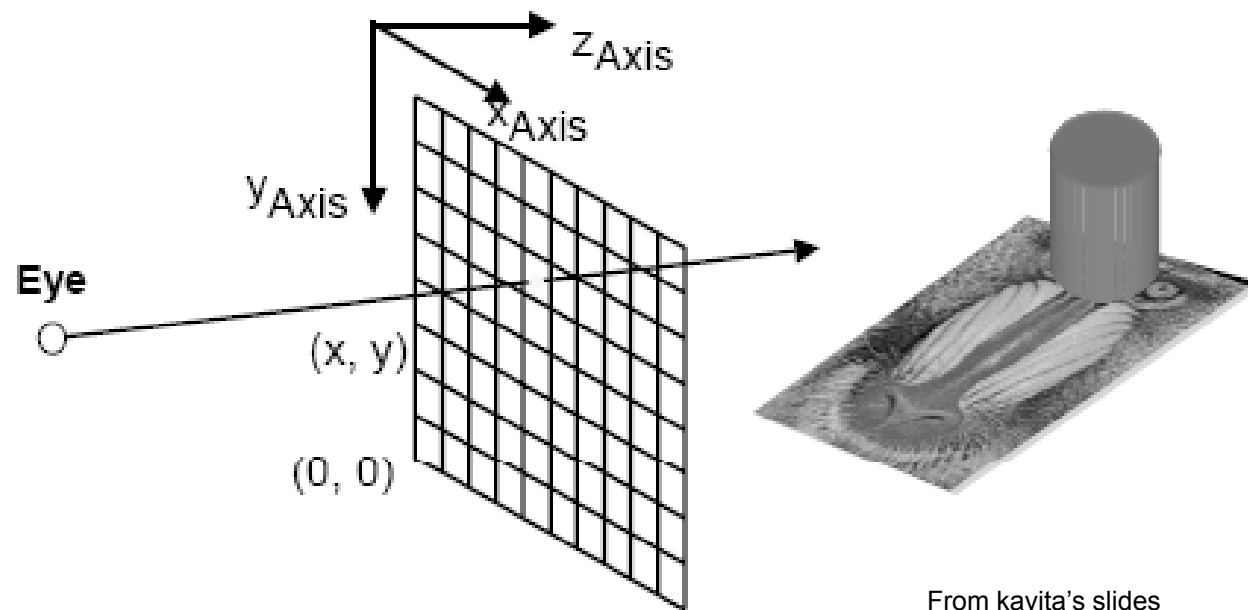
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- Trace rays from eye into scene
  - Backward ray tracing
- Ray casting used to compute visibility at the eye
- Perform ray tracing for arbitrary rays needed for shading
  - Reflections
  - Refraction and transparency
  - Shadows

# Basic Algorithms of Ray Tracing

- Rays are cast from the eye point through each pixel in the image

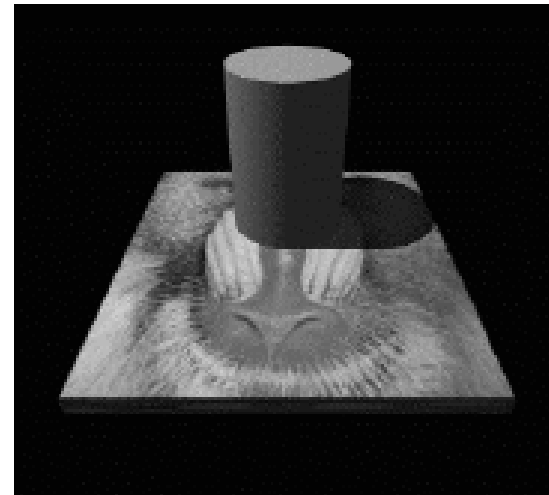
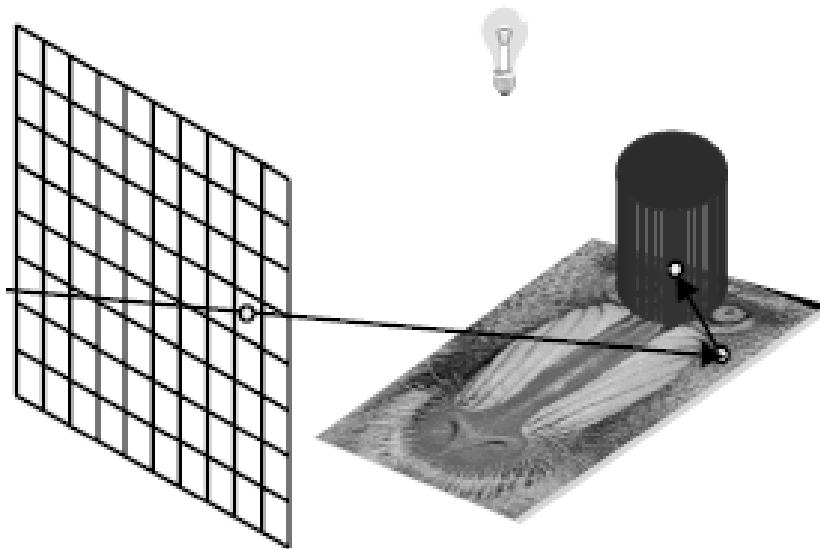


# Shadows

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- Cast ray from the intersection point to each light source
  - Shadow rays

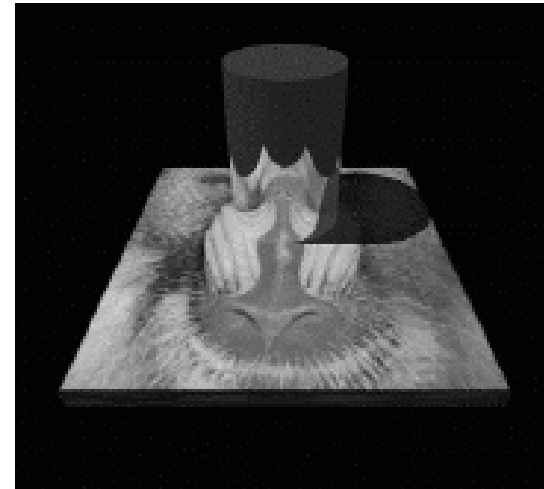
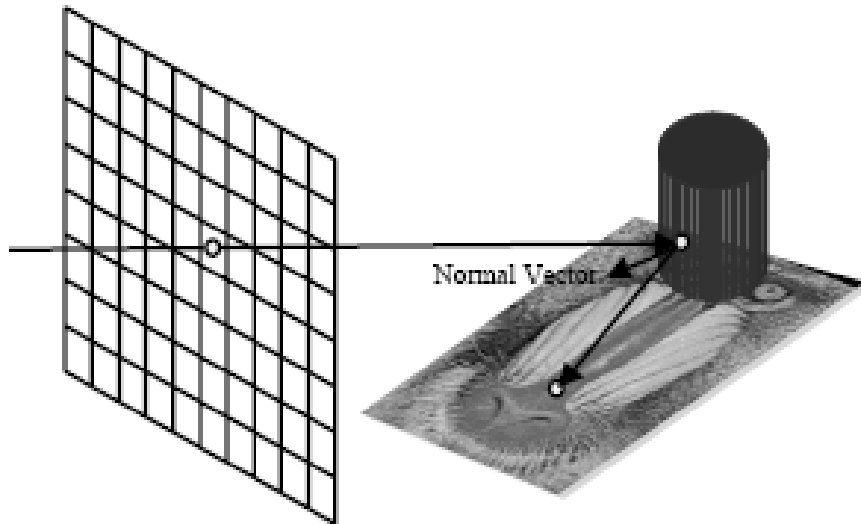


From kavita's slides



# Reflections

- If object specular, cast secondary reflected rays



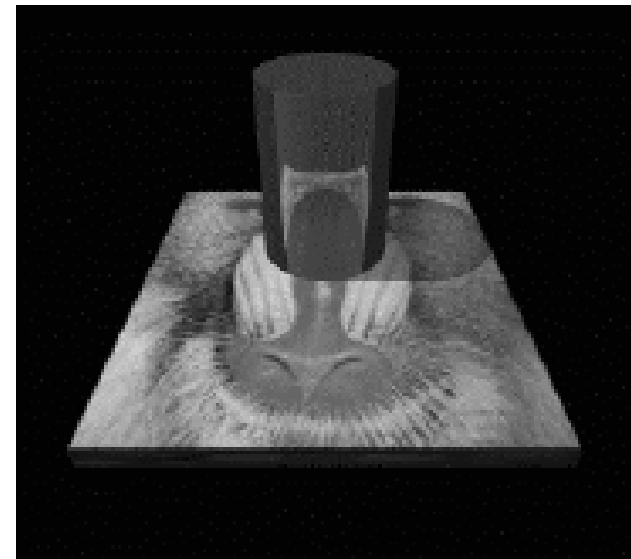
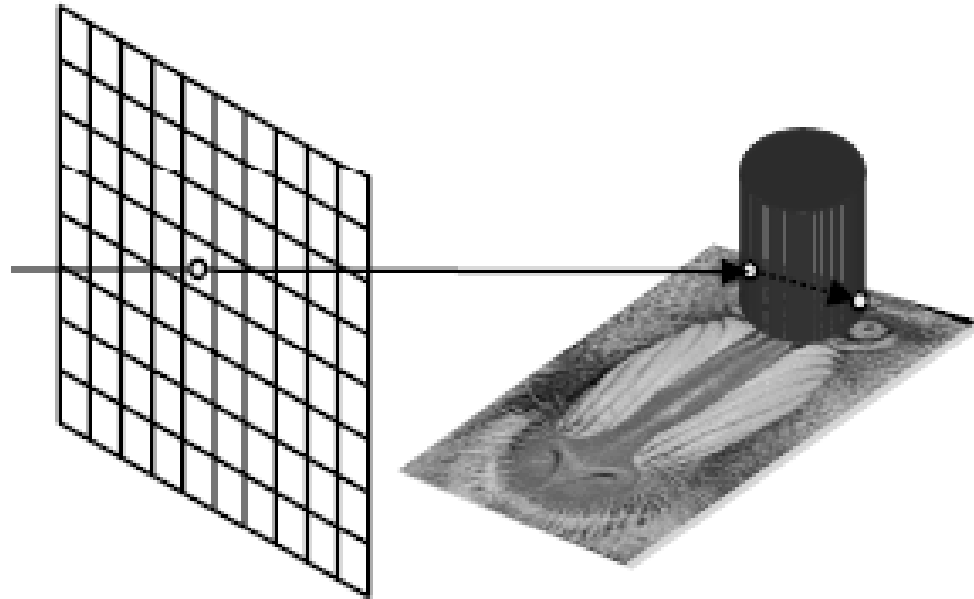
From kavita's slides

# Refractions

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- If object transparent, cast secondary refracted rays



From kavita's slides

# An Improved Illumination Model [Whitted 80]

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- Phong model

$$I_r = \sum_{j=1}^{\text{numLights}} (k_a^j I_a^j + k_d^j I_d^j (\hat{N} \cdot \hat{L}_j) + k_s^j I_s^j (\hat{V} \cdot \hat{R})^{n_s})$$

- Whitted model

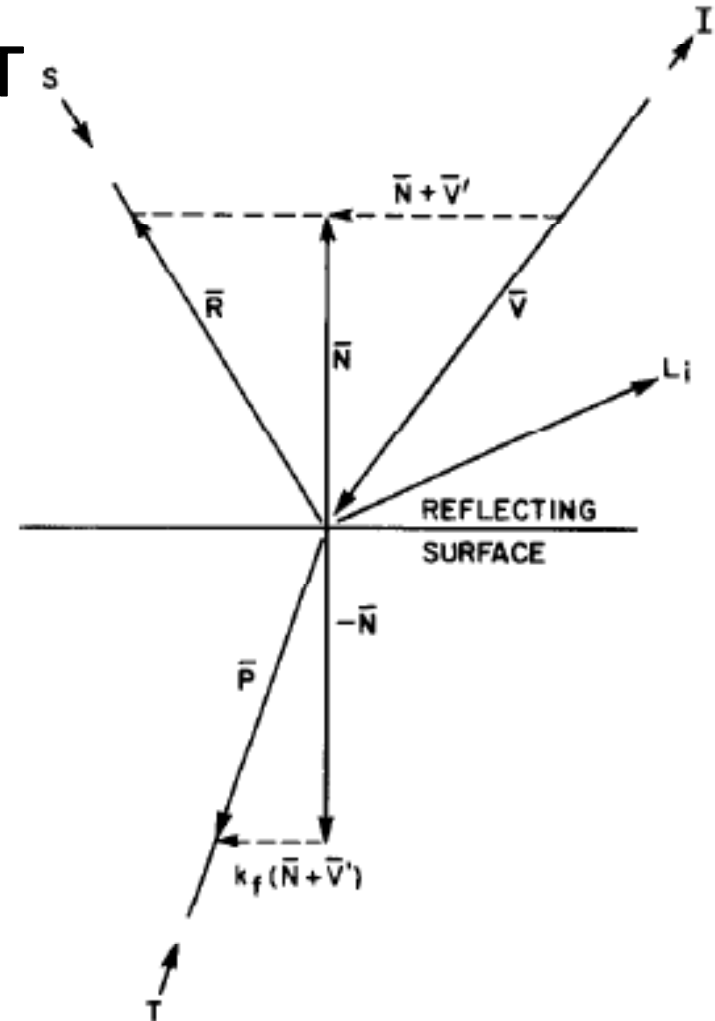
$$I_r = \sum_{j=1}^{\text{num\_Visible\_Lights}} (k_a^j I_a^j + k_d^j I_d^j (\hat{N} \cdot \hat{L}_j)) + k_s S + k_t T$$

- S and T are intensity of light from reflection and transmission rays
- Ks and Kt are specular and transmission coefficient

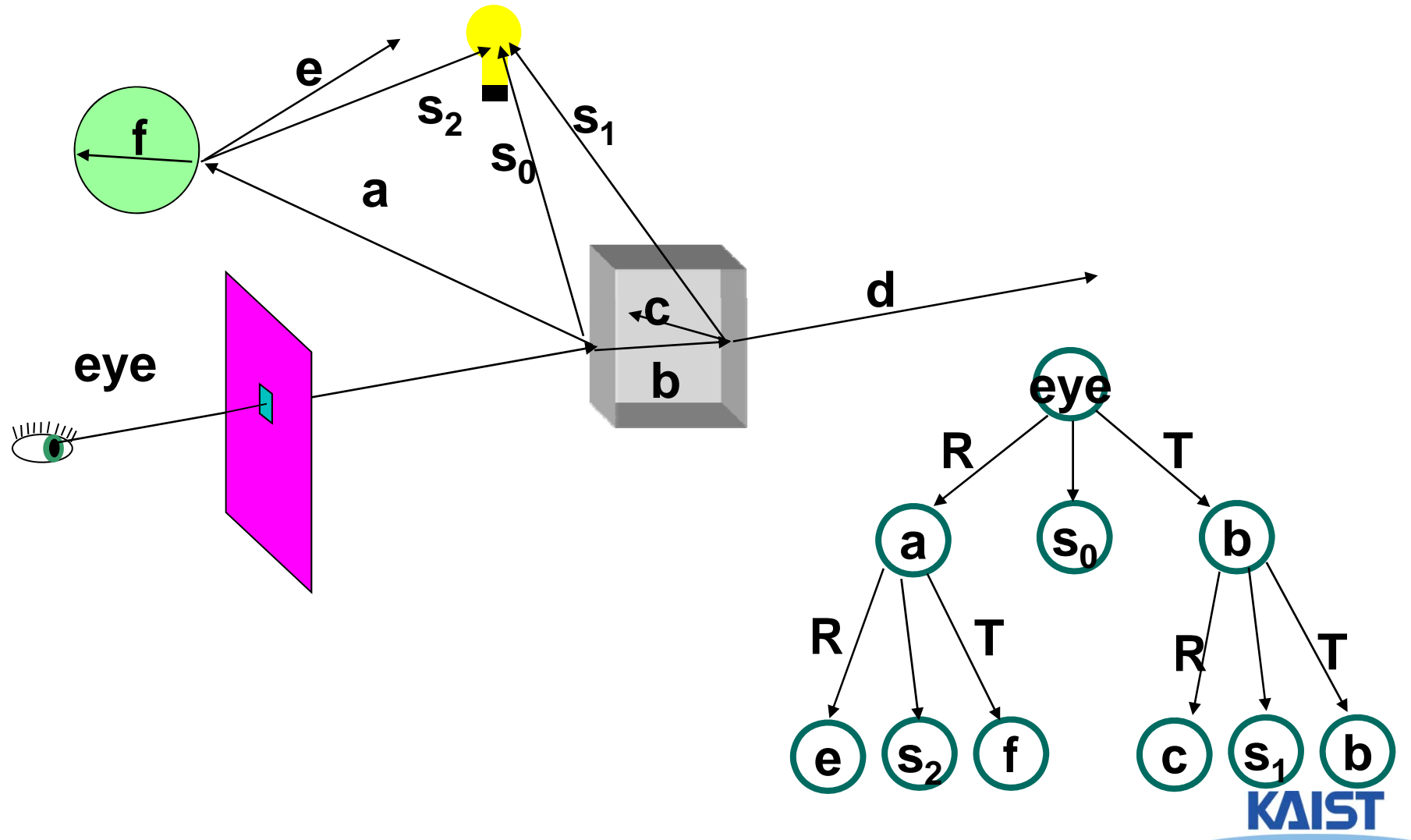
# An Improved Illumination Model [Whitted 80]

$$I_r = \sum_{j=1}^{\text{numLights}} (k_a^j I_a^j + k_d^j I_d^j (\hat{N} \cdot \hat{L}_j)) + k_s S + k_t T_s$$

Computing reflection and transmitted/refracted rays is based on Snell's law (refer to Chapter 9.6 and 9.7)



# Ray Tree



# Overall Algorithm of Ray Tracing

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- Per each pixel, compute a ray,  $R$

function RayTracing ( $R$ )

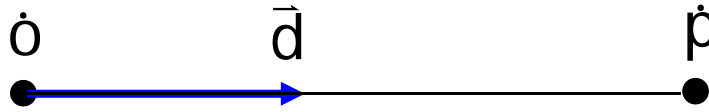
- Compute an intersection against objects
- If no hit,
  - Return the background color
- Otherwise,
  - Compute shading,  $c$
  - General secondary ray,  $R'$
  - Perform  $c' = \text{RayTracing}(R')$
  - Return  $c+c'$

# Ray Representation

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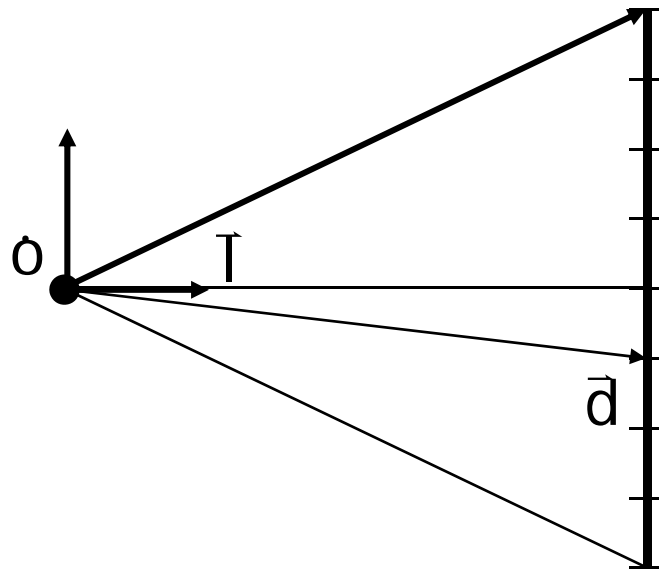
- We need to compute the first surface hit along a ray
  - Represent ray with origin and direction
  - Compute intersections of objects with ray
  - Return closest object

$$\vec{p}(t) = \vec{o} + t\vec{d}$$


# Generating Primary Rays

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# Generating Secondary Rays

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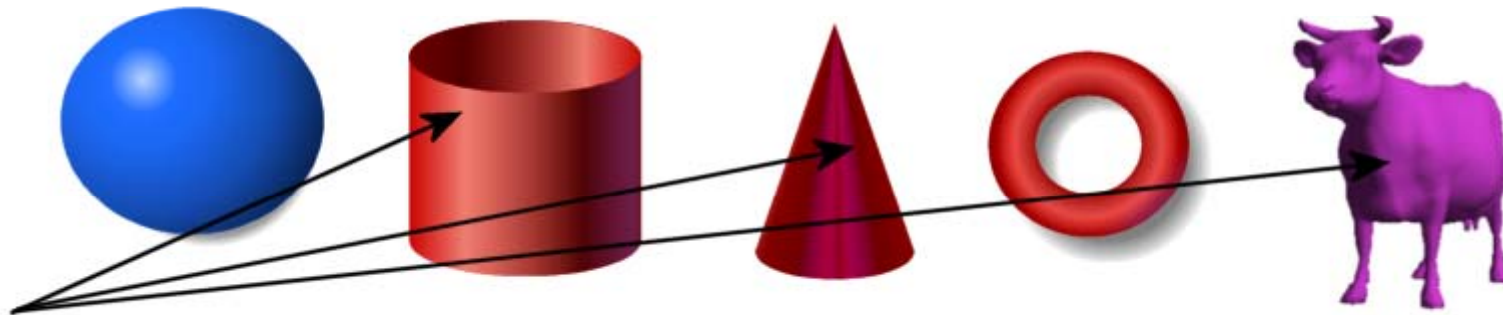
- The origin is the intersection point  $p_0$
- Direction depends on the type of ray
  - Shadow rays – use direction to the light source
  - Reflection rays – use incoming direction and normal to compute reflection direction
  - Transparency/refraction – use snell's law

# Intersection Tests

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Go through all of the objects in the scene to determine the one closest to the origin of



**Strategy: Solve of the intersection of the Ray with a mathematical description of the object**

# Simple Strategy

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- **Parametric ray equation**

- Gives all points along the ray as a function of the parameter

$$\dot{p}(t) = \dot{o} + t \vec{d}$$

- **Implicit surface equation**

- Describes all points on the surface as the zero set of a function

$$f(\dot{p}) = 0$$

- **Substitute ray equation into surface function and solve for t**

$$f(\dot{o} + t \vec{d}) = 0$$

# Ray-Plane Intersection

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- **Implicit equation of a plane:**

$$\vec{n} \cdot \vec{p} - d = 0$$

- **Substitute ray equation:**

$$\vec{n} \cdot (\vec{o} + t\vec{d}) - d = 0$$

- **Solve for t:**

$$t(\vec{n} \cdot \vec{d}) = d - \vec{n} \cdot \vec{o}$$

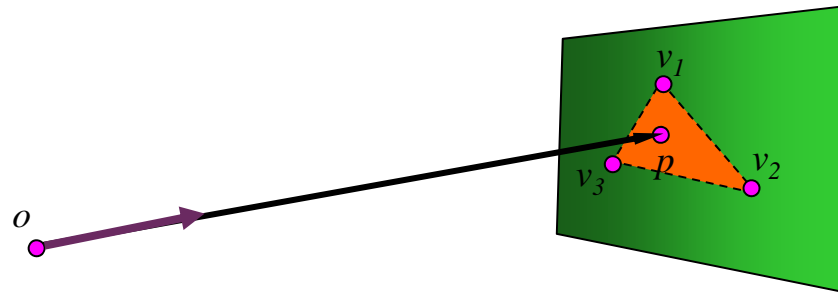
$$t = \frac{d - \vec{n} \cdot \vec{o}}{\vec{n} \cdot \vec{d}}$$

# Generalizing to Triangles

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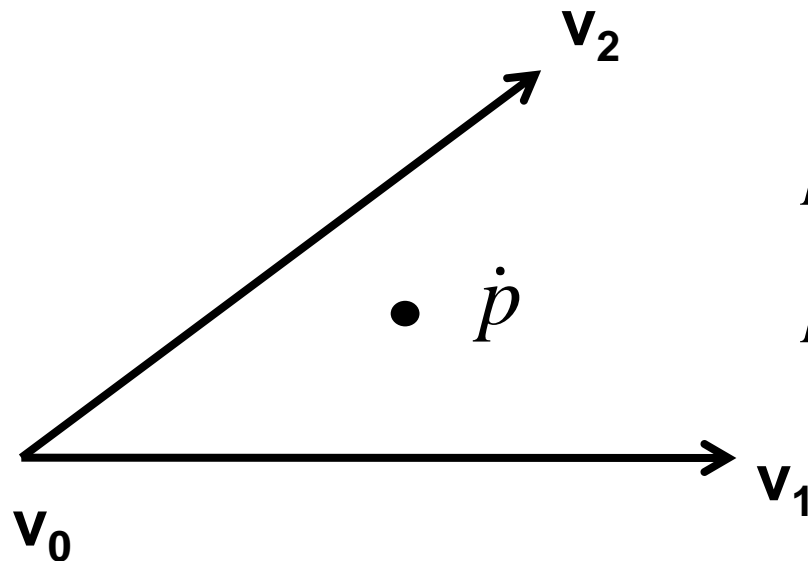
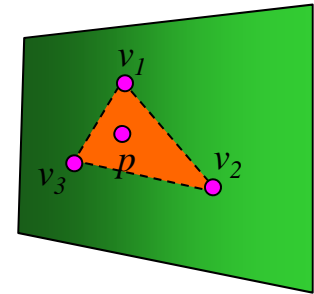
- Find of the point of intersection on the plane containing the triangle
- Determine if the point is inside the triangle
  - Barycentric coordinate method
  - Many other methods



# Barycentric Coordinates

- Points in a triangle have positive barycentric coordinates:

$$\dot{p} = \alpha \dot{v}_0 + \beta \dot{v}_1 + \gamma \dot{v}_2 \quad , \text{where } \alpha + \beta + \gamma = 1$$



$$\dot{p} = \dot{v}_0 + \beta(\dot{v}_1 - \dot{v}_0) + \gamma(\dot{v}_2 - \dot{v}_0)$$

$$\dot{p} = (1 - \beta - \gamma)\dot{v}_0 + \beta\dot{v}_1 + \gamma\dot{v}_2$$

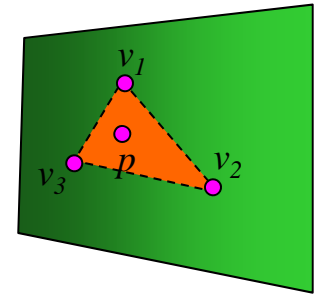
# Barycentric Coordinates

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- Points in a triangle have positive barycentric coordinates:

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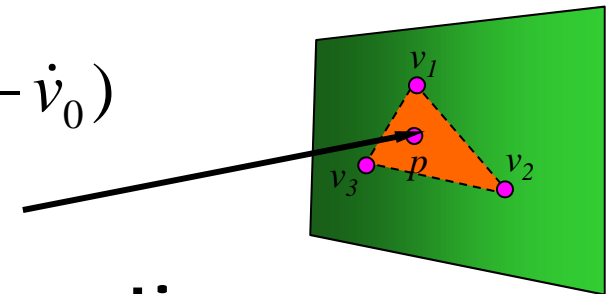


- **Benefits:**
  - Barycentric coordinates can be used for interpolating vertex parameters (e.g., normals, colors, texture coordinates, etc)

# Ray-Triangle Intersection

- A point in a ray intersects with a triangle

$$\dot{p}(t) = \dot{v}_0 + \beta(\dot{v}_1 - \dot{v}_0) + \gamma(\dot{v}_2 - \dot{v}_0)$$



- Three unknowns, but three equations
- Compute the point based on  $t$
- Then, check whether the point is on the triangle
- Refer to Sec. 9.3.2 in the textbook for the detail equations

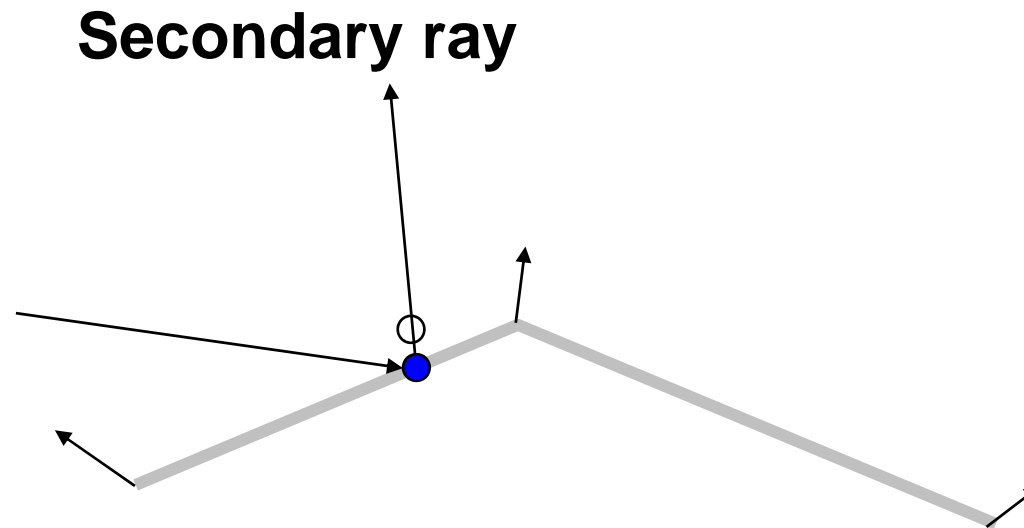


# Robustness Issues

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- **False self-intersections**
  - One solution is to offset the origin of the ray from the surface when tracing secondary rays

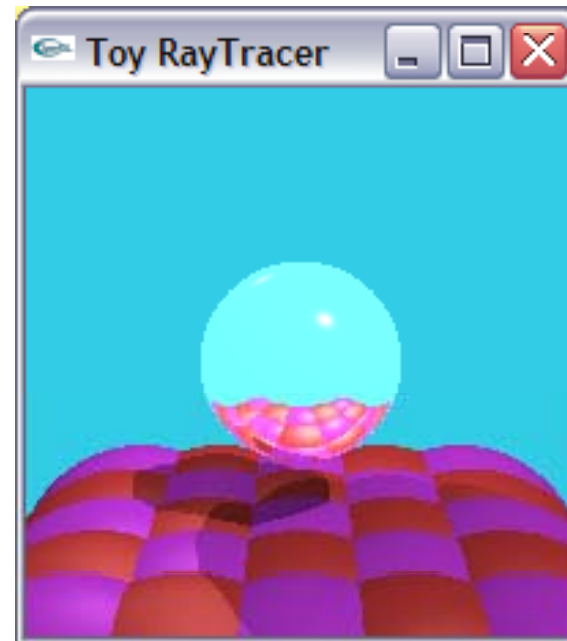


# Pros and Cons of Ray Tracing

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## Advantages of Ray Tracing:

- Very simple design
- Improved realism over the graphics pipeline



## Disadvantages:

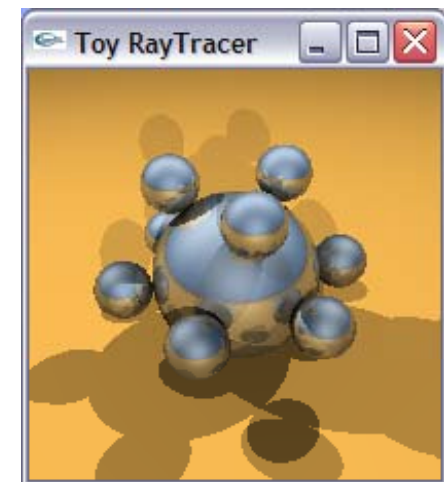
- Very slow per pixel calculations
- Only approximates full global illumination
- Hard to accelerate with special-purpose H/W

# Acceleration Methods

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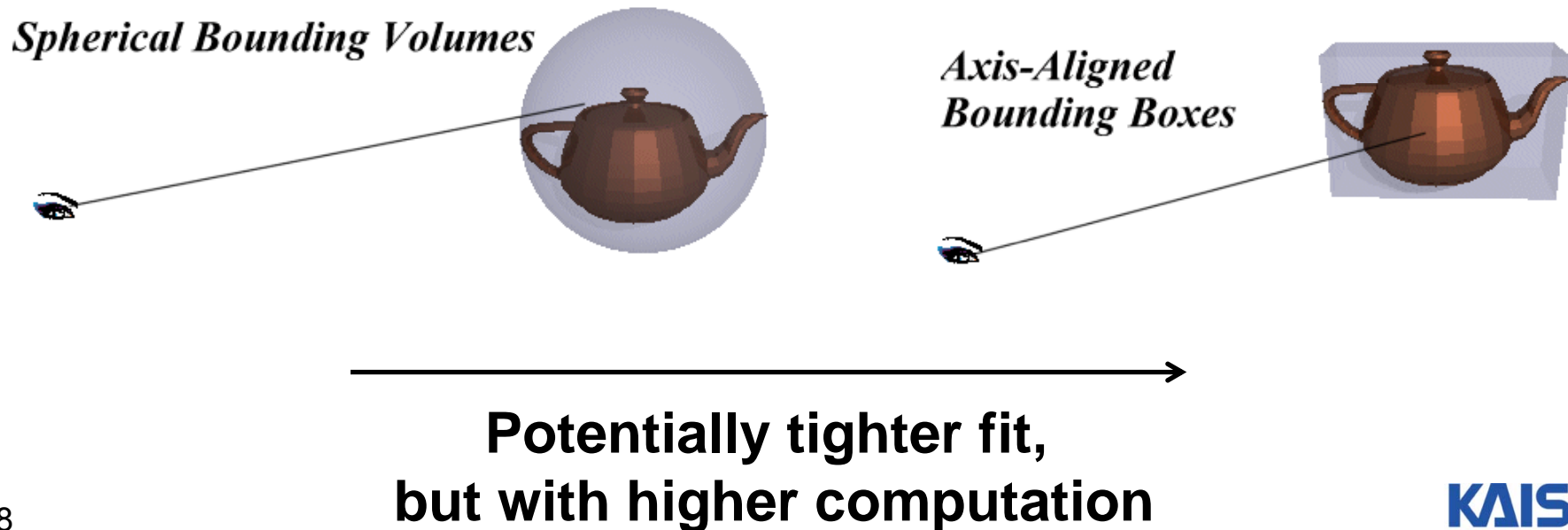
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- **Rendering time for a ray tracer depends on the number of ray intersection tests per pixel**
  - The number of pixels X the number of primitives in the scene
- **Early efforts focused on accelerating the ray-object intersection tests**
- **More advanced methods required to make ray tracing practical**
  - **Bounding volume hierarchies**
  - **Spatial subdivision**



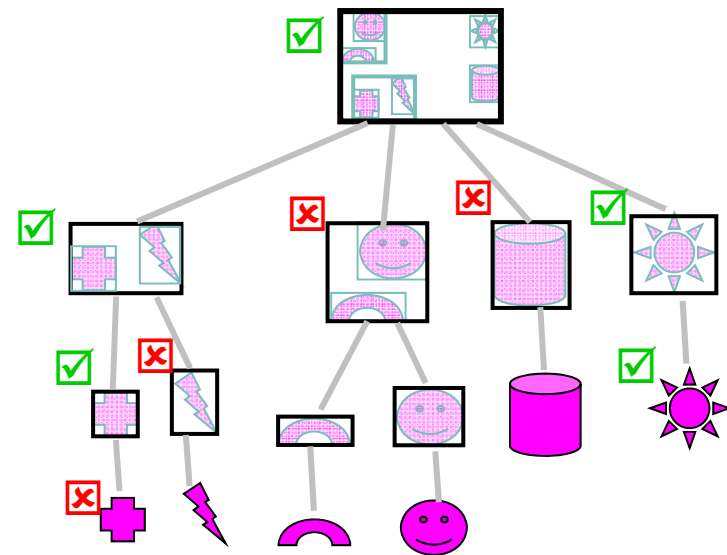
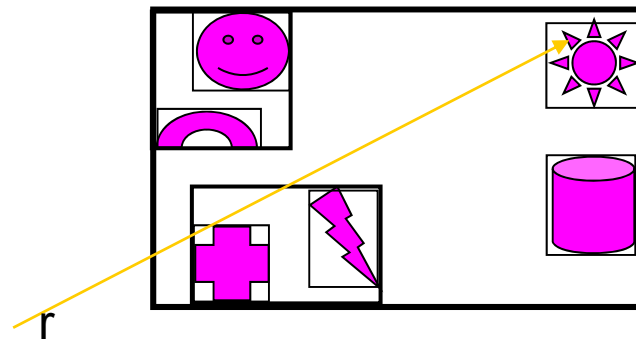
# Bounding Volumes

- Enclose complex objects within a simple-to-intersect objects
  - If the ray does not intersect the simple object then its contents can be ignored
  - The likelihood that it will strike the object depends on how tightly the volume surrounds the object.



# Hierarchical Bounding Volumes

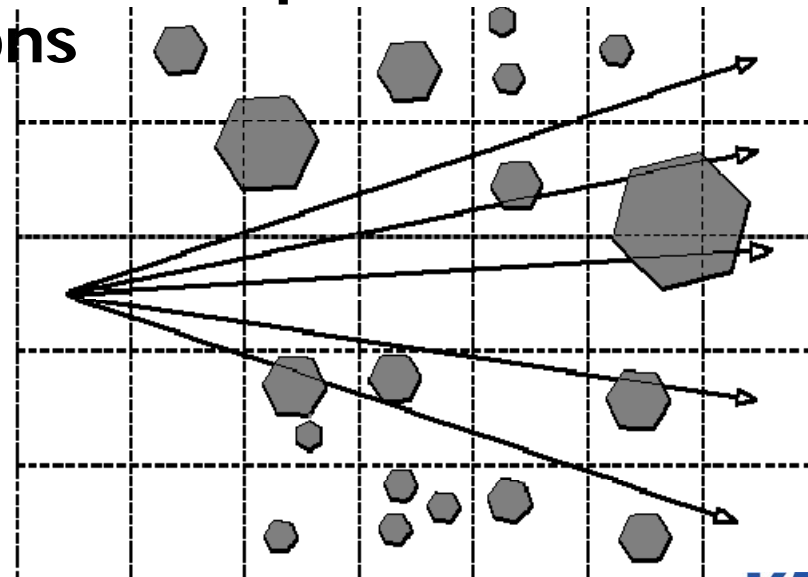
- Organize bounding volumes as a tree
- Each ray starts with the root BV of the tree and traverses down through the tree



# Spatial Subdivision

**Idea:** Divide space in to subregions

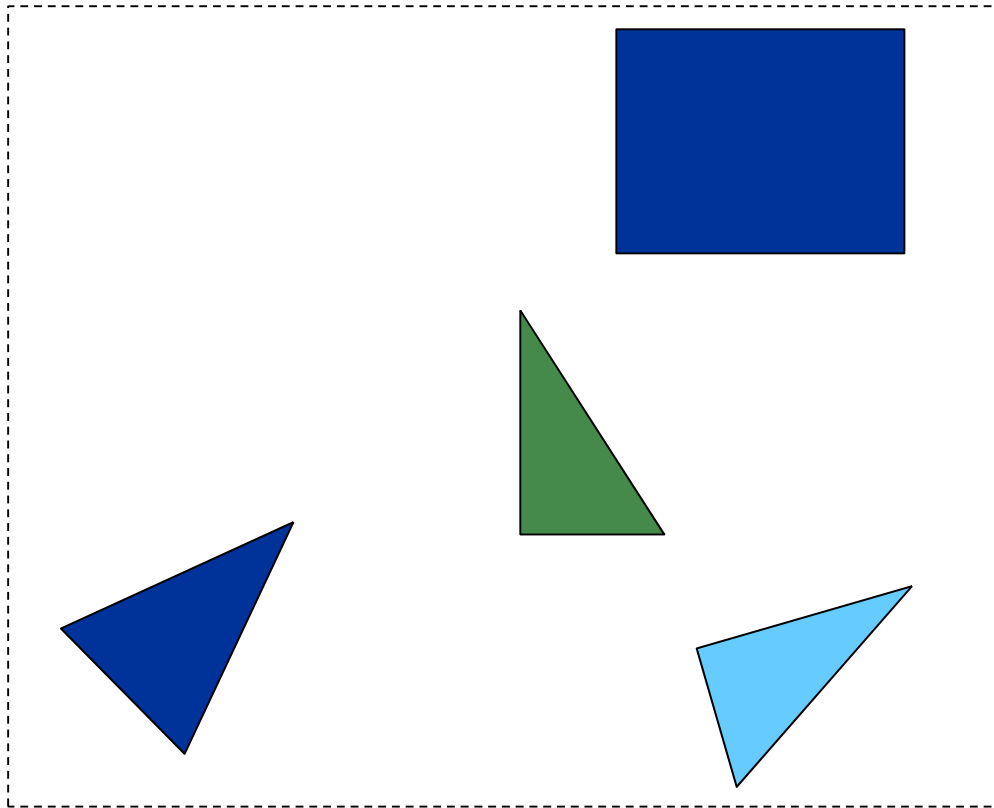
- Place objects within a subregion into a list
- Only traverse the lists of subregions that the ray passes through
- “Mailboxing” used to avoid multiple test with objects in multiple regions
- Many types
  - Regular grid
  - Octree
  - BSP tree
  - kd-tree



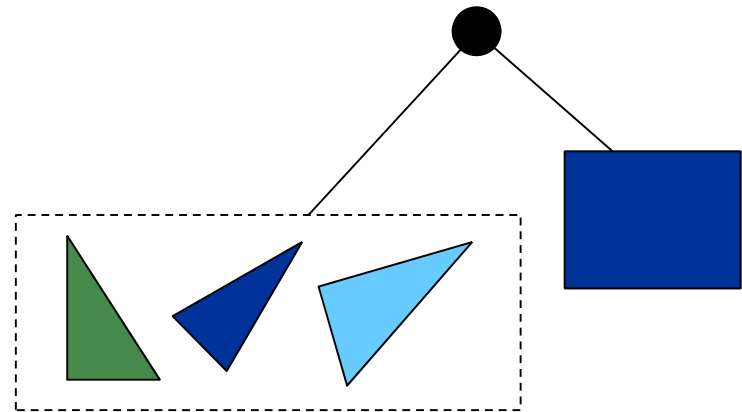
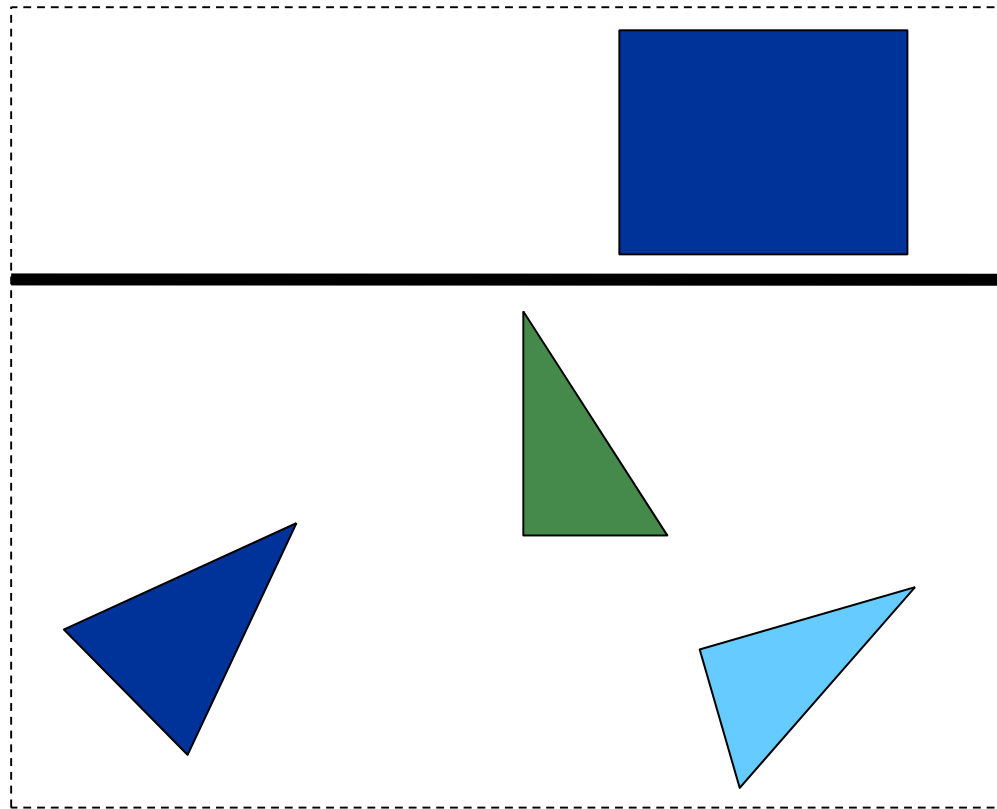
# Kd-tree: Example

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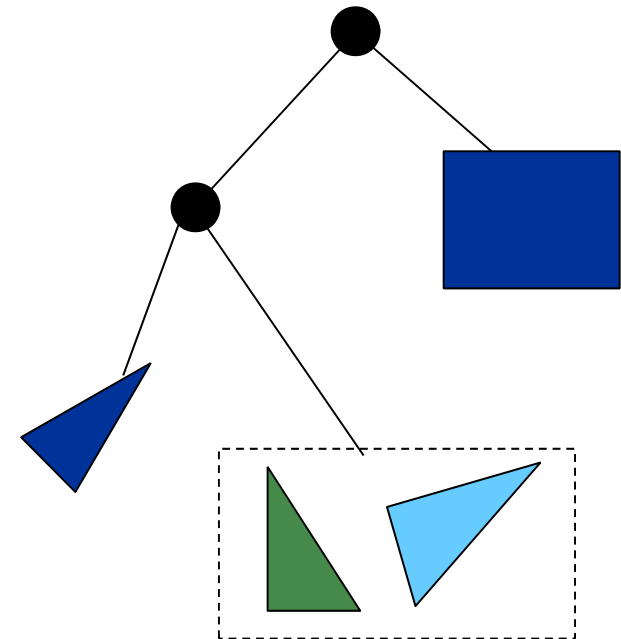
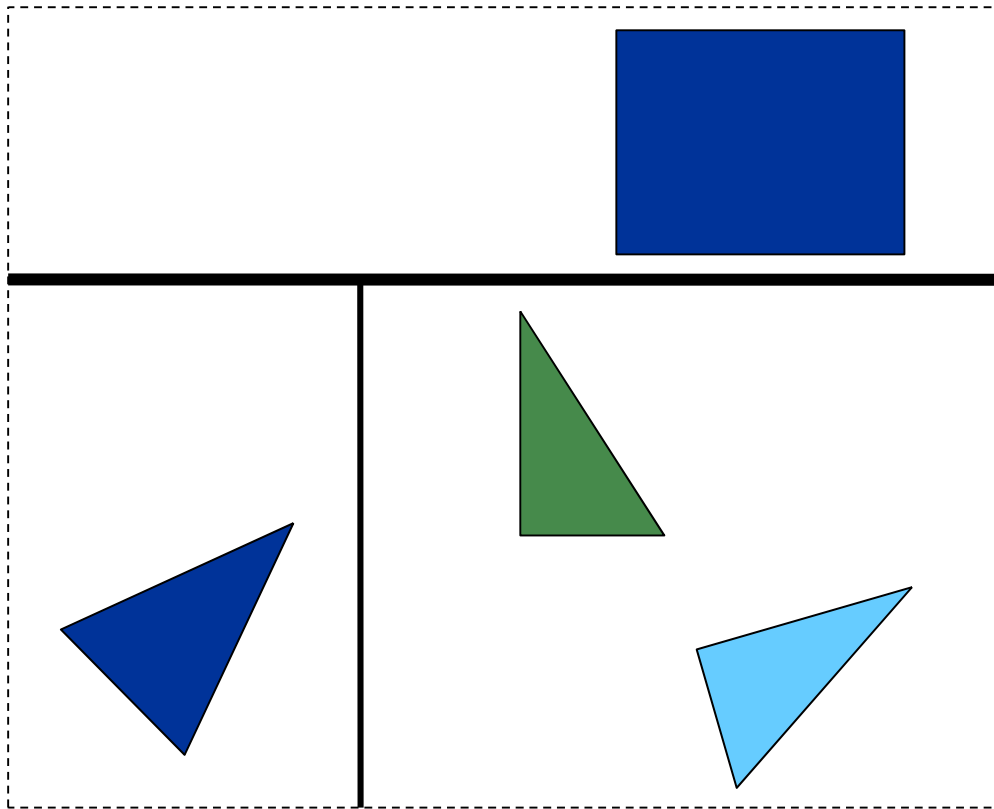


# Kd-tree: Example

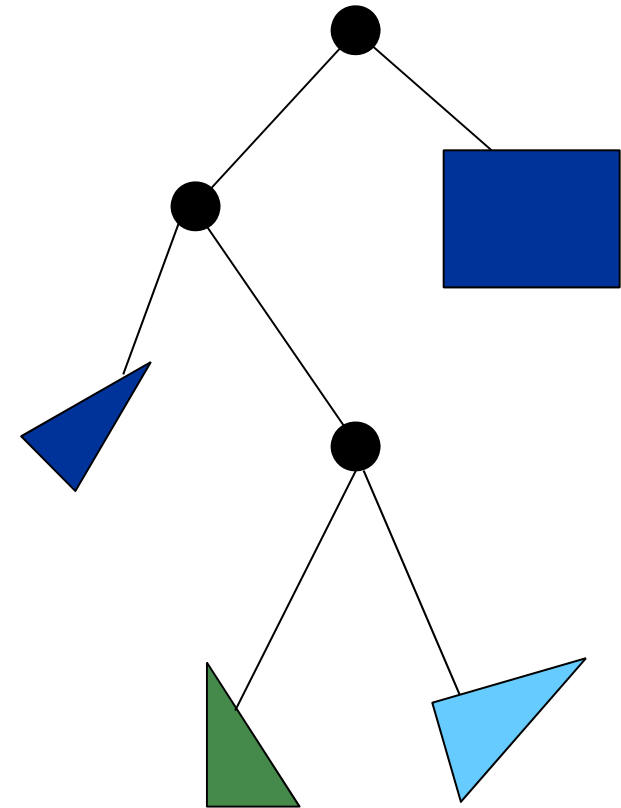
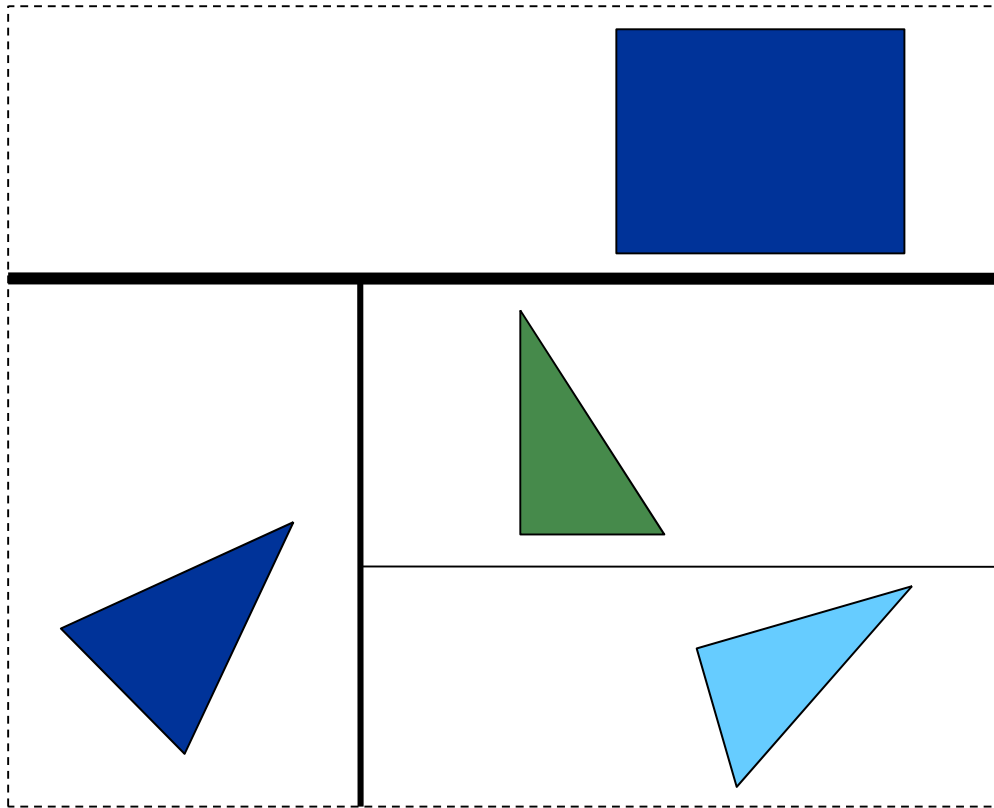




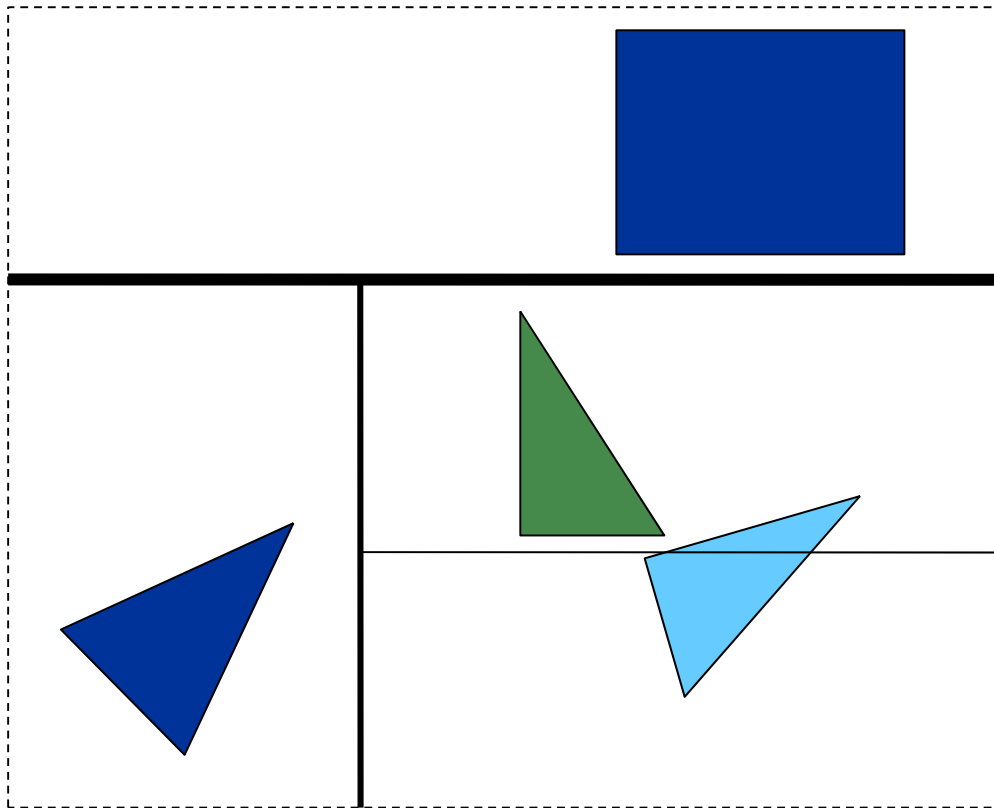
# Kd-tree: Example



# Example

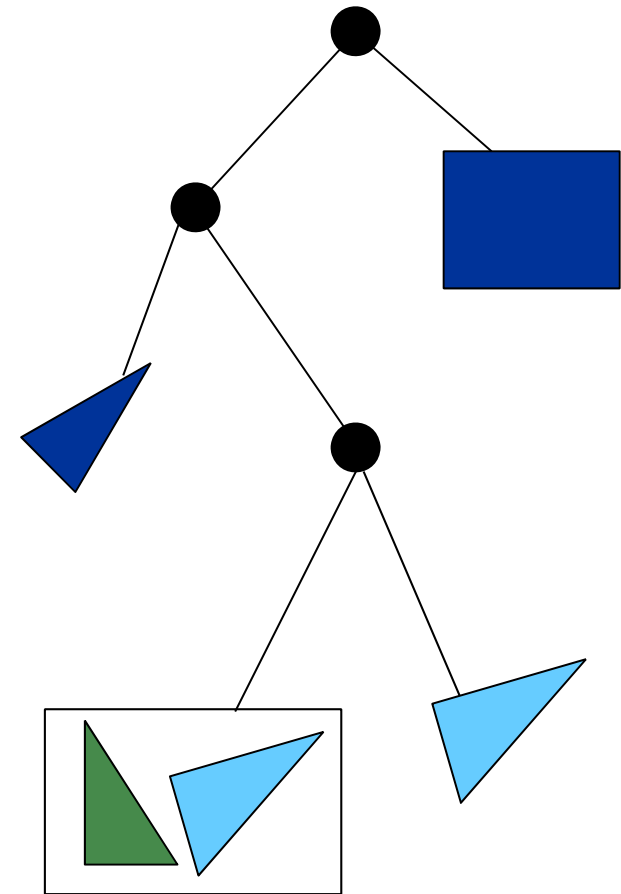
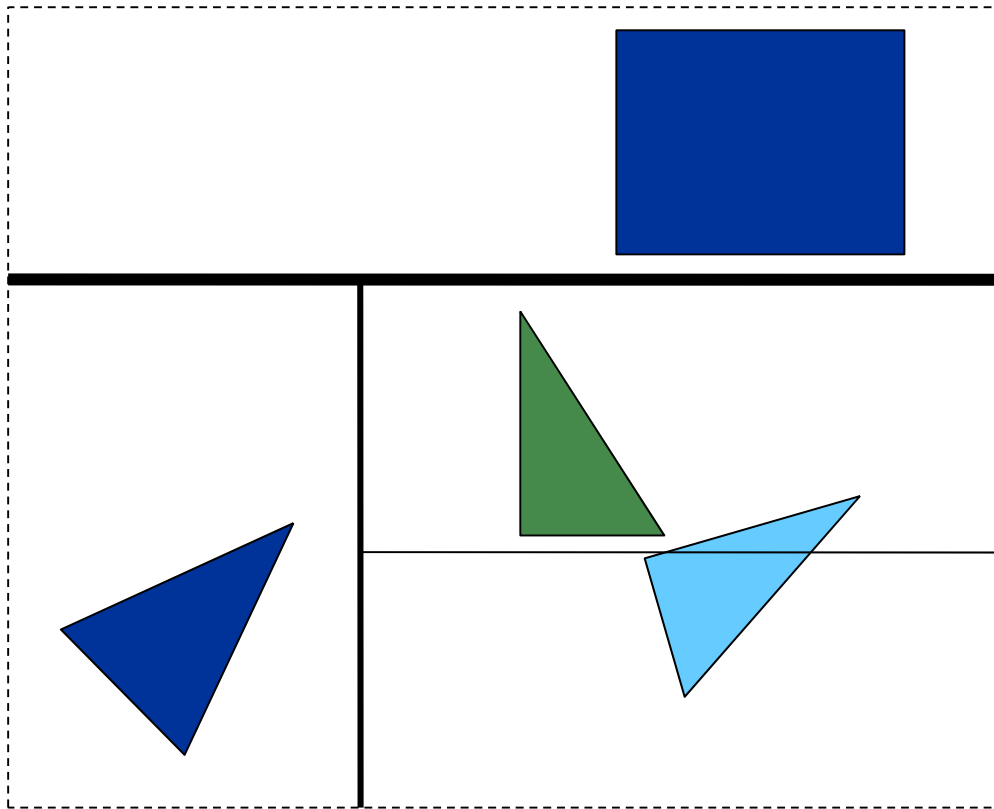


# Kd-tree: Example



What about triangles overlapping the split?

# Kd-tree: Example



# Split Planes

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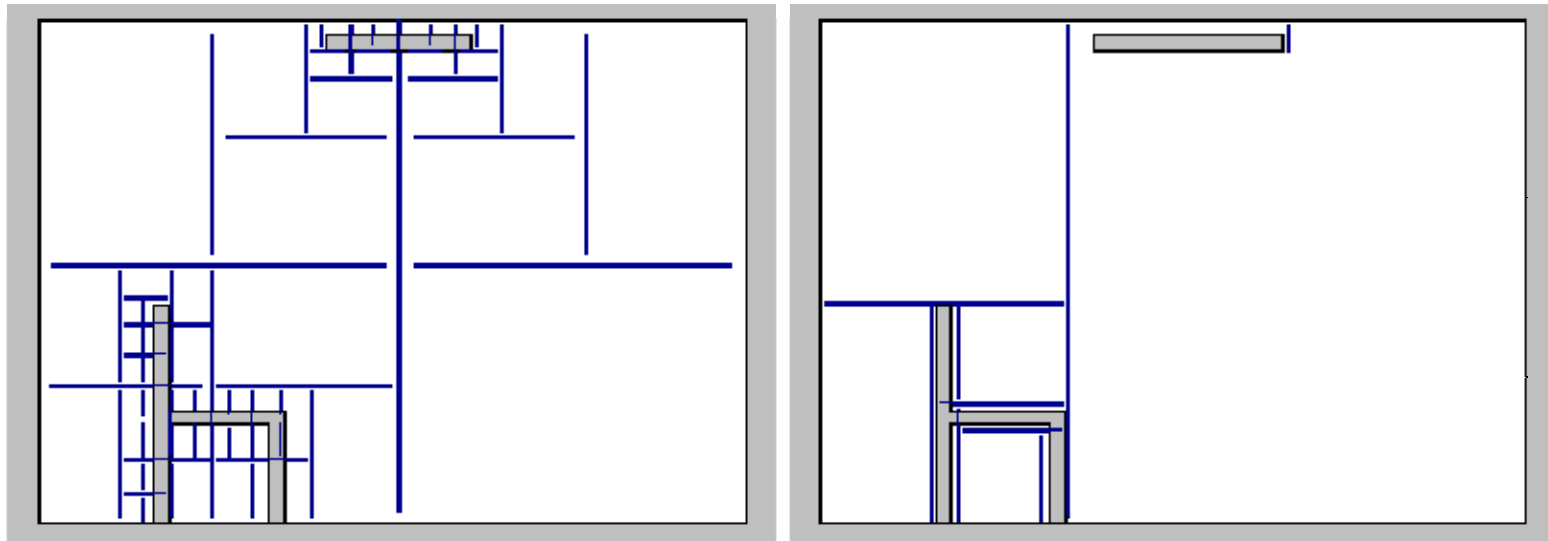
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- **How to select axis & split plane?**
  - Largest dimension, subdivide in middle
  - More advanced:
    - Surface area heuristic
- **Makes large difference**
  - 50%-100% higher *overall* speed

# Median vs. SAH

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*(from [Wald04])*

# Ray Tracing with kd-tree

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- Goal: find closest hit with scene
- Traverse tree front to back (starting from root)
- At each node:
  - If leaf: intersect with triangles
  - If inner: traverse deeper

# Other Optimizations

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- Shadow cache
- Adaptive depth control
- Lazy geometry loading/creation



# Distributed Ray Tracing [Cook et al. 84]

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- Cook et al. realized that ray-tracing, when combined with randomized sampling, which they called “jittering”, could be adapted to address a wide range of rendering problems:

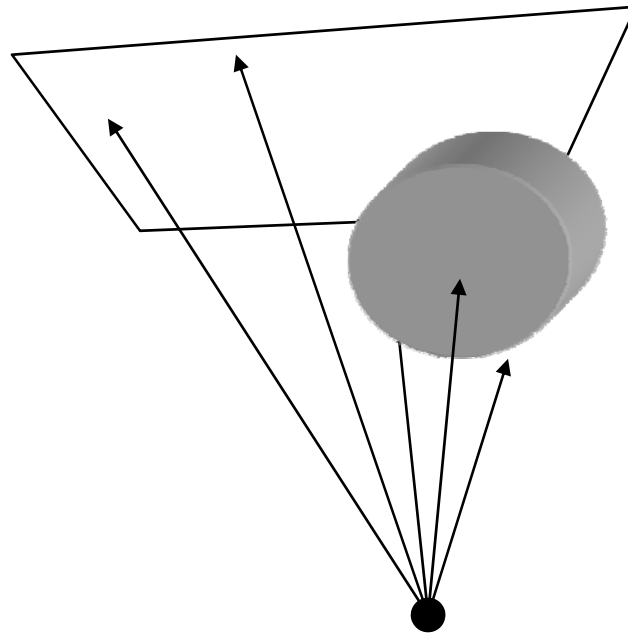


# Soft Shadows

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- Take many samples from area light source and take their average
  - Computes fractional visibility leading to penumbra



# Antialiasing

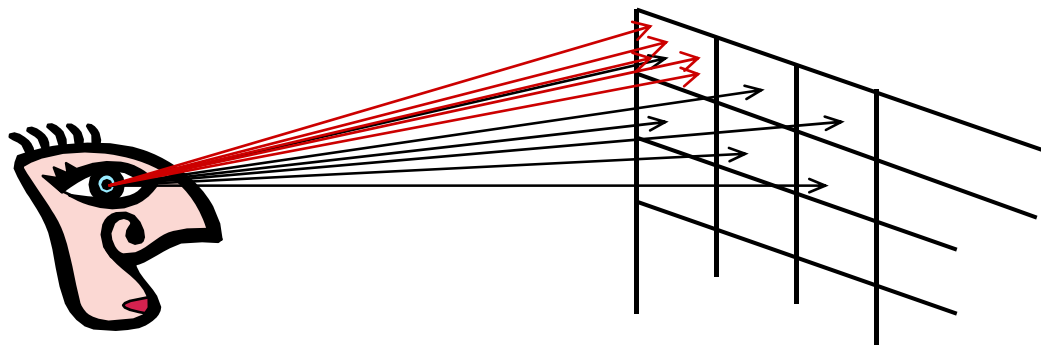
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- **The need to sample is problematic because sampling leads to aliasing**
- **Solution 1: super-sampling**
  - **Increases sampling rate, but does not completely eliminate aliasing**
  - **Difficult to completely eliminate aliasing without prefiltering because the world is not band-limited**

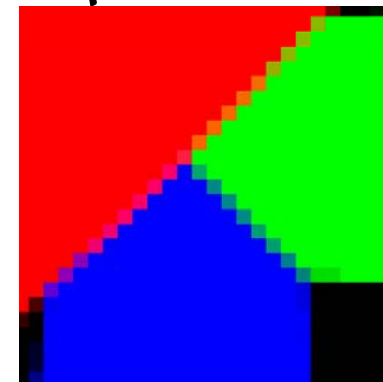
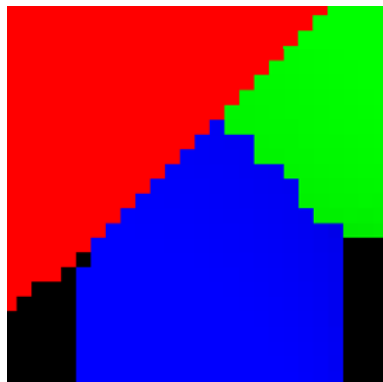
# Antialiasing

- **Solution 2: distribute the samples randomly**
  - Converts the aliasing energy to noise which is less objectionable to the eye



*Instead of casting one ray per pixel, cast several sub-sampling.*

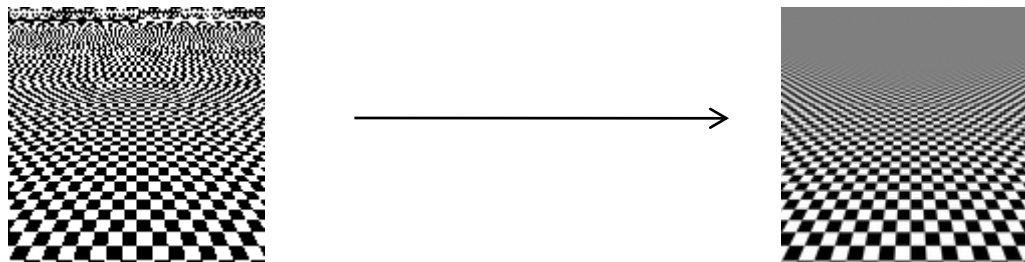
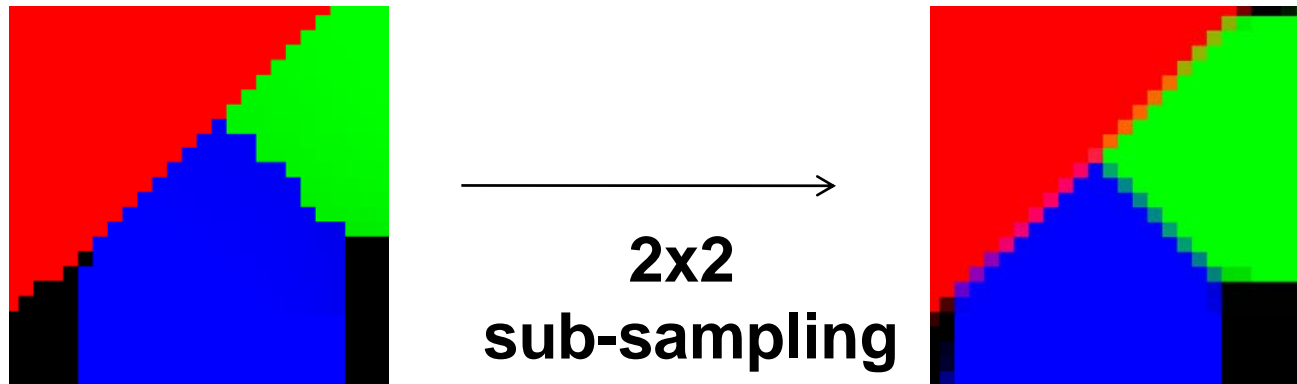
*Instead of uniform sub-sampling, jitter the pixels slightly off the grid.*



# Jittering Results for Antialiasing

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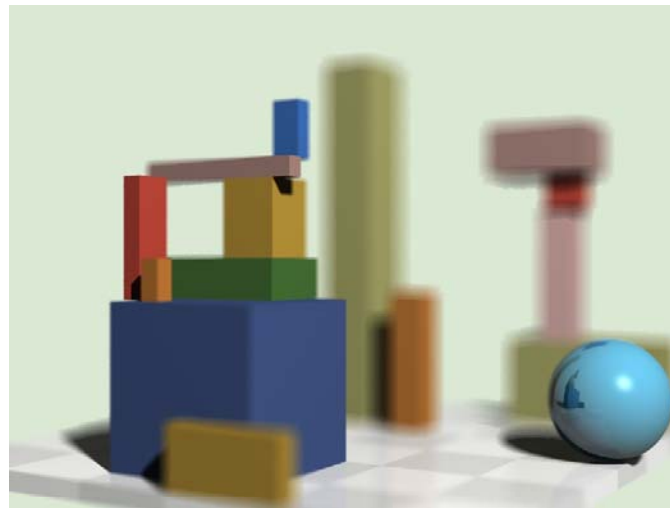


# Depth-of-Field

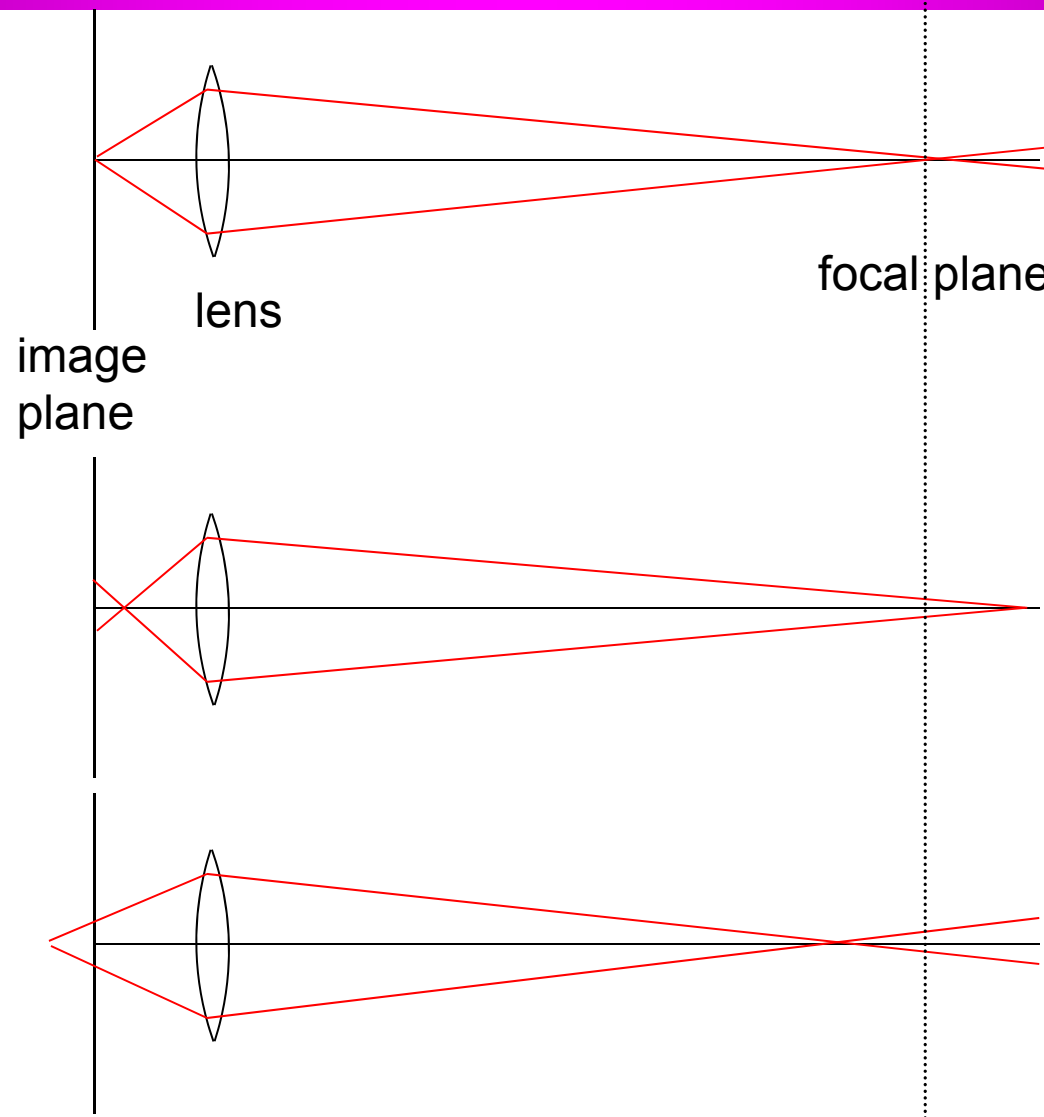
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- Rays don't have to all originate from a single point.
- Real cameras collect rays over an aperture
  - Can be modeled as a disk
  - Final image is blurred away from the focal plane
  - Gives rise to depth-of-field effects

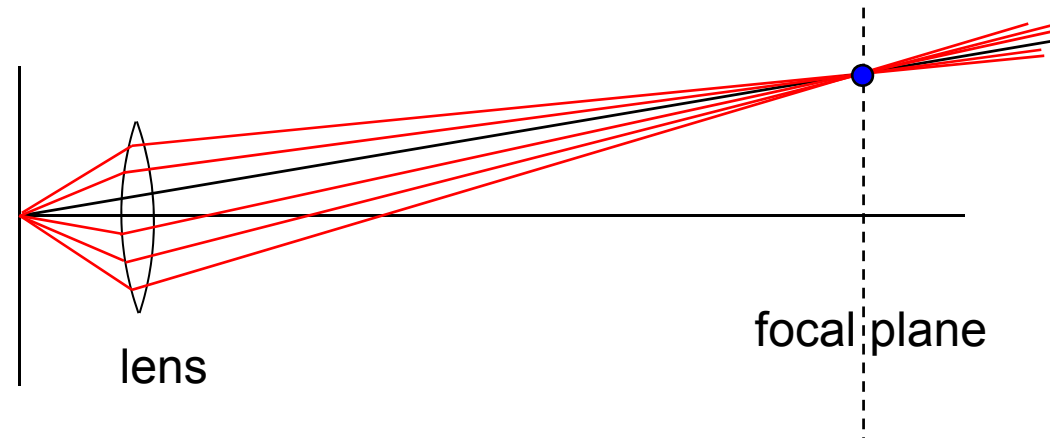


# Depth of Field



# Depth of Field

- Start with normal eye ray and find intersection with focal plane
- Choose jittered point on lens and trace line from lens point to focal point





# Motion Blur

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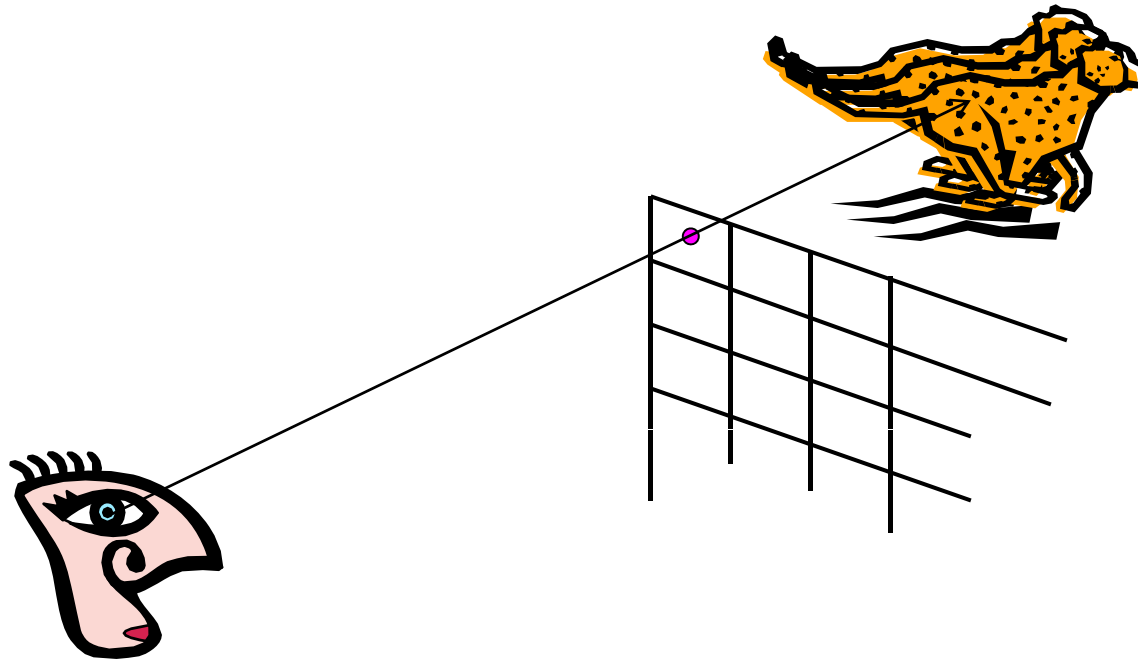


- **Jitter samples through time**
  - **Simulate the finite interval that a shutter is open on a real camera**

# Motion Blur

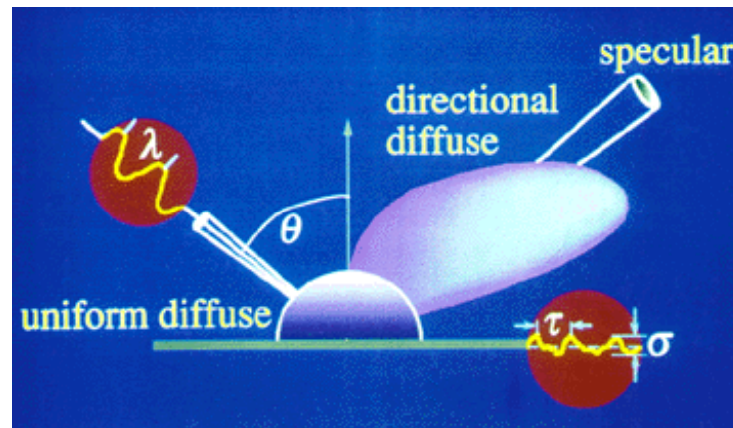
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# Complex Interreflection

- Model true reflection behavior as described by a full BRDF
- Randomly sample rays over the hemisphere, weight them by their BRDF value, and average them together
  - This technique is called “Monte Carlo Integration”



# CS680

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- **Advanced Computer Graphics**
  - Focus on rendering techniques that generate photo-realistic images
- **CS580 at spring 2013**
  - I'll teach high-quality rendering techniques