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# CS380: Computer Graphics

# Texture Mapping

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**Course URL:**  
<http://sglab.kaist.ac.kr/~sungeui/CG>

**KAIST**



# Class Objectives (CH. 11)

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- Texture mapping overview
- Texture filtering
- Various applications of texture mapping

# Texture Mapping

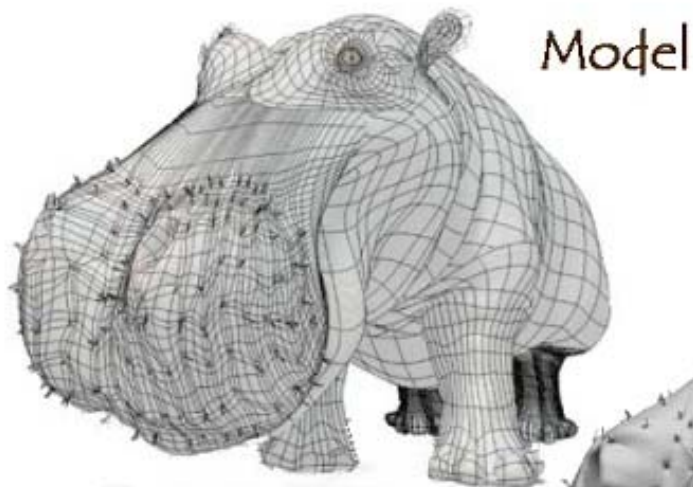
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- Requires lots of geometry to fully represent complex shapes of models
- Add details with image representations



# The Quest for Visual Realism



Model + Shading



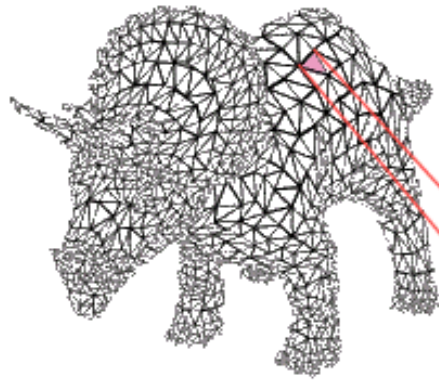
Model + Shading  
+ Textures

At what point  
do things start  
looking real?

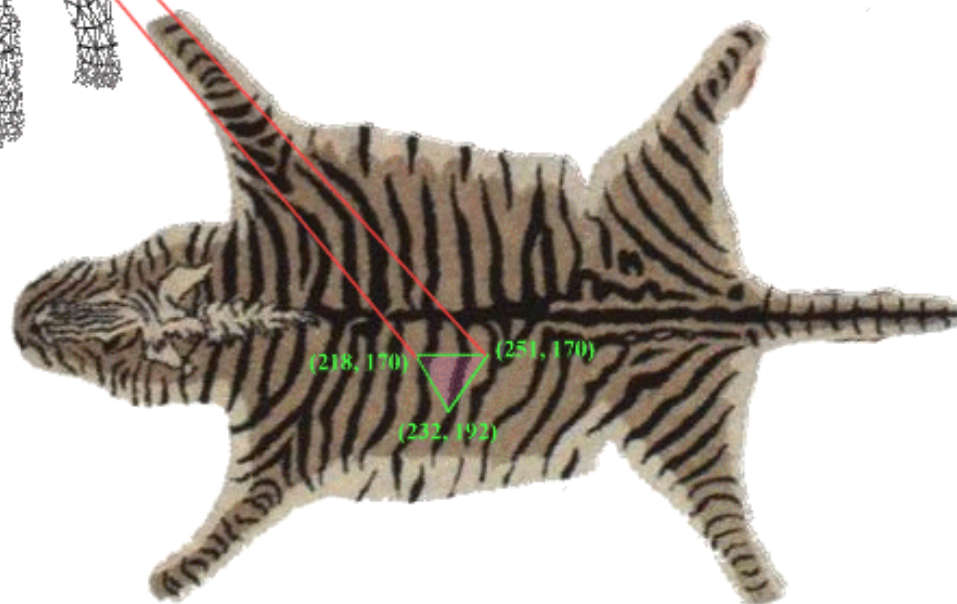


For more info on the computer artwork of Jeremy Birn  
see <http://www.3drender.com/jbirn/productions.html>

# Photo-Textures

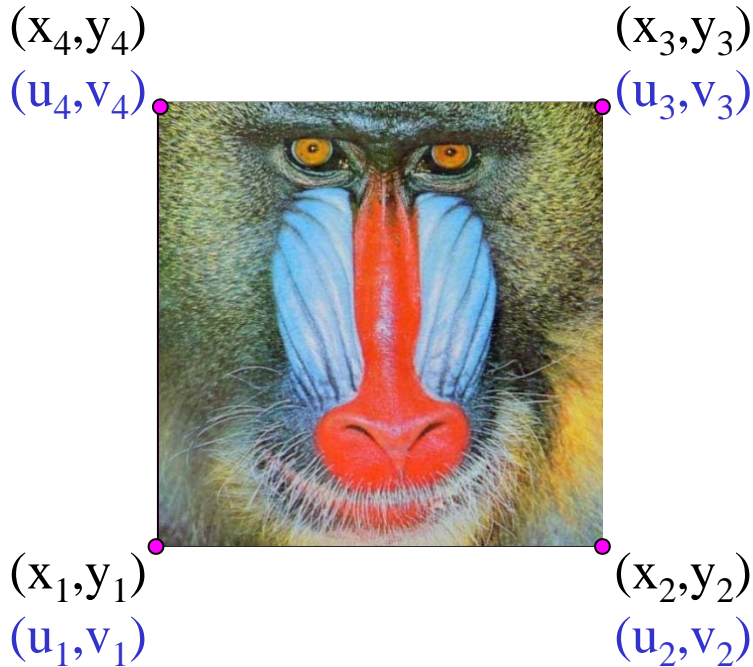


*For each triangle in the model  
establish a corresponding region  
in the phototexture*



*During rasterization interpolate the  
coordinate indices into the texture map*

# Texture Maps in OpenGL



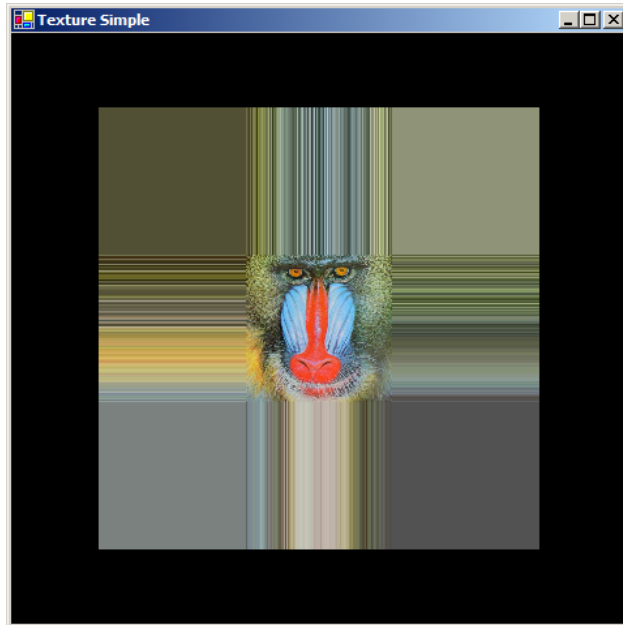
- Specify normalized texture coordinates at each of the vertices  $(u, v)$
- Texel indices  $(s, t) = (u, v) \cdot (\text{width}, \text{height})$

```
glBindTexture(GL_TEXTURE_2D, texID)
glBegin(GL_POLYGON)
    glTexCoord2d(0,1); glVertex2d(-1,-1);
    glTexCoord2d(1,1); glVertex2d( 1,-1);
    glTexCoord2d(1,0); glVertex2d( 1, 1);
    glTexCoord2d(0,0); glVertex2d(-1, 1);
glEnd()
```

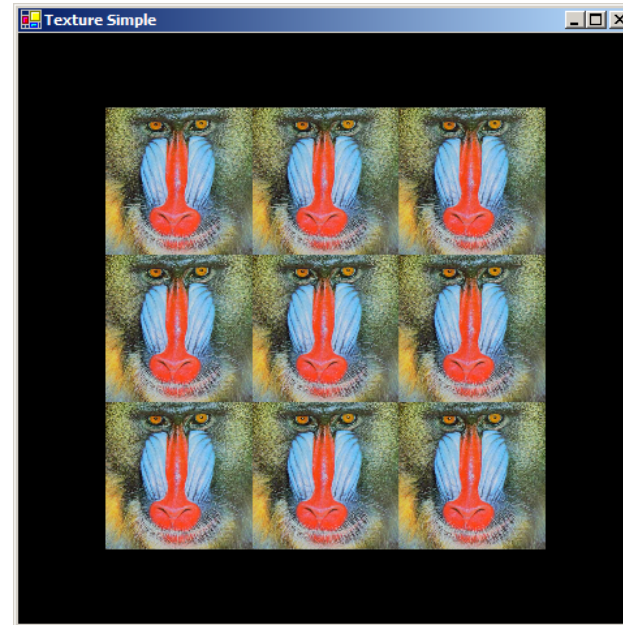
# Wrapping

- The behavior of texture coordinates outside of the range  $[0,1)$  is determined by the texture wrap options.

```
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_WRAP_S, wrap_mode )  
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_WRAP_T, wrap_mode )
```



GL\_CLAMP



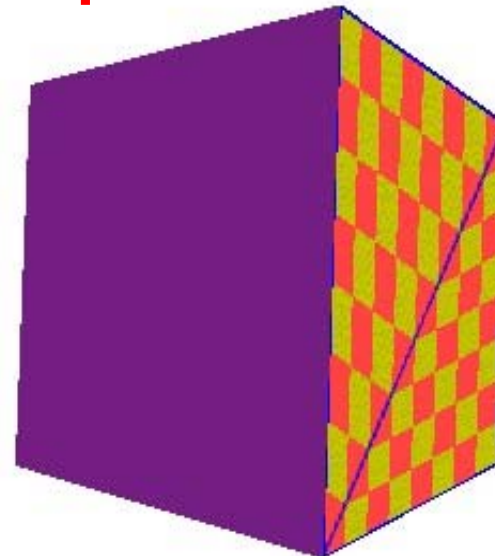
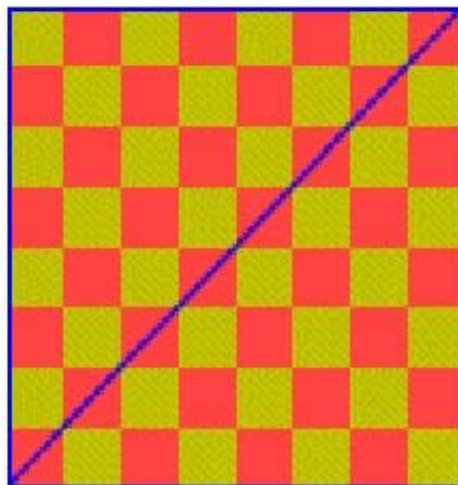
GL\_REPEAT

# Linear Interpolation of Texture Coordinates

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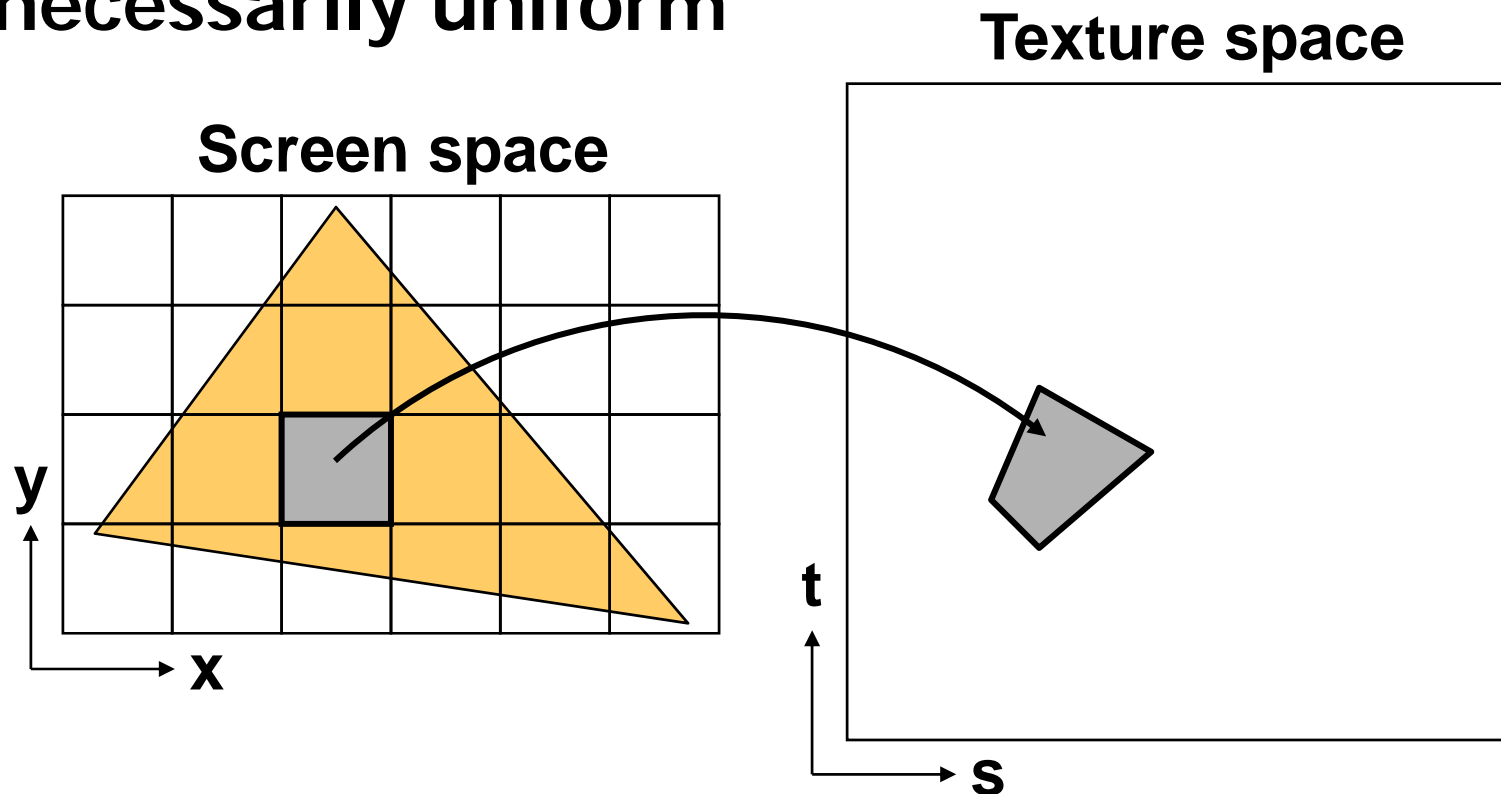
- Simple linear interpolation of  $u$  and  $v$  over a triangle in a screen space leads to unexpected results
  - Distorted when the triangle's vertices do not have the same depth
  - **Perspective-correct interpolation (interpolation in the object space) is implemented**





# Sampling Texture Maps

- The uniform sampling pattern in screen space corresponds to some sampling pattern in texture space that is not necessarily uniform

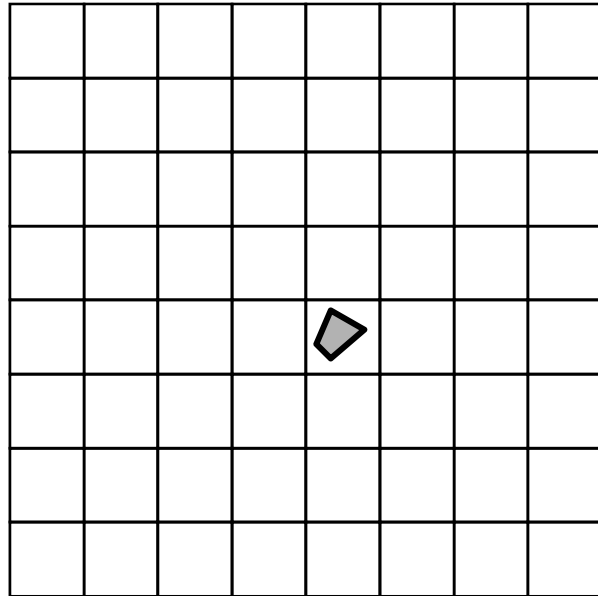


# Sampling Density Mismatch

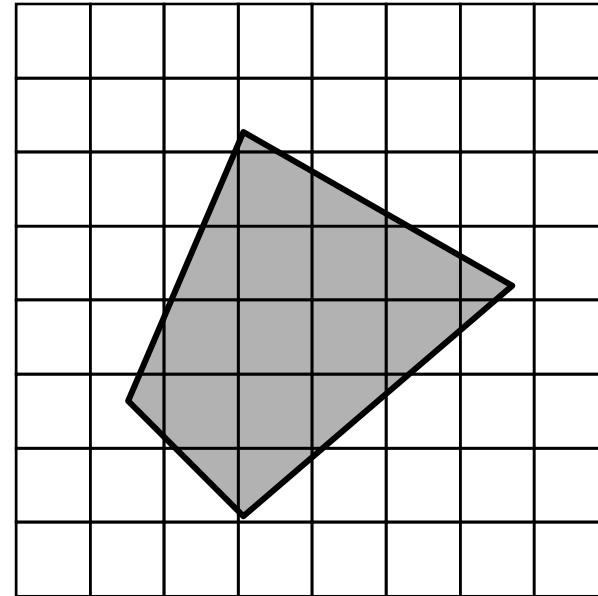
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- Sampling density in texture space rarely matches the sample density of the texture itself

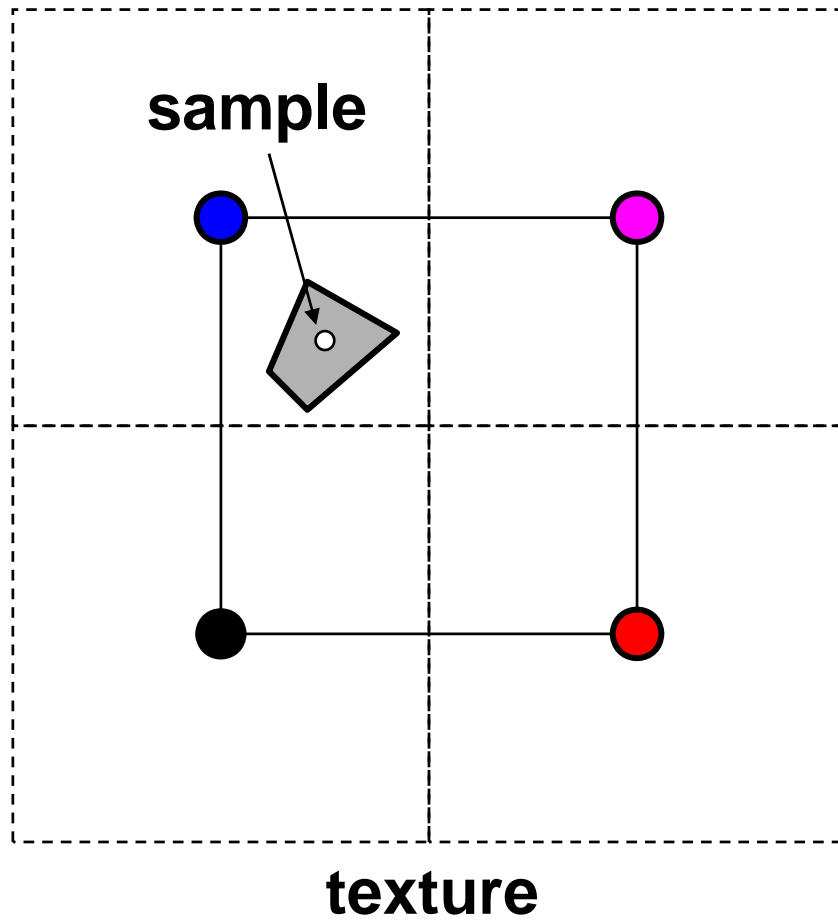


**Oversampling  
(Magnification)**



**Undersampling  
(Minification)**

# Handling Oversampling

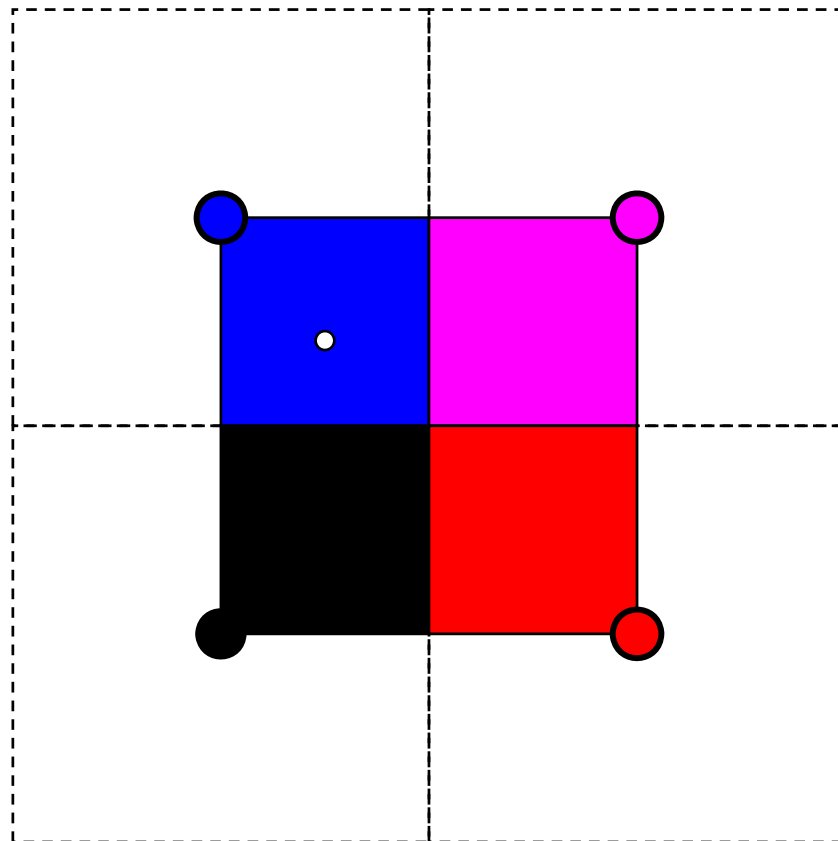


- How do we compute the color to assign to this sample?

# Handling Oversampling

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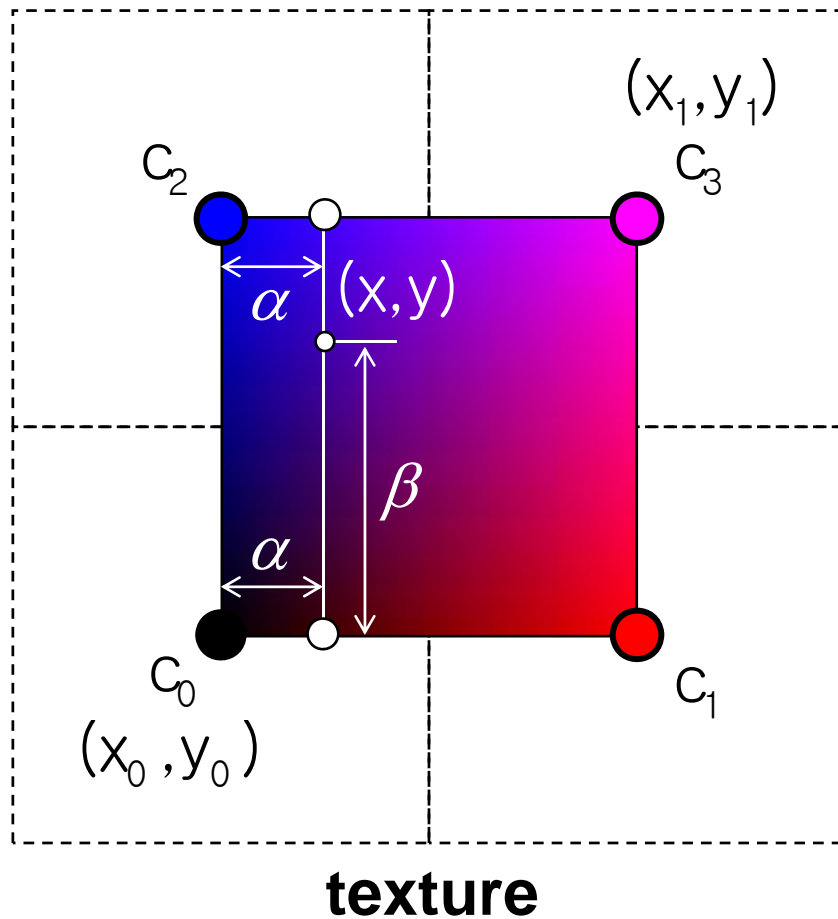
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texture

- How do we compute the color to assign to this sample?
- Nearest neighbor – take the color of the closest texel

# Handling Oversampling



- How do we compute the color to assign to this sample?

- Nearest neighbor – take the color of the closest texel

- Bilinear interpolation

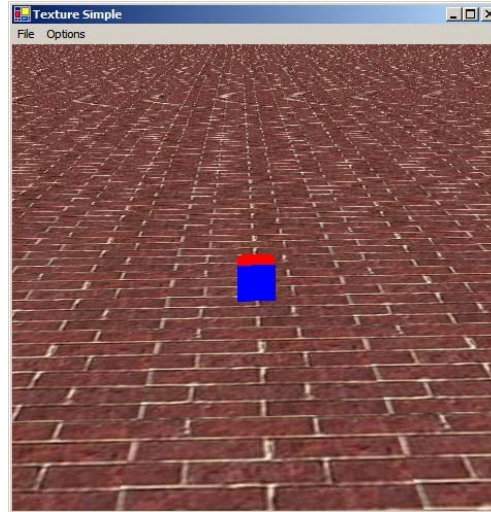
$$\alpha = \frac{x - x_0}{x_1 - x_0} \quad \beta = \frac{y - y_0}{y_1 - y_0}$$

$$c = ((1 - \alpha)c_0 + \alpha c_1)(1 - \beta) + ((1 - \alpha)c_2 + \alpha c_3)\beta$$

# Undersampling

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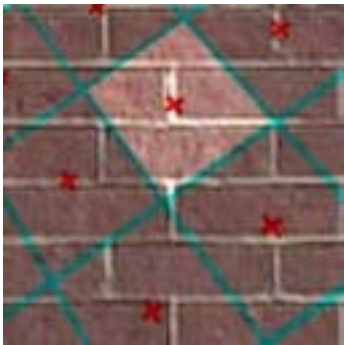
- Details in the texture tend to pop (disappear and reappear)
  - Mortar (white substances) in the brick
- High-frequency details lead to strange patterns
  - Aliasing

# Spatial Filtering

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- To avoid aliasing we need to prefilter the texture to remove high frequencies
  - Prefiltering is essentially a spatial integration over the texture
  - Integrating on the fly is expensive: perform integration in a pre-process



Samples and their extents

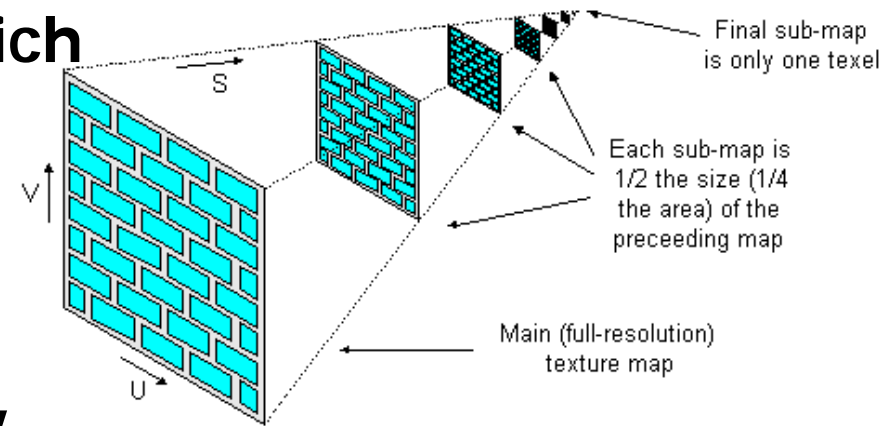


Proper filtering removes aliasing

# MIP Mapping

- MIP is an acronym for the Latin phrase *multum in parvo*, which means "many in one place"

- Constructs an *image pyramid*
- Each level is a prefiltered version of the level below resampled at half the frequency



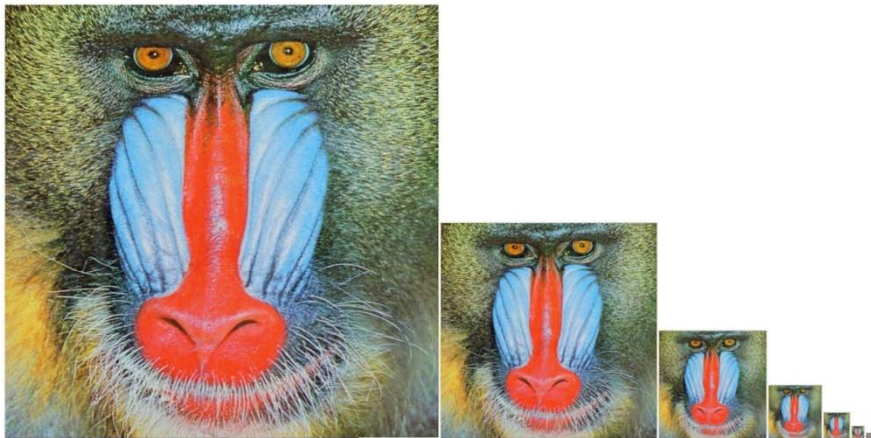
- While rasterizing use the level with the sampling rate closest to the desired sampling rate
  - Can also interpolate between pyramid levels
- How much storage overhead is required?

$$\text{mip map size} = \sum_{i=0}^{\infty} \left(\frac{1}{4}\right)^i = \frac{1}{1 - \frac{1}{4}} = \frac{4}{3}$$

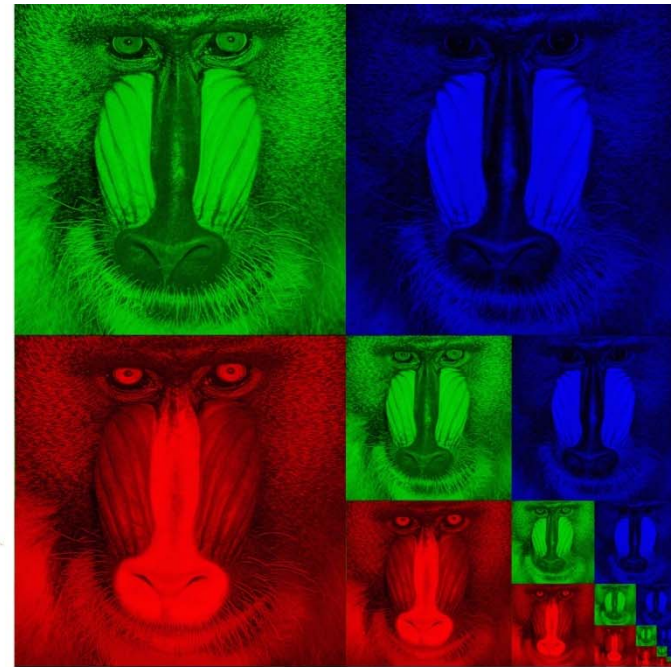



# Storing MIP Maps

- One convenient method of storing a MIP map is shown below
  - It also nicely illustrates the 1/3 overhead of maintaining the MIP map



10-level mip map



Memory format of a mip map 

# Finding the MIP Level

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- Use the projection of a pixel in screen into texture space to figure out which level to use

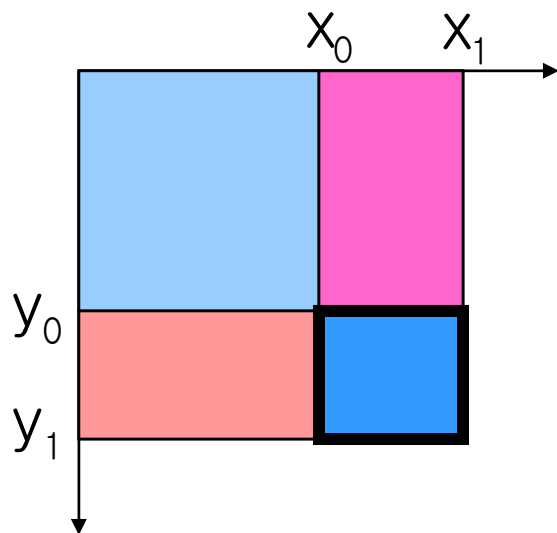
# Summed-Area Tables

- Another way performing the prefiltering integration on the fly
- Each entry in the summed area table is the sum of all entries above and to the left:

1	6	8	3
0	0	3	7
4	7	8	8
5	0	9	9

→

1	7	15	18
1	7	18	28
5	18	37	55
10	23	51	78



What is the sum of the highlighted region?

$$T(x_1, y_1) - T(x_1, y_0) - T(x_0, y_1) + T(x_0, y_0)$$

Divide out area  $(y_1 - y_0)(x_1 - x_0)$

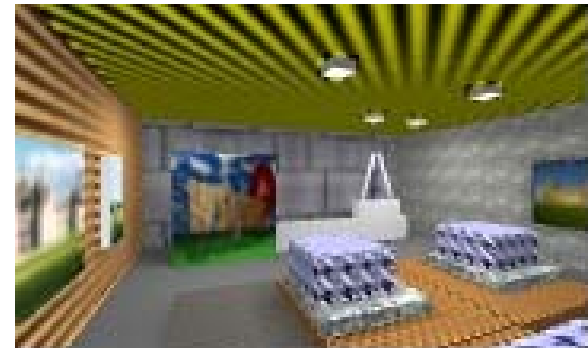
# Summed-Area Tables

- How much storage does a summed-area table require?
- Does it require more or less work per pixel than a MIP map?
- Can be implemented in a fragment shader

No  
Filtering



MIP  
mapping



Summed-  
Area  
Table



# Texture Filtering in OpenGL

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- Automatic creation

```
gluBuild2DMipmaps(GL_TEXTURE_2D, GL_RGBA, width, height,  
                 GL_RGBA, GL_UNSIGNED_BYTE, data)
```

- Filtering

```
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER, filter )
```

```
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER, filter )
```

where filter is:

GL\_NEAREST

GL\_LINEAR

GL\_LINEAR\_MIPMAP\_LINEAR

GL\_NEAREST\_MIPMAP\_NEAREST

GL\_NEAREST\_MIPMAP\_LINEAR

GL\_LINEAR\_MIPMAP\_NEAREST

inter-level

intra-level

# Uses of Texture Maps

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- **Texture maps are used to add complexity to a scene**
  - Easier to paint or capture an image than geometry
- **Model light**
- **Model geometry, etc**



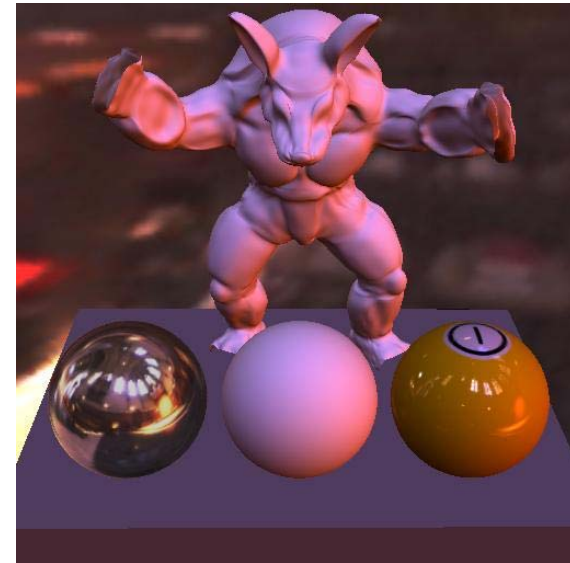
**One of key techniques to overcome various problems of rasterization techniques!**

# Modeling Lighting

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- **Light maps**
  - Supply the lighting directly
  - Good for static environments
- **Projective textures**
  - Can be used to simulate a spot light
  - Shadow maps
- **Environment maps**
  - A representation of the scene around an object
  - Good for reflection

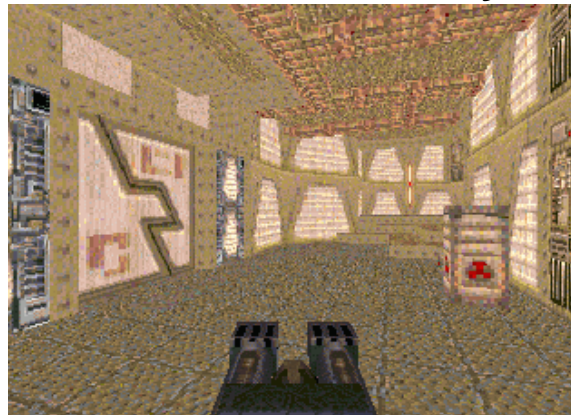


# Light Maps in Quake

- Light maps are used to store pre-computed illumination

	Texture Maps	Light Maps
Data	RGB	Intensity
Resolution	High	Low

Textures Only



Textures & Light Maps



Light map  
image by Nick  
Chirkov



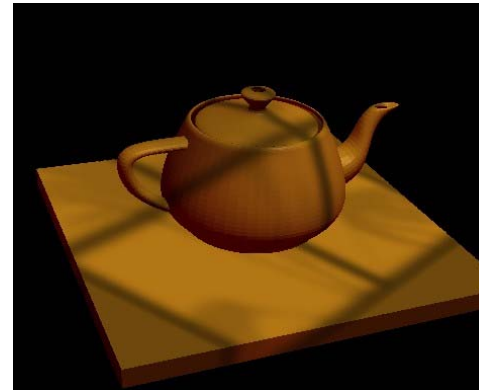
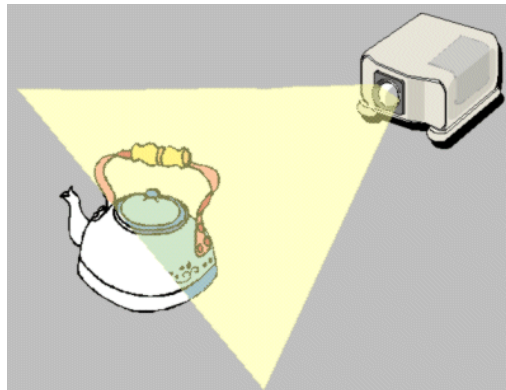


# Projective Textures

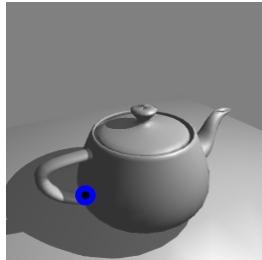
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- **Treat the texture as a slide in a projector**
  - A good model for shading variations due to illumination (cool spotlights)
- **Projectors work like cameras in reverse**
  - Camera: color of point in scene  $\rightarrow$  color of corresponding pixel
  - Projector: color of pixel  $\rightarrow$  color of corresponding point in the scene

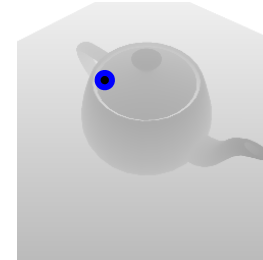


# Shadow Maps

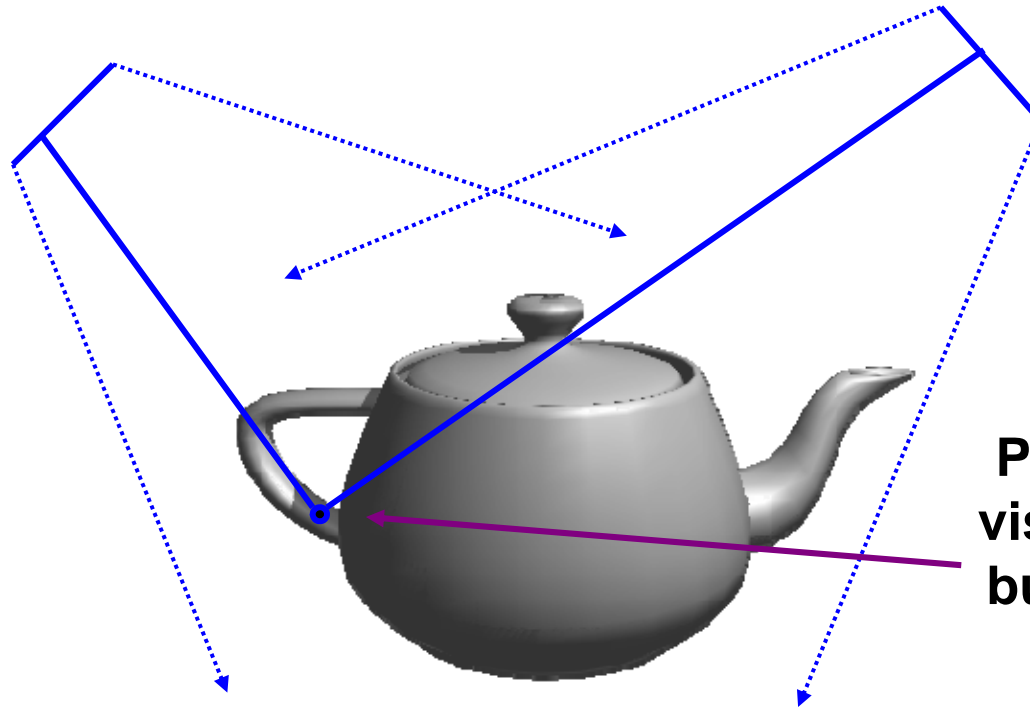


Eye

Use the depth map in the light view to determine if sample point is visible



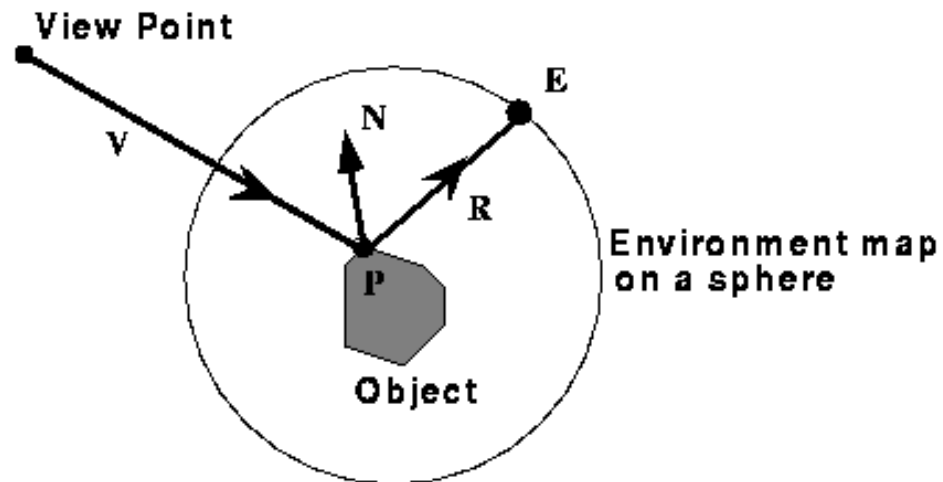
Light



Point in shadow visible to the eye, but not visible to the light

# Environment Maps

- Simulate complex mirror-like objects
  - Use textures to capture environment of objects
  - Use surface normal to compute texture coordinates



# Environment Maps - Example

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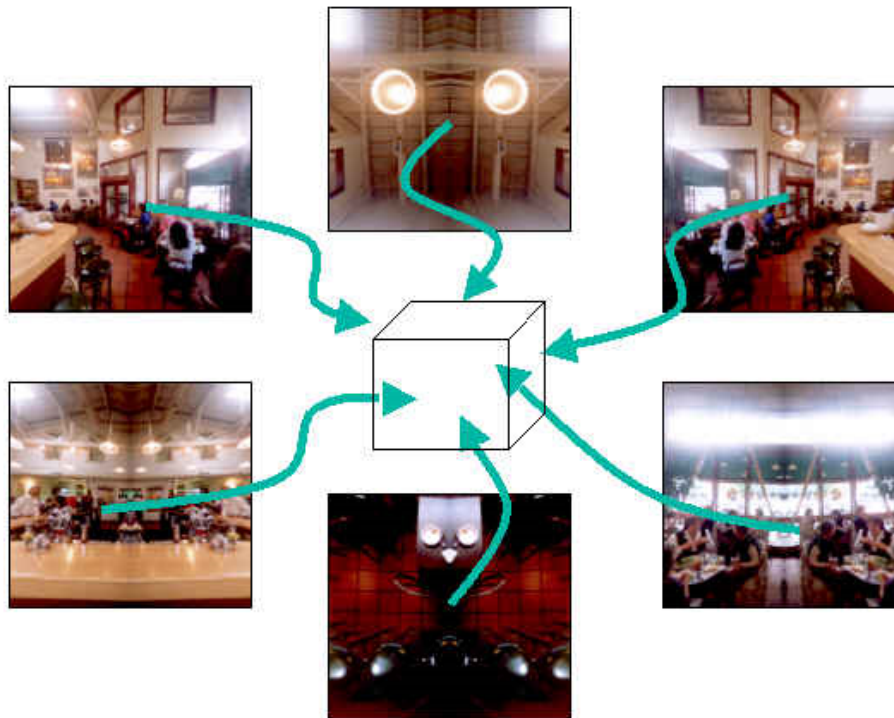
**T1000 in Terminator 2 from Industrial Light and Magic**

# Cube Maps

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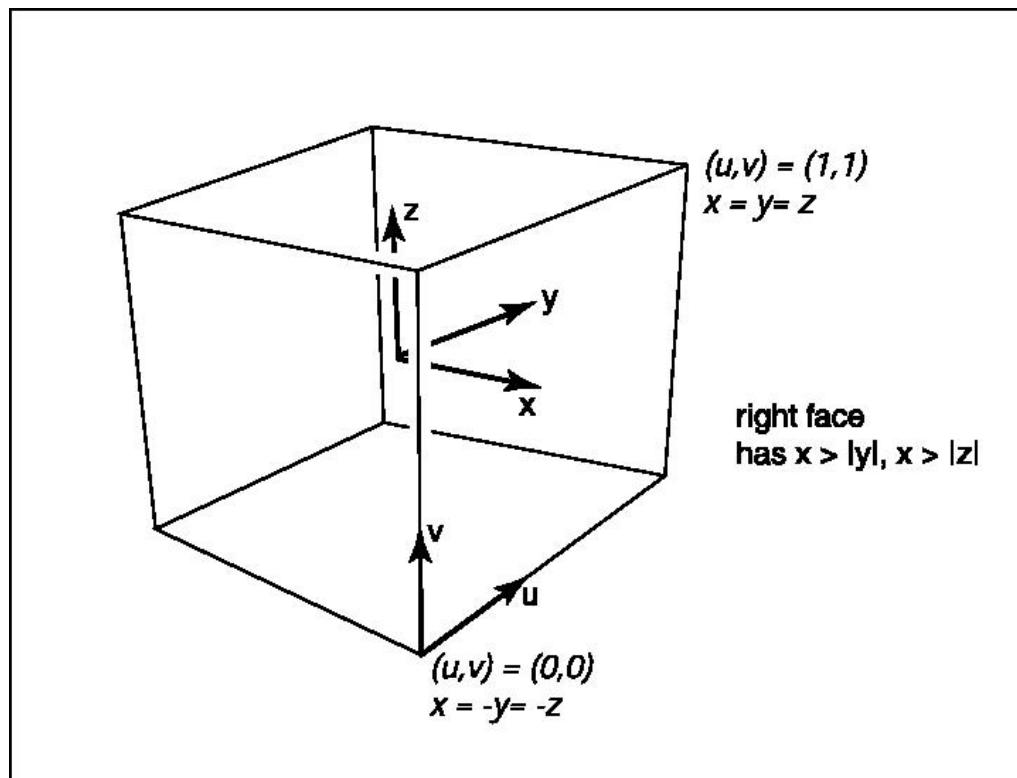
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- Maps a viewing direction  $\mathbf{b}$  and returns an RGB color
  - Use stored texture maps



# Cube Maps

- Maps a viewing direction  $\mathbf{b}$  and returns an RGB color
  - Assume  $\mathbf{b} = (x, y, z)$ ,



- Identify a face based on magnitude of  $x, y, z$

-For the right face, compute texture coord.  $(u, v)$

$$u = (y+x)/(2x)$$

$$v = (z+x)/(2x)$$

# Environment Maps - Problems

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- Expensive to update dynamically
- Not completely accurate
  - One of main reason that Cars (Pixar movie of 2006) used ray tracing



images from NVIDIA

Reflection of swimming pool is wrong

# Environment Maps - Problems

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- Expensive to update dynamically
- Not completely accurate
  - One of main reason that Cars (Pixar movie of 2006) used ray tracing





# Modeling Geometry

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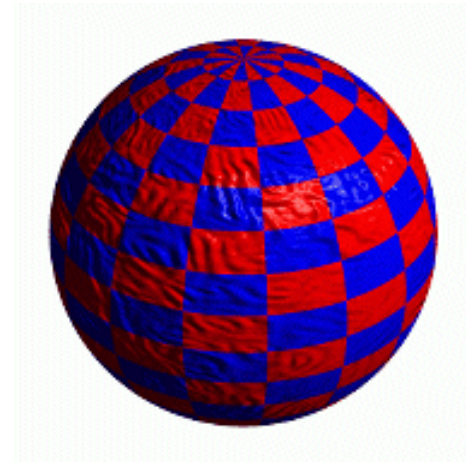
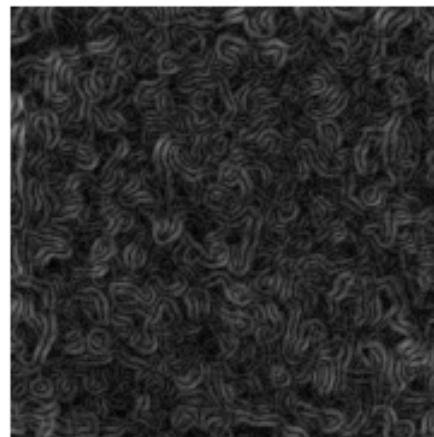
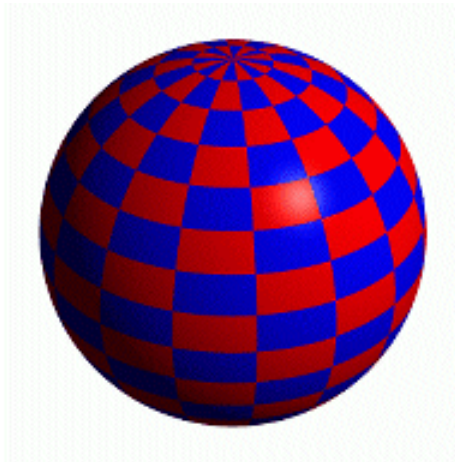
- **Store complex surface details in a texture rather than modeling them explicitly**
- **Bump maps**
  - Modify the existing normal
- **Normal maps**
  - Replace the existing normal
- **Displacement maps**
  - Modify the geometry
- **Opacity maps and billboards**
  - Knock-out portions of a polygon using the alpha channel

# Bump Mapping

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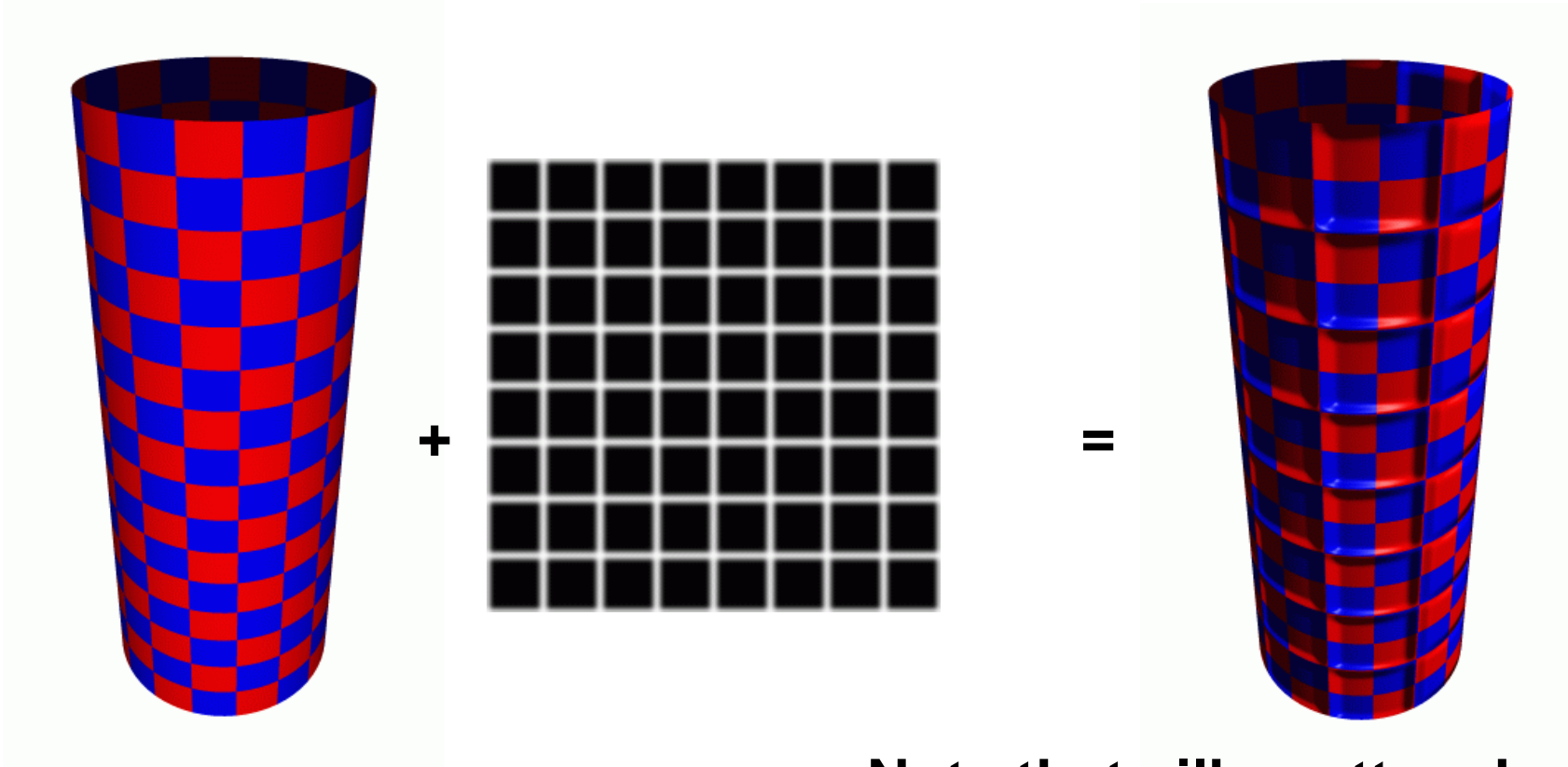
- **Modifies the normal not the actual geometry**
  - **Texture treated as a heightfield**
  - **Partial derivatives used to change the normal**
  - **Causes surface to appear deformed by the heightfield**



# More Bump Map Examples

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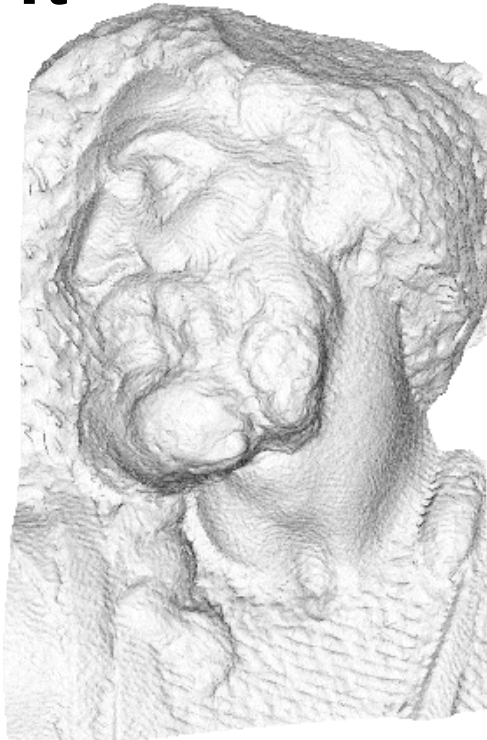
**Note that silhouette edge of the object not affected!**

# Normal Mapping

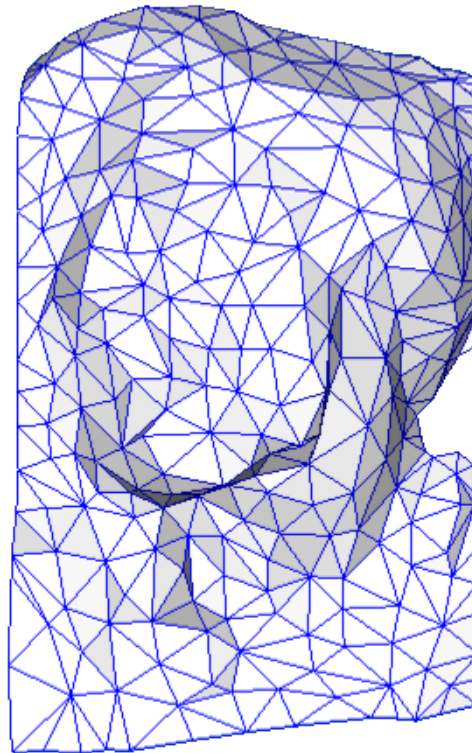
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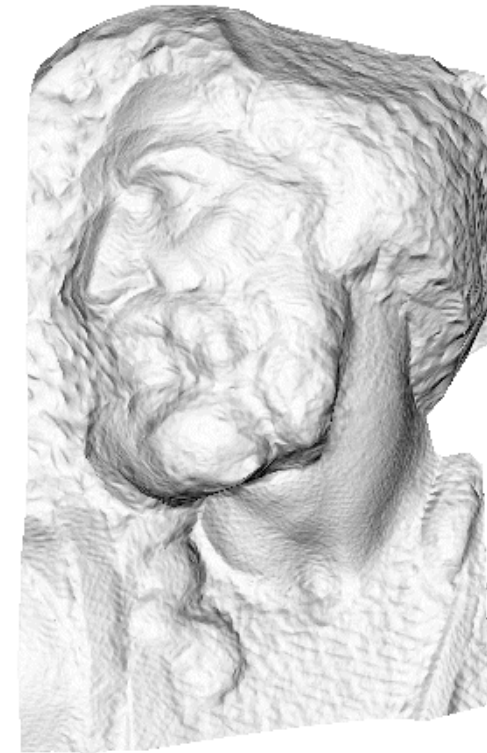
- Replaces the normal rather than tweaking it



original mesh  
4M triangles



simplified mesh  
500 triangles



simplified mesh  
and normal mapping  
500 triangles

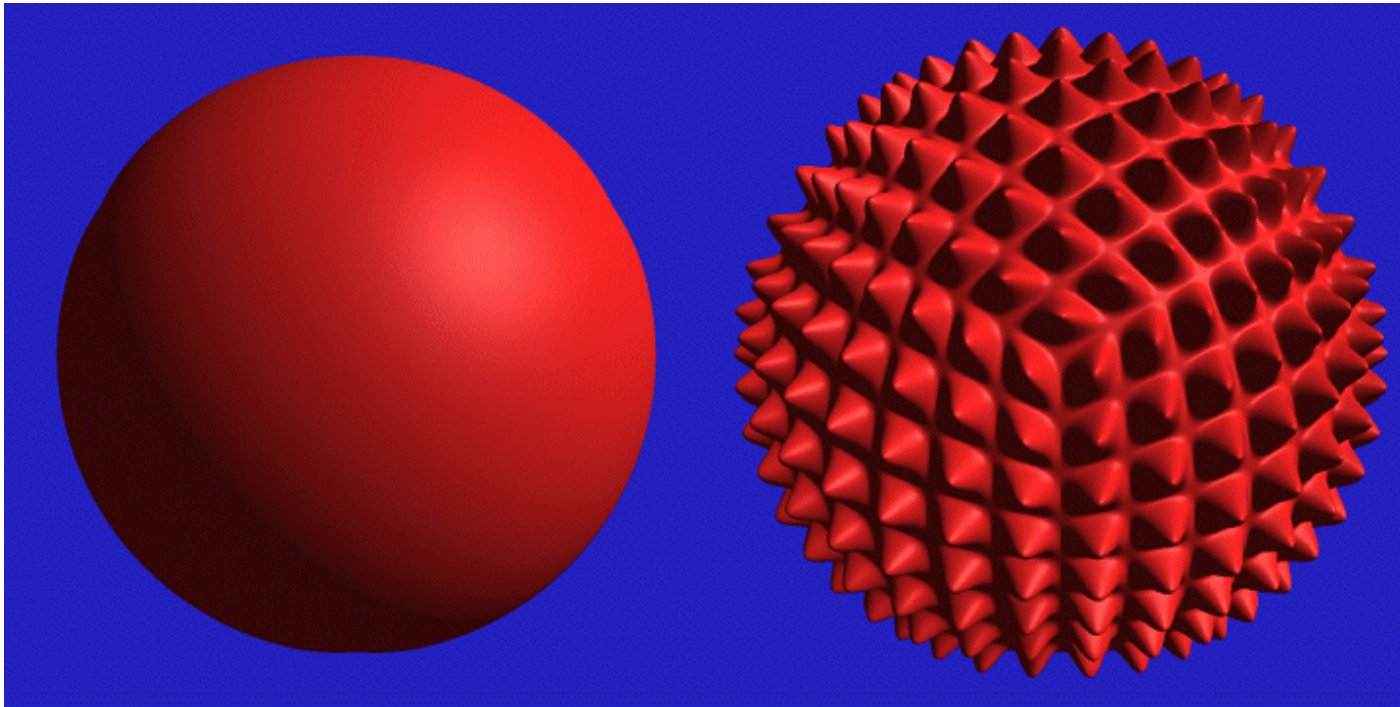


# Displacement Mapping

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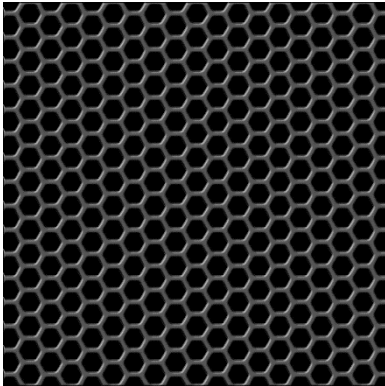
- Texture maps can be used to actually move surface points



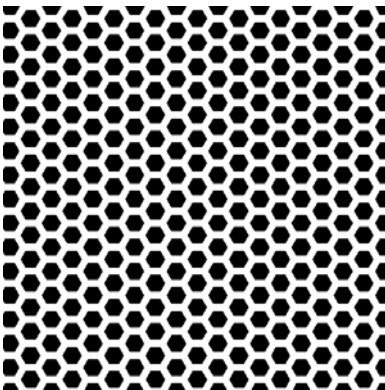
# Opacity Maps

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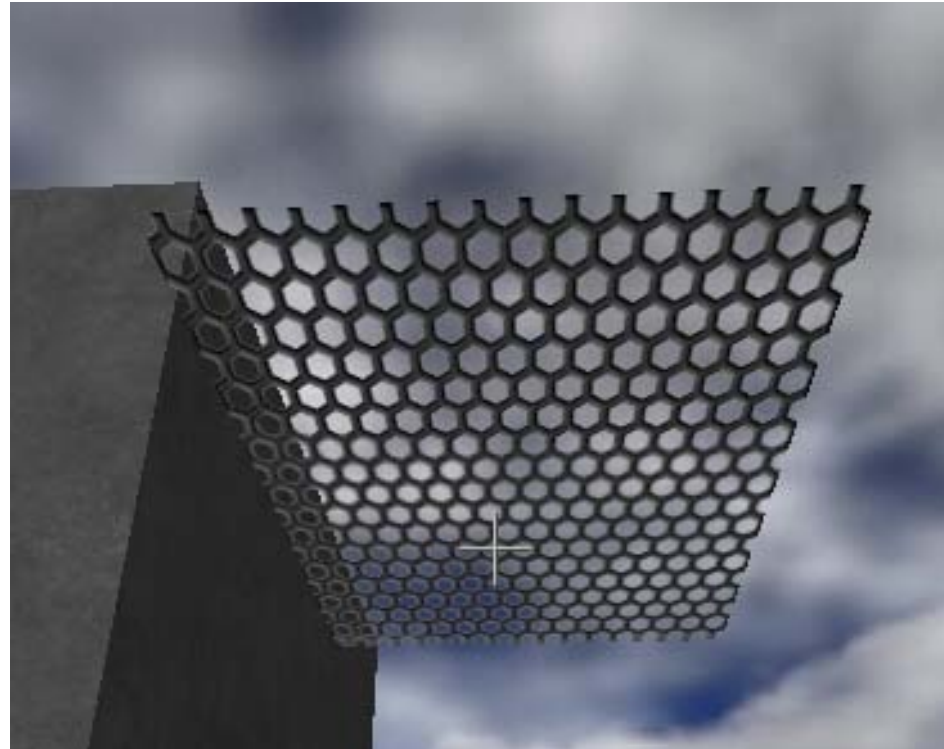
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RGB channels



alpha channel

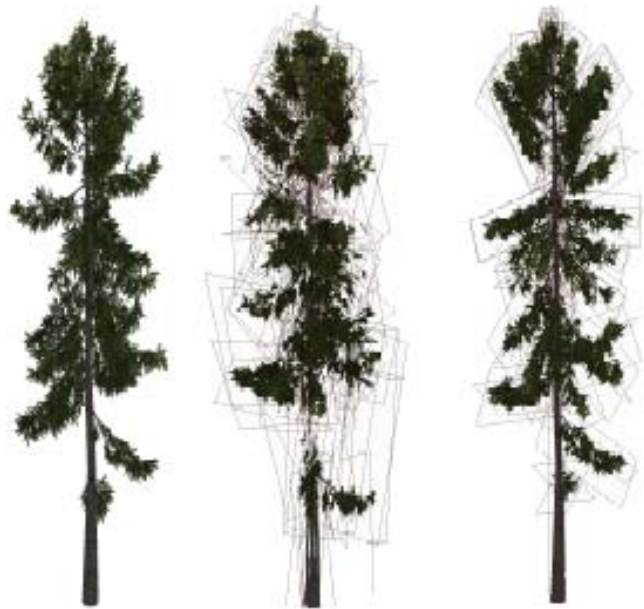


Use the alpha channel to make portions of the texture transparent

# Billboards

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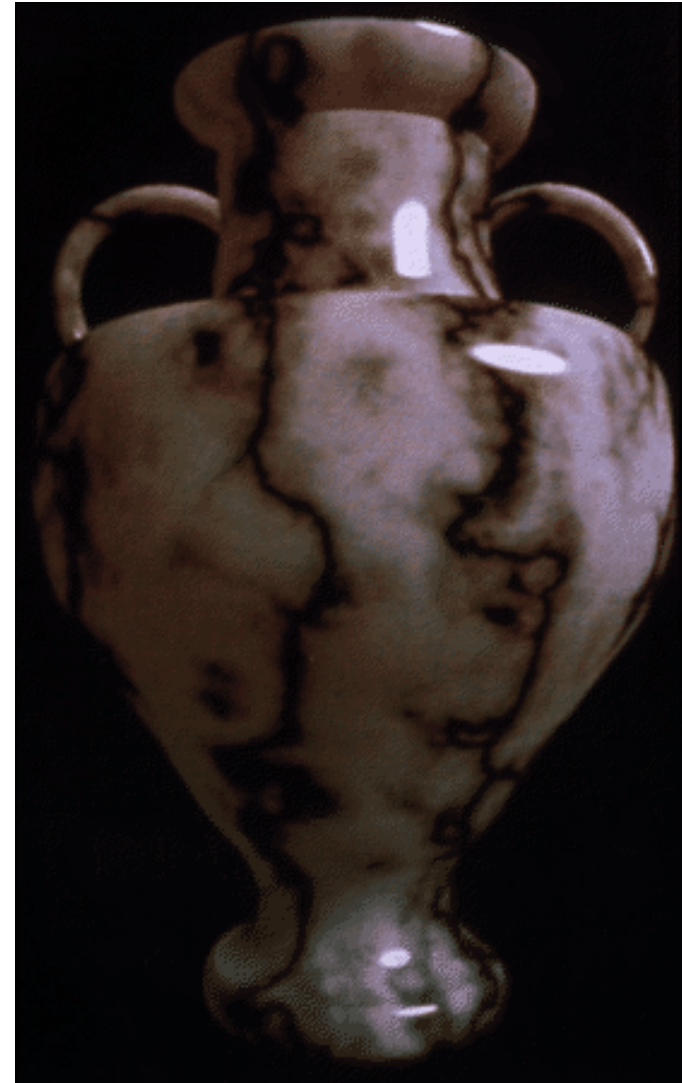
Replace complex geometry with polygons  
texture mapped with transparent textures

# 3D or Solid Textures

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- **Solid textures are three dimensional assigning values to points in 3 space**
  - **Very effective at representing some types of materials such as marble and wood**
- **Generally, solid textures are defined procedural functions rather than tabularized functions as used in 2D**





# Class Objectives were:

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- Texture mapping overview
- Texture filtering
- Various applications of texture mapping

# Next Time

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- **Visibility and ray tracing**

# Homework

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- **Go over the next lecture slides before the class**
- **No more video abstract submissions on June**

# Any Questions?

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- **Come up with one question on what we have discussed in the class and submit at the end of the class**
  - 1 for already answered questions
  - 2 for all the other questions
- **Submit at least four times during the whole semester**