CS580: Monte Carlo Ray Tracing:

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http://sgvr.kaist.ac.kr/~sungeui/GCG



Project Guidelines: Project Topics

- Any topics related to the course theme are okay
 - You can find topics by browsing recent papers



Expectations

- Mid-term project presentation
 - Introduce problems and explain why it is important
 - Give an overall idea on the related work
 - Explain what problems those existing techniques have
 - (Optional) explain how you can address those problems
 - Explain roles of each member



Expectations

- Final-term project presentation
 - Cover all the materials that you talked for your mid-term project
 - Present your ideas that can address problems of those state-of-the-art techniques
 - Give your qualitatively (or intuitive) reasons how your ideas address them
 - Also, explain expected benefits and drawbacks of your approach
 - (Optional) backup your claims with quantitative results collected by some implementations
 - Explain roles of each members



A few more comments

- Start to implement a paper, if you don't have any clear ideas
 - While you implement it, you may get ideas about improving it

 Utilize any existing materials (codes) with proper ack.



Project evaluation sheet

You name:

ID:

Score table: higher score is better.

Speaker	Novelty of the project and idea (1 ~ 5)	Practical benefits of the method (1 ~ 5)	Completeness level of the project (1 ~ 5)	Total score (3 ~ 15)	Role of each student is clear and well balanced? (Yes or No)
XXX					
YYY					

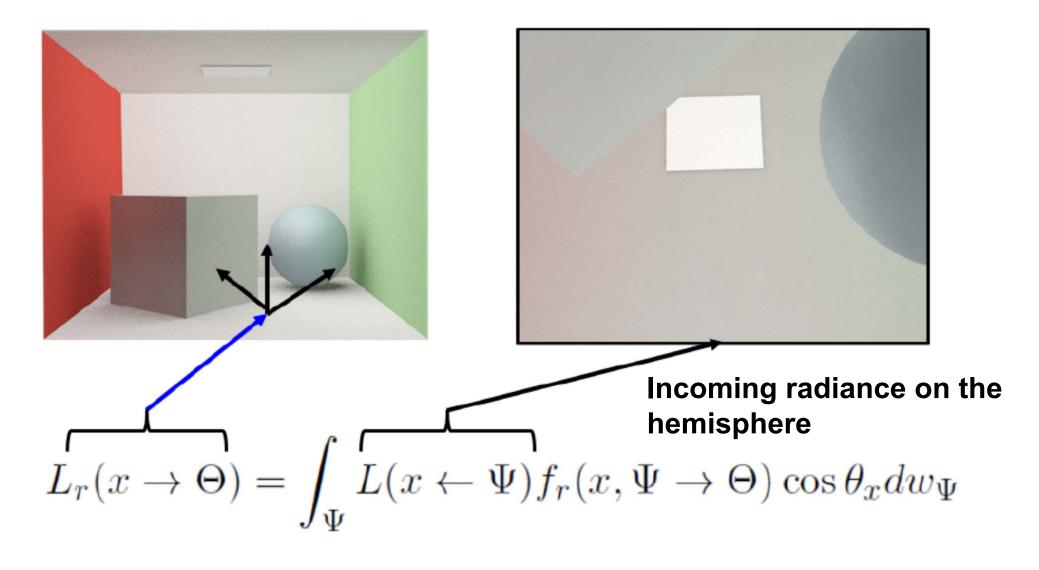


Class Objectives

- Understand a basic structure of Monte Carlo ray tracing
 - Russian roulette for its termination
 - Path tracing
 - Biased techniques



Rendering Equation

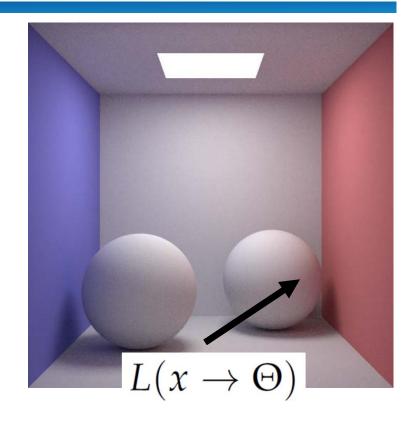




Evaluation

- To compute $L(x \to \Theta)$:
 - Check $L_e(x \to \Theta)$

• Evaluate $L_r(x \to \Theta)$



$$L_r(x \to \Theta) = \int_{\Psi} L(x \leftarrow \Psi) f_r(x, \Psi \to \Theta) \cos \theta_x dw_{\Psi}$$



Evaluation

Use Monte Carlo

 Generate random directions on hemisphere Ψ using pdf p(Ψ)

$$L_r(x \to \Theta) = \int_{\Psi} L(x \leftarrow \Psi) f_r(x, \Psi \to \Theta) \cos \theta_x dw_{\Psi}$$

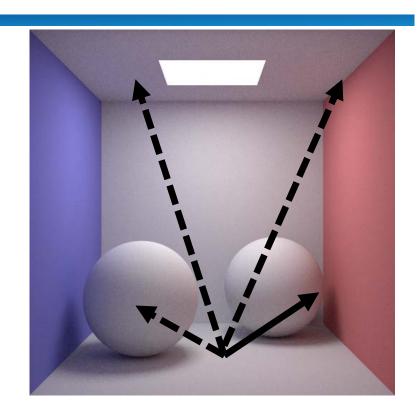
$$\hat{L}_r(x \to \Theta) = \frac{1}{N} \sum_{i=1}^N \frac{L(x \leftarrow \Psi_i) f_r(x, \Psi_i \to \Theta) \cos \theta_x}{p(\Psi_i)}$$

• How about $L(x \leftarrow \Psi_i)$?



Evaluation

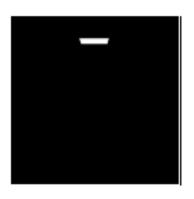
- How about $L(x \leftarrow \Psi_i)$?
- Perform ray casting backward
- Compute radiance from those visible points to x
 - Assume reciprocity



- Recursively perform the process
 - Each additional bounce supports one more indirect illumination



When to end recursion?









From kavita's slides

- Contributions of further light bounces become less significant
 - Max recursion
 - Some threshold for radiance value
- If we just ignore them, estimators will be biased



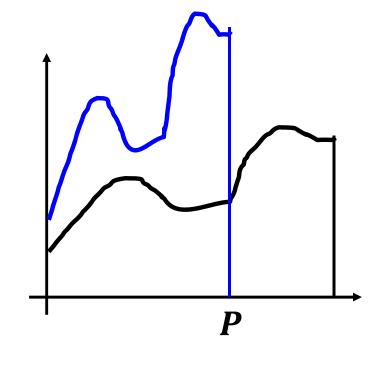
Russian Roulette

• Integral: Substitute y = Px

$$I = \int_0^1 f(x) dx = \int_0^P \frac{f(y/P)}{P} dy.$$

Estimator

$$\hat{I}_{roulette} = \begin{cases} \frac{f(x_i)}{P} & \text{if } x_i \leq P, \\ 0 & \text{if } x_i > P. \end{cases}$$



• Variance?



Russian Roulette

- Pick absorption probability, a = 1-P
 - Recursion is terminated

- P is commonly to be equal to the reflectance of the material of the surface
 - Water: 7%
 - Snow: 65%



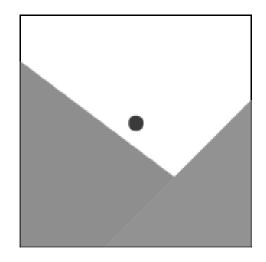
Algorithm so far

- Shoot primary rays through each pixel
- Shoot indirect rays, sampled over hemisphere
- Terminate recursion using Russian Roulette



Pixel Anti-Aliasing

- Compute radiance only at the center of pixel
 - Produce jaggies



- We want to evaluate using MC
- Simple box filter
 - The averaging method

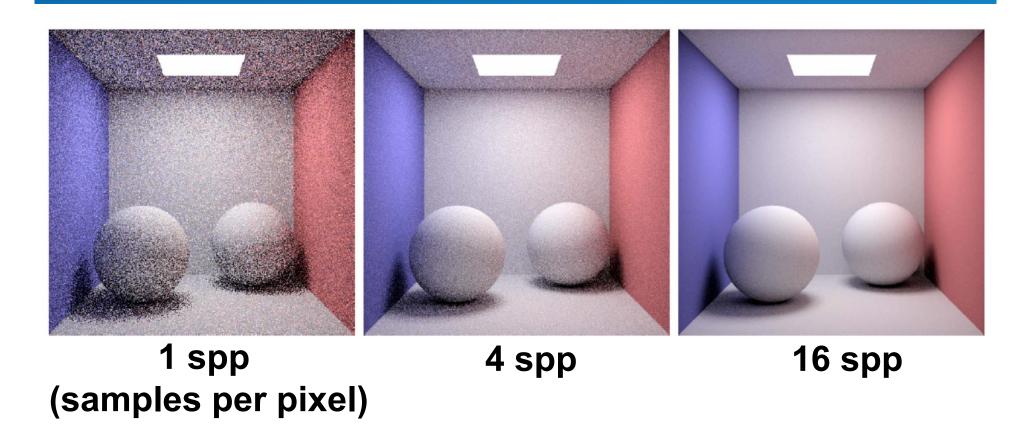


Stochastic Ray Tracing

- Parameters
 - Num. of starting ray per pixel
 - Num. of random rays for each surface point (branching factor)
- Path tracing
 - Branching factor = 1



Path Tracing



 Pixel sampling + light source sampling folded into one method



Algorithm so far

- Shoot primary rays through each pixel
- Shoot indirect rays, sampled over hemisphere
 - Path tracing shoots only 1 indirect ray
- Terminate recursion using Russian Roulette



Performance

- Want better quality with smaller # of samples
 - Fewer samples/better performance
 - Quasi Monte Carlo: well-distributed samples
 - Adaptive sampling
- See my book, if you are interested



Some Example



Uniform sampling (64 samples per pixel)

Adaptive sampling

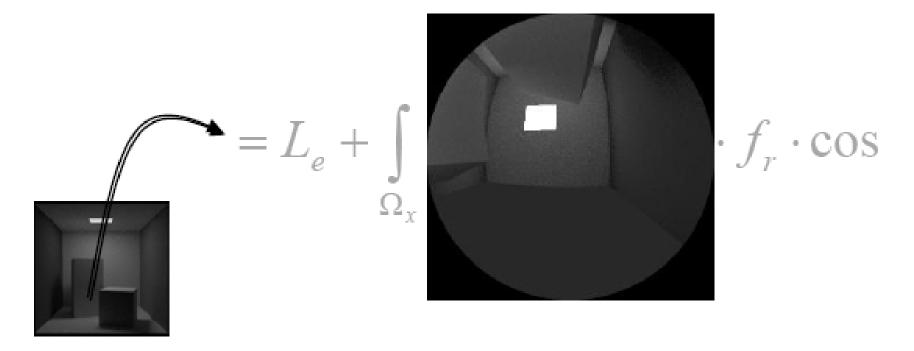
Reference



Importance Sampling

$$L(x \to \Theta) = L_e(x \to \Theta) + \int_{\Omega_x} f_r(\Psi \leftrightarrow \Theta) \cdot L(x \leftarrow \Psi) \cdot \cos(\Psi, n_x) \cdot d\omega_{\Psi}$$

Radiance from light sources + radiance from other surfaces



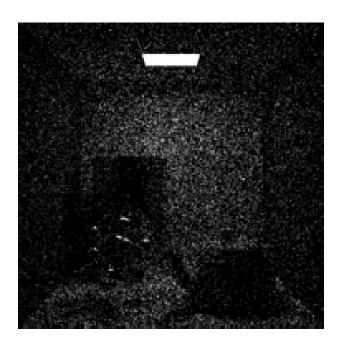
Importance Sampling

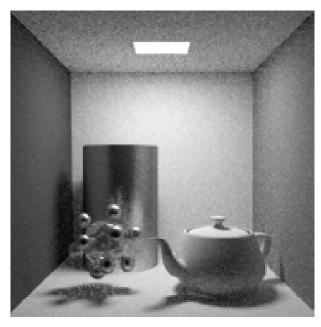
$$L(x \to \Theta) = L_e + L_{direct} + L_{indirect}$$

$$=L_e + \int_{\Omega_x} \mathbf{r} \cdot \mathbf{r} \cdot$$

 So ... sample direct and indirect with separate MC integration

Comparison





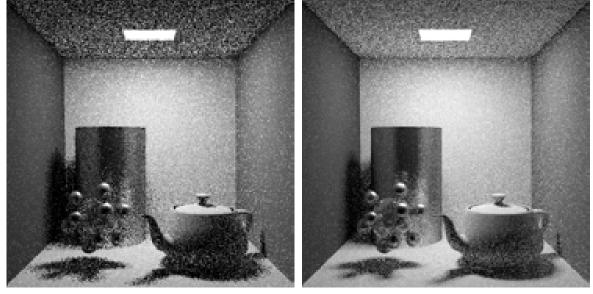
From kavita's slides

- With and without considering direct illumination
 - 16 samples / pixel



Rays per pixel

1 sample/ pixel



4 samples/ pixel

16 samples/ pixel



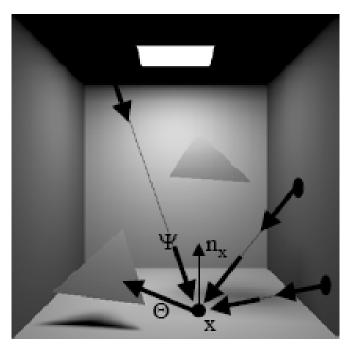
256 samples/ pixel

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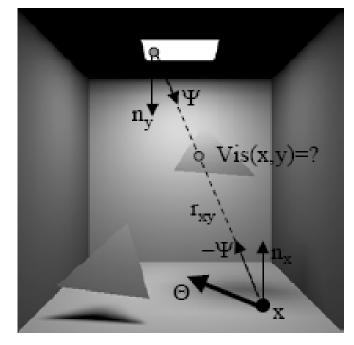
Direct Illumination

$$L(x \to \Theta) = \int_{A_{source}} f_r(x, -\Psi \leftrightarrow \Theta) \cdot L(y \to \Psi) \cdot G(x, y) \cdot dA_y$$

$$G(x, y) = \frac{\cos(n_x, \Theta)\cos(n_y, \Psi)Vis(x, y)}{r_{xy}^2}$$



hemisphere integration



area integration

Estimator for direct lighting

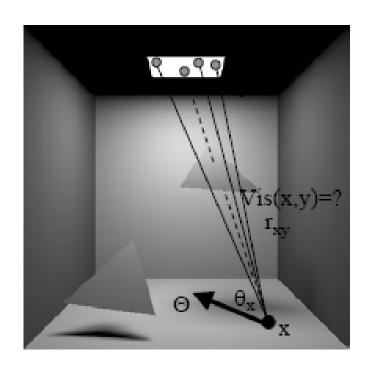
Pick a point on the light's surface with pdf
 p(y)

For N samples, direct light at point x is:

$$E(x) = \frac{1}{N} \sum_{i=1}^{N} \frac{f_r L_{source} \frac{\cos \theta_x \cos \theta_{\overline{y}_i}}{r_{x\overline{y}_i}^2} Vis(x, \overline{y}_i)}{p(\overline{y}_i)}$$

Generating direct paths

- Pick surface points y_i on light source
- Evaluate direct illumination integral



$$\langle L(x \to \Theta) \rangle = \frac{1}{N} \sum_{i=1}^{N} \frac{f_r(...)L(...)G(x, y_i)}{p(y_i)}$$

PDF for sampling light

Uniform

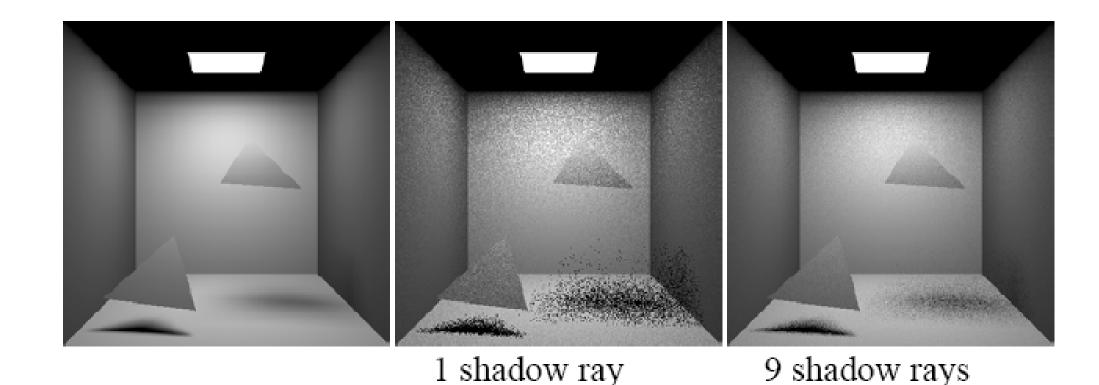
$$p(y) = \frac{1}{Area_{source}}$$

- Pick a point uniformly over light's area
 - Can stratify samples

Estimator:

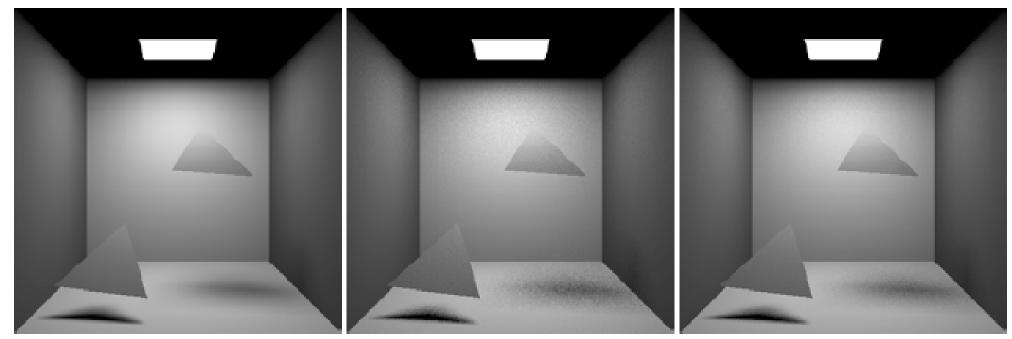
$$E(x) = \frac{Area_{source}}{N} \sum_{i=1}^{N} f_r L_{source} \frac{\cos \theta_x \cos \theta_{\overline{y}_i}}{r_{x\overline{y}_i}^2} Vis(x, \overline{y}_i)$$

More points ...



 $E(x) = \frac{Area_{source}}{N} \sum_{i=1}^{N} f_r L_{source} \frac{\cos \theta_x \cos \theta_{\bar{y}_i}}{r_{x\bar{y}_i}^2} Vis(x, \bar{y}_i)$

Even more points ...



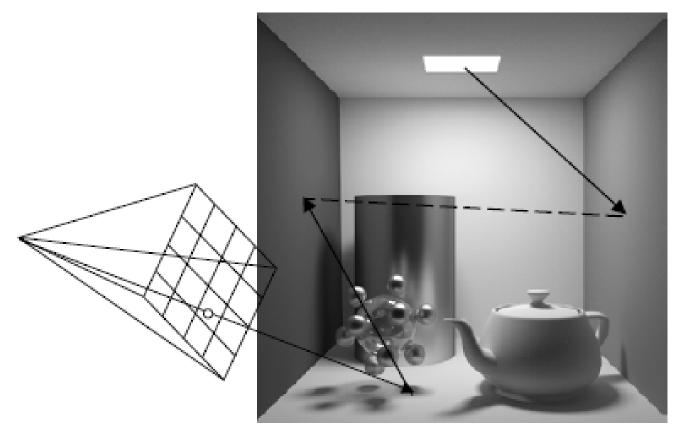
36 shadow rays

100 shadow rays

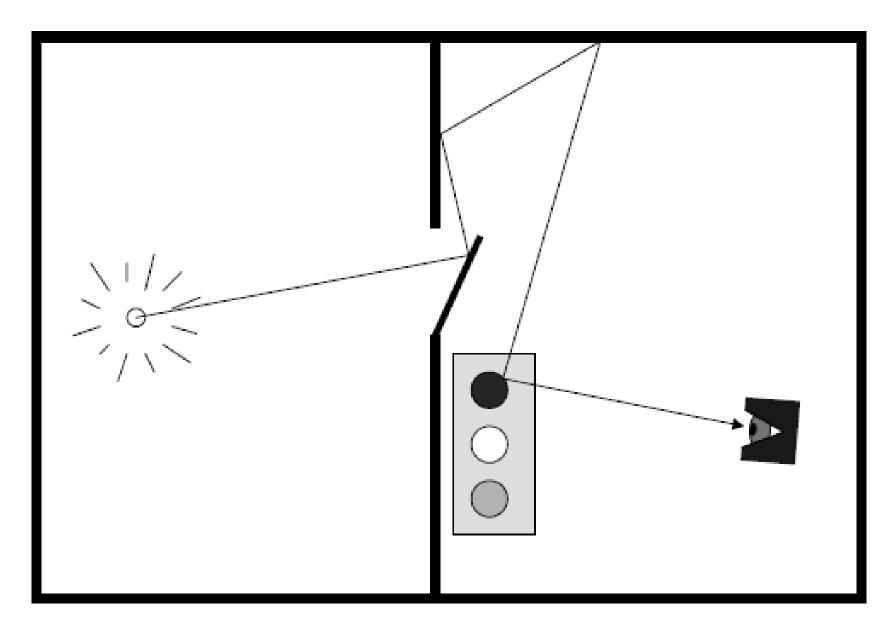
$$E(x) = \frac{Area_{source}}{N} \sum_{i=1}^{N} f_r L_{source} \frac{\cos \theta_x \cos \theta_{\overline{y}_i}}{r_{x\overline{y}_i}^2} Vis(x, \overline{y}_i)$$

Bidirectional Path Tracing

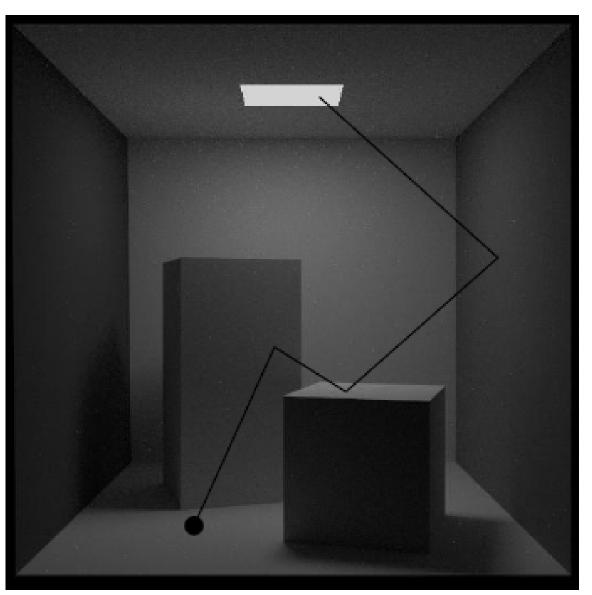
 Or paths generated from both camera and source at the same time ...!



 Connect endpoints to compute final contribution

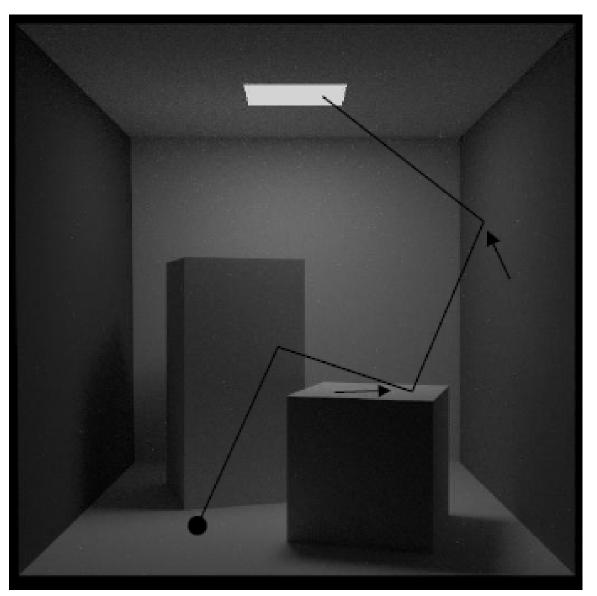


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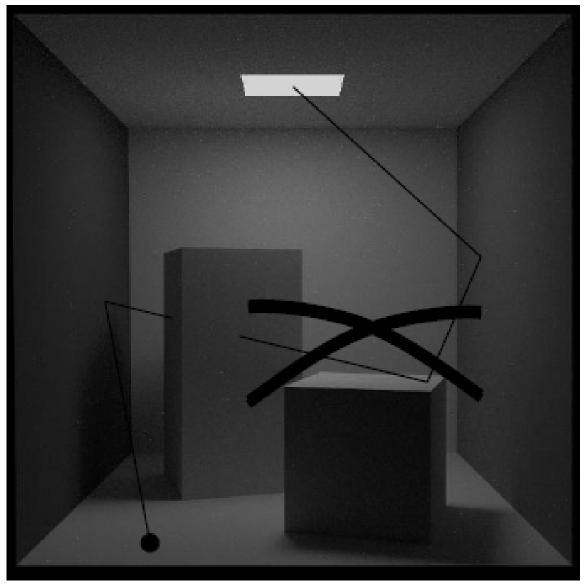
valid path

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small perturbations

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Accept mutations based on energy transport

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Unbiased vs. Consistent

Unbiased

- No systematic error
- $E[I_{estimator}] = I$
- Better results with larger N

Consistent

- Converges to correct results with more samples
- $E[I_{estimator}] = I + \varepsilon$, where $\lim_{n\to\infty} \varepsilon = 0$



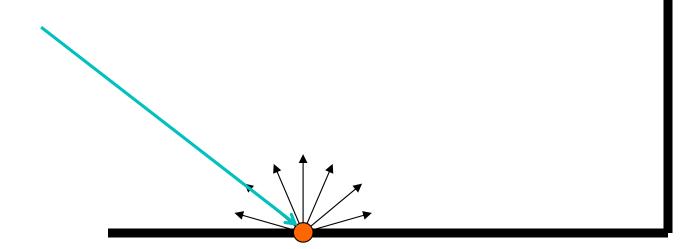
Biased Methods

- MC methods
 - Too noisy and slow
 - Nose is objectionable
- Biased methods: store information (caching)
 - Irradiance caching
 - Photon mapping



Biased Methods: Irradiance Caching

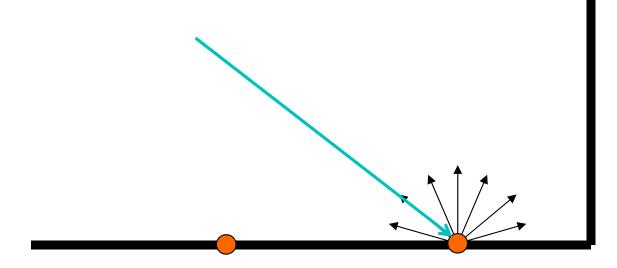
- Indirect changes smoothly.
- Cache irradiance.





Irradiance Caching

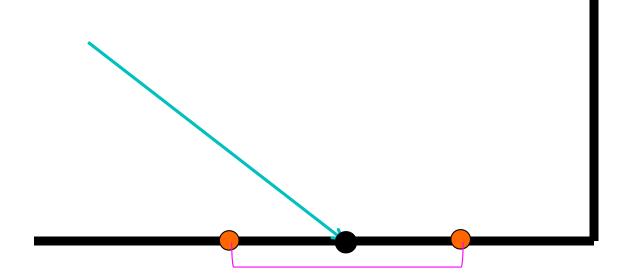
- Indirect changes smoothly.
- Cache irradiance.





Irradiance Caching

- Indirect changes smoothly.
- Cache irradiance.
- Interpolate them.





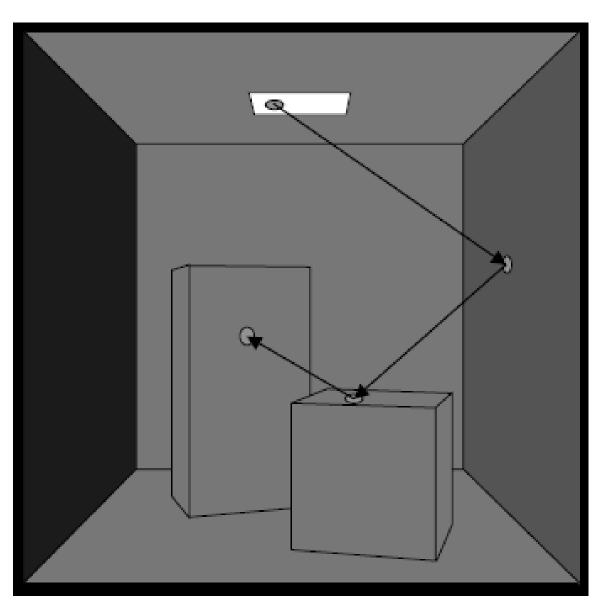
Biased Method: Photon Mapping

• 2 passes:

- Shoot "photons" (light-rays) and record any hit-points
- Shoot viewing rays and collect information from stored photons



Pass 1: shoot photons



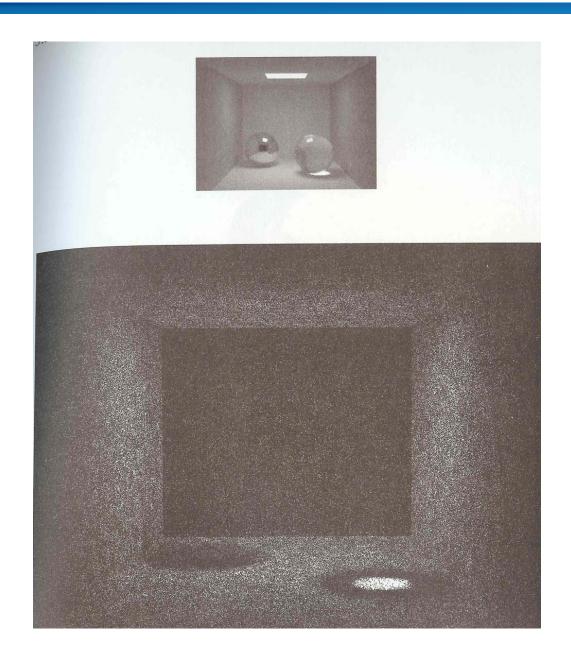
 Light path generated using MC techniques and Russian Roulette

Store:

- position
- incoming direction
- color
- ...

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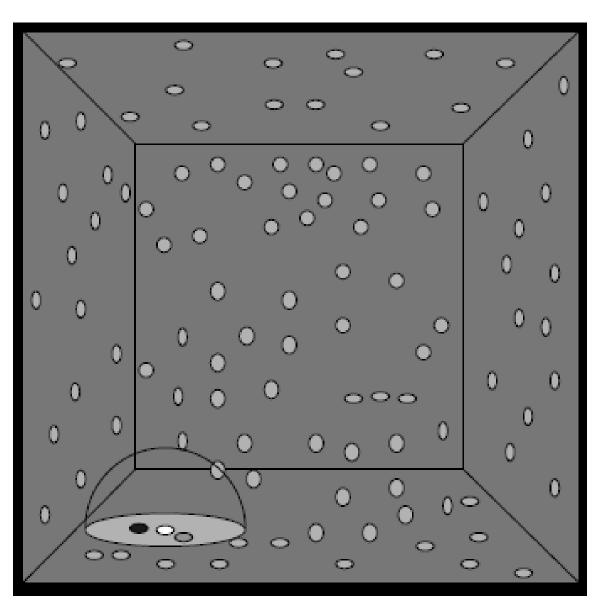
Stored Photons



Generate a few hundreds of thousands of photons



Pass 2: viewing ray

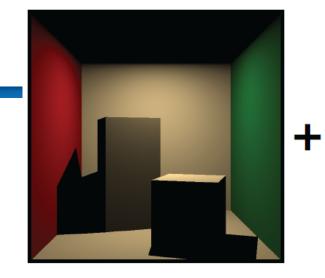


- Search for N
 closest photons
 (+check normal)
- Assume these photons hit the point we're interested in

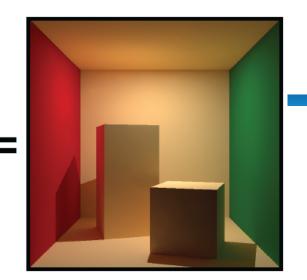
 Compute average radiance

Direct

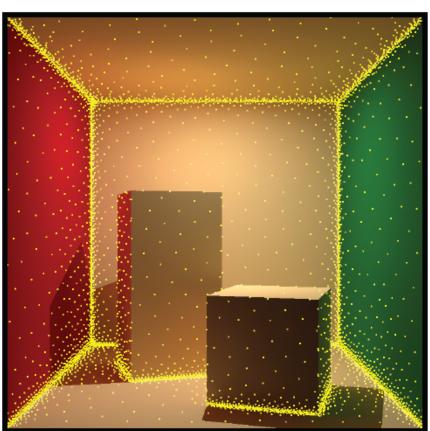
Indirect













Result



350K photons for the caustic map



Result



350K photons for the caustic map



Class Objectives were:

- Understand a basic structure of Monte Carlo ray tracing
 - Russian roulette for its termination
 - Path tracing

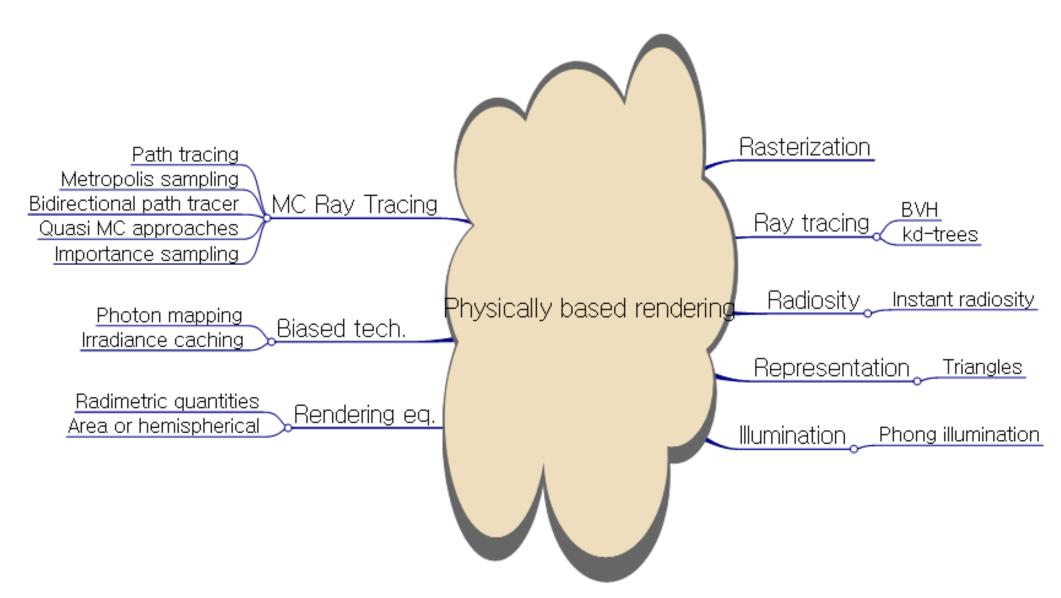


Summary

- Two basic building blocks
- Radiometry
- Rendering equation
- MC integration
- MC ray tracing
 - Unbiased methods
 - Biased methods



Summary



Next Time...

Instant radiosity



Homework

- Go over the next lecture slides before the class
- Watch 2 SIG/CVPR/ISMAR videos and submit your summaries every Tue. class
 - Just one paragraph for each summary
 - Any top-tier conf (e.g., ICRA) is okay

Example:

Title: XXX XXXX XXXX

Abstract: this video is about accelerating the performance of ray tracing. To achieve its goal, they design a new technique for reordering rays, since by doing so, they can improve the ray coherence and thus improve the overall performance.

Any Questions?

- Submit three times before the mid-term exam
- Come up with one question on what we have discussed in the class and submit:
 - 1 for typical or already answered questions
 - 2 for questions that have some thoughts or surprise me

