

Extending microfacet-based normal mapping

Team 4

20186413 Gaspard Murat

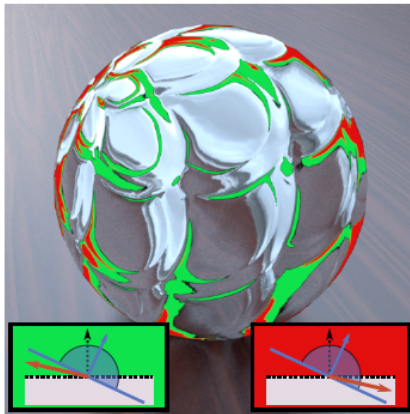
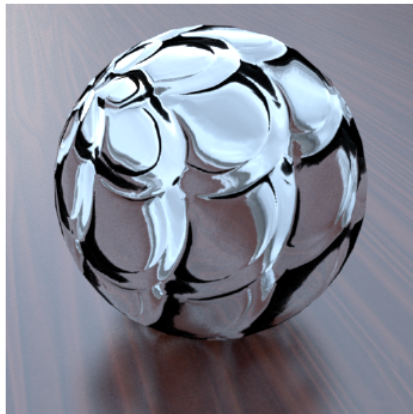
20193001 Dahyun Kang

20193164 Hakyong Kim



- Introduction
- Problem Statement
- Goal
- Experiment & Result
- Summary

Classic Normal Mapping
24 seconds



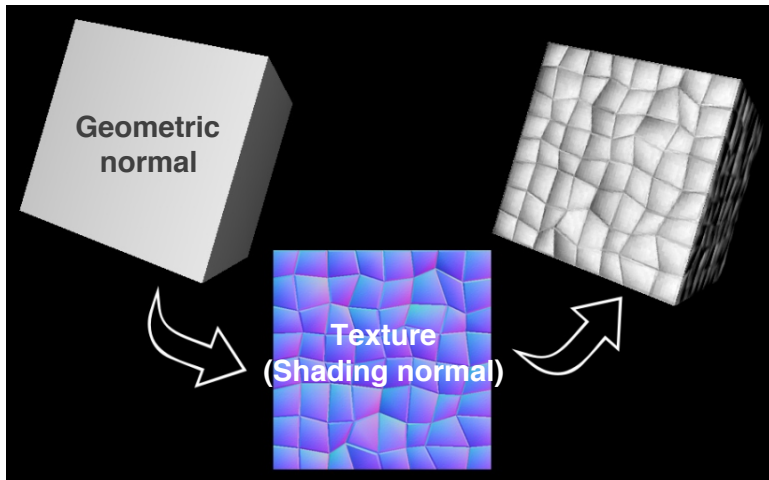
Microfacet-Based Normal Mapping (ours)
27 seconds



Microfacet-based Normal Mapping for Robust Monte Carlo Path Tracing

VINCENT SCHÜSSLER, ERIC HEITZ, JOHANNES HANIKA, CARSTEN DACHSBACHER

I Normal map

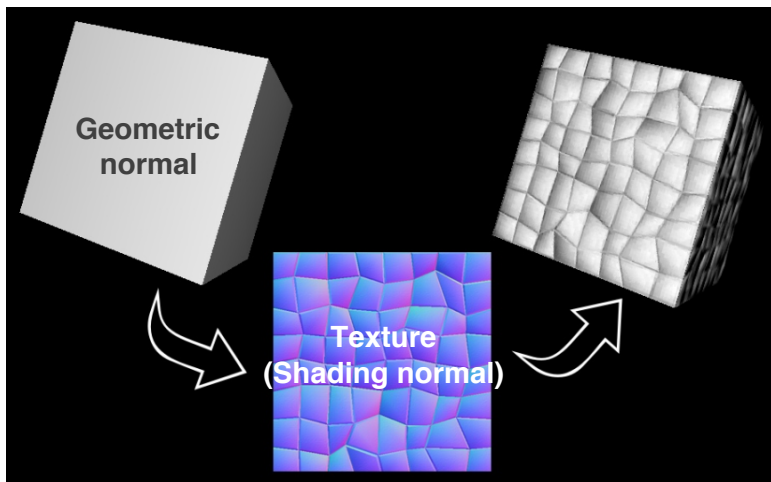


Problem:

Breaks the consistency of light transport

Cause flawed approach for PBRT(Monte Carlo Path Tracing)

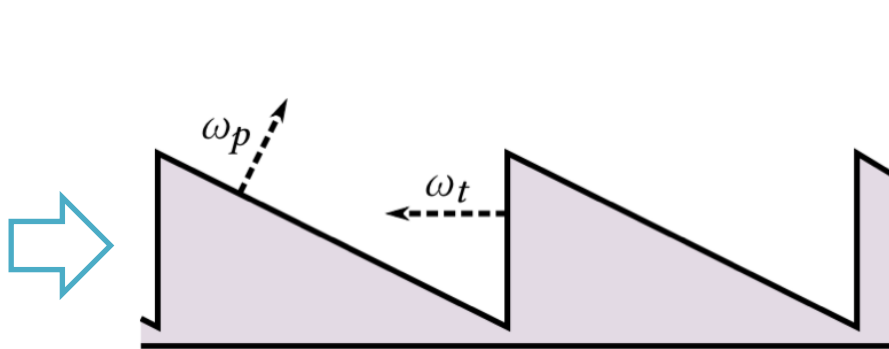
I Normal map



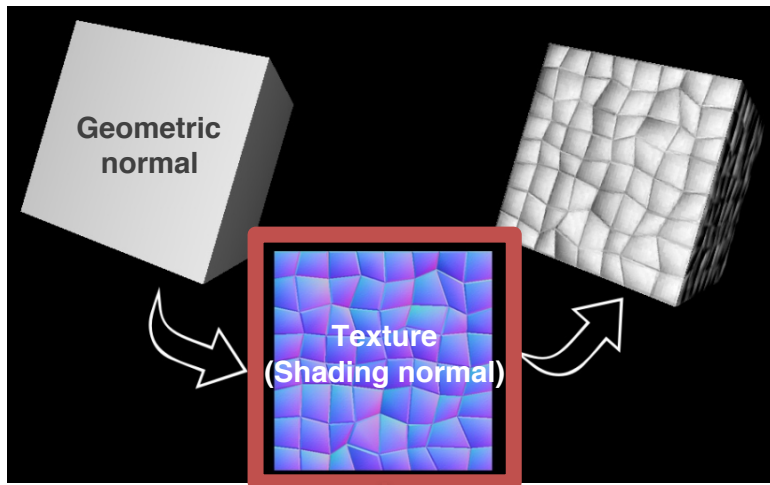
Problem:

Breaks the consistency of light transport
Cause flawed approach for PBRT

I Microfacet-based Normal mapping

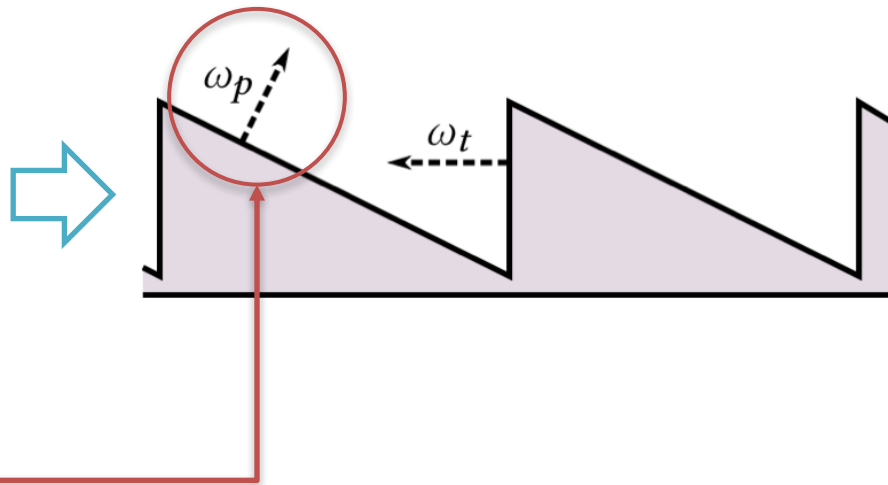


I Normal map

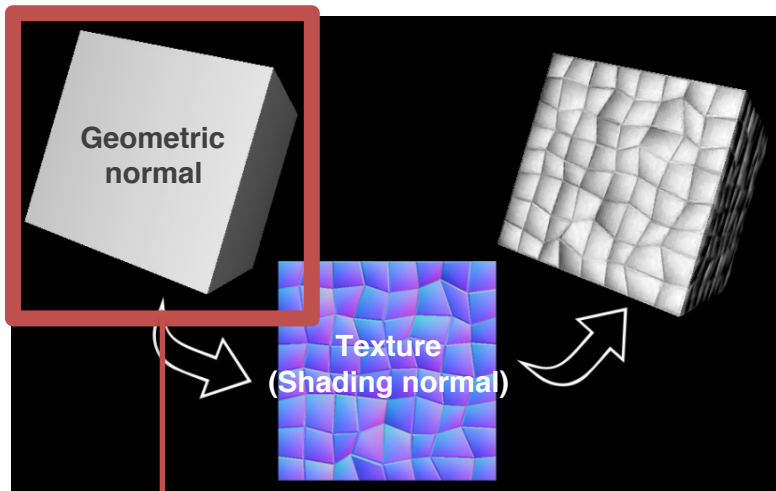


I Microfacet-based Normal mapping

Perturbed normal



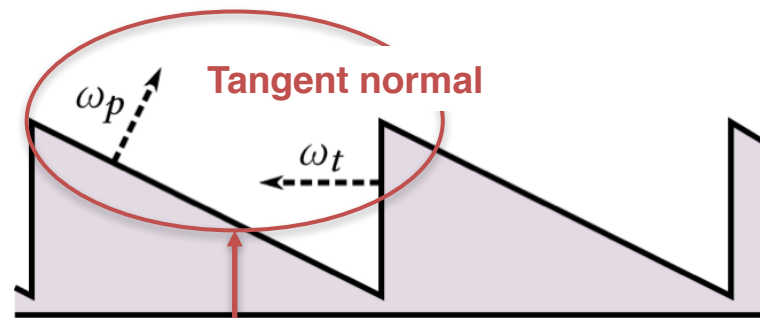
I Normal map



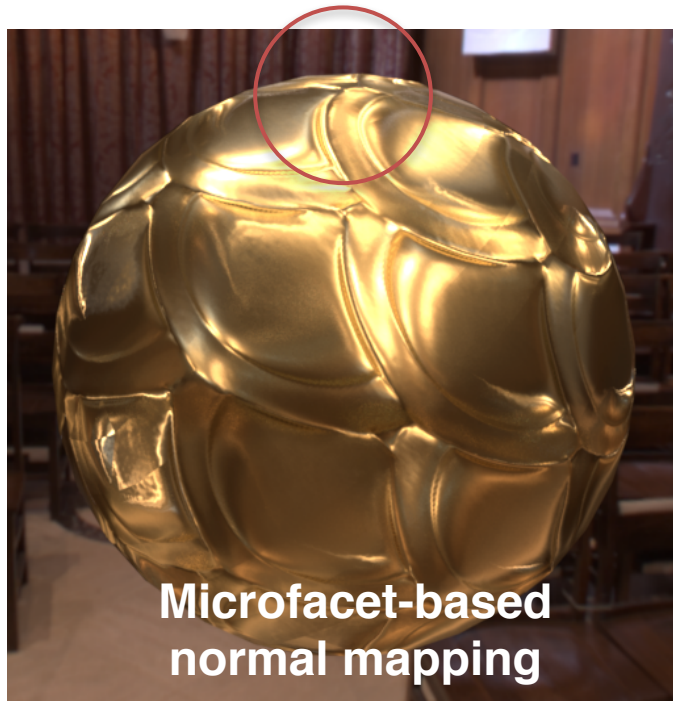
Average normal of microsurface
remains geometric normal

I Microfacet-based Normal mapping

Perturbed normal



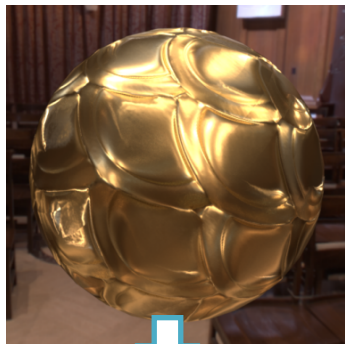
I Paper Result



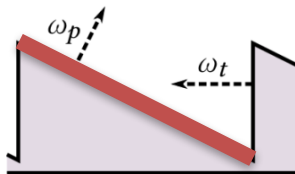
Problem statement

Addressed problem.

1. Limited support of different material types



Micro-BRDF of perturbed face



= Rough **conductor**



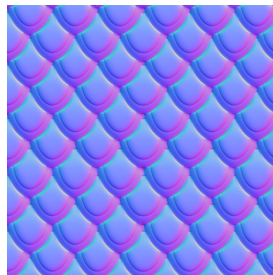
Microfacet-based normal mapping fails

= Rough **dielectric**

Wanted image



Dielectric material w/o normal mapping

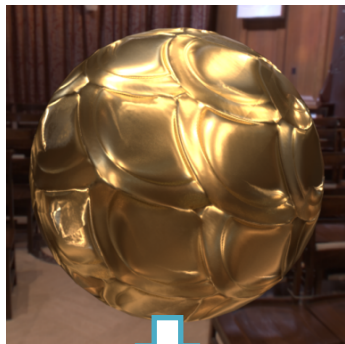


Microfacet model that support shading normal mapping

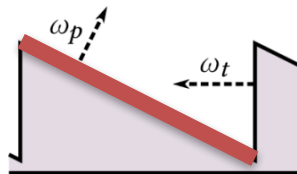
Problem statement

Addressed problem.

1. Limited support of different material types



Micro-BRDF of perturbed face



= Rough **conductor**

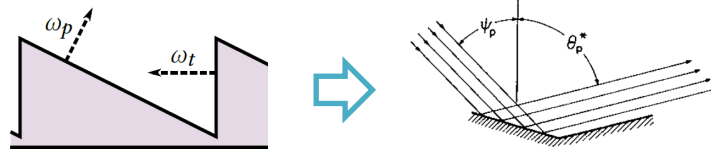


Microfacet-based normal mapping fails

= Rough **dielectric**

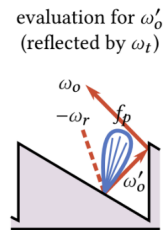
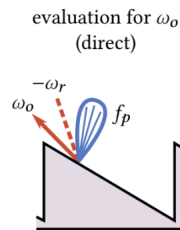
Further extent of implementation

2. Variation of microgeometry



3. Analytic solution of multiple scattering

- Speed enhancement



Limited support of different material types

1. Support transmittance term in microfacet-based normal mapping

Variation of microgeometry

2. Experiment microgeometry with non-tangent microfacet

Analytic solution for multiple scattering

3. Analyze assumptions of the problem and explore for the solution

Study 1. Support Transmittance

Author's implementation of microfacet-based normal mapping

Mitsuba-plugin : inherit BSDF class

```
43 class NormalMapMicrofacet : public BSDF {
44 public:
45     NormalMapMicrofacet(const Properties &props) : BSDF(props), rng(new Random) {
```

3 main function that implements the algorithm

```
119     Spectrum eval(const BSDFSamplingRecord &bRec_, EMeasure measure) const {
```

- Evaluate the **BSDF** $f(\mathbf{w}_i, \mathbf{w}_o)$

```
133     Float pdf(const BSDFSamplingRecord &bRec, EMeasure measure) const {
```

- Compute the probability of sampling ***bRec.wo*** (given ***bRec.wi***).

```
138     Spectrum sample(BSDFSamplingRecord &bRec, const Point2 &sample) const {
```

- Sample the BSDF and return the importance weight
- (i.e. the value of the BSDF divided by the probability density of the sample).

Study 1. Support Transmittance

1) Modify function `eval`

```
119 Spectrum eval(const BSDFSamplingRecord &bRec_, EMeasure measure) const {
```

Calls `evalMirror` according to paper's algorithm implementation

```
Spectrum evalMirror(const BSDFSamplingRecord &bRec, EMeasure measure) const {
```

```
    if (measure != ESolidAngle
```

```
        || Frame::cosTheta(bRec.wi) <= 0
```

```
        || Frame::cosTheta(bRec.wo) <= 0)
```

```
        //|| Frame::cosTheta(bRec.wi) <= 0
```

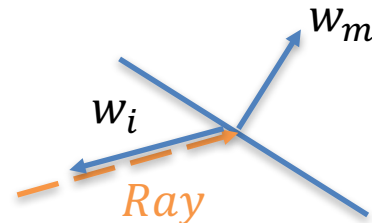
```
        //|| Frame::cosTheta(bRec.wo) <= 0
```

```
    )
```

```
    return Spectrum(0.0f);
```

When ray hits
the back-face of microfacet

Author's code stops evaluation
→ Delete to support transparency



Study 1. Support Transmittance

1) Modify function `eval`

```
119 Spectrum eval(const BSDFSamplingRecord &bRec_, EMeasure measure) const {
```

Calls `evalMirror` according to paper's algorithm implementation

```
Spectrum evalMirror(const BSDFSamplingRecord &bRec, EMeasure measure) const {
```

```
    if (measure != ESolidAngle
```

```
        || Frame::cosTheta(bRec.wl) <= 0
```

```
        || Frame::cosTheta(bRec.wo) <= 0)
```

```
        //|| Frame::cosTheta(bRec.wl) <= 0
```

```
        if (!singleScattering) {
```

```
            float pdfWo = m_nested->pdf(queryEvalReflection, measure);
```

```
            pdfWo /= Frame::cosTheta(queryEvalReflection.wo);
```

```
            pdfWo /= abs(Frame::cosTheta(queryEvalReflection.wo));
```

After sampling of `wo`

Study 1. Support Transmittance

1) Modify function `eval`

```
119 Spectrum eval(const BSDFSamplingRecord &bRec_, EMeasure measure) const {
```

Calls `evalMirror` according to paper's algorithm implementation

```
Spectrum evalMirror(const BSDFSamplingRecord &bRec, EMeasure measure) const {
```

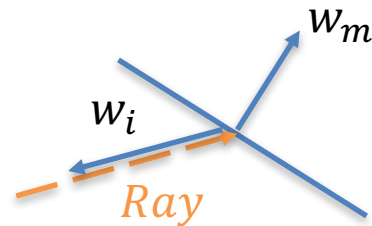
```
    if (i >= maxScatteringOrder || generateRandomNumber() < G1_) break;
```

```
    //if a ray goes down, stop traveling
```

```
    if ( Frame::cosTheta(query_wp.wo) < 0.f || i >= maxScatteringOrder || generateRandomNumber() < G1_) break;
```

In case of **transmission**

Stop randomwalk for multiple scattering and compute refracted ray

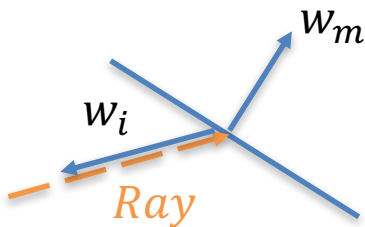


Study 1. Support Transmittance

2) Modify function pdf and sample

```
133   Float pdf(const BSDFSamplingRecord &bRec, EMeasure measure) const {
138   Spectrum sample(BSDFSamplingRecord &bRec, const Point2 &sample) const {
```

Consider back-facing facet



```
Float pdfMirror(const BSDFSamplingRecord &bRec, EMeasure measure) const {
    if (measure != ESolidAngle
        || Frame::cosTheta(bRec.wi) <= 0
        || Frame::cosTheta(bRec.wo) <= 0
        //|| Frame::cosTheta(bRec.wi) <= 0
        //|| Frame::cosTheta(bRec.wo) <= 0
    )
        return 0.0f;
Spectrum sampleMirror(BSDFSamplingRecord &bRec, const Point2 &sample) const {
    if (Frame::cosTheta(bRec.wi) <= 0)
        return Spectrum(0.0f);

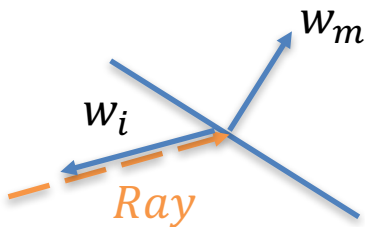
    //when a ray hit the backward surface, return 0
    //if (Frame::cosTheta(bRec.wi) <= 0)
    //    return Spectrum(0.0f);
```


Study 1. Support Transmittance

2) Modify function pdf and sample

```
133 Float pdf(const BSDFSamplingRecord &bRec, EMeasure measure) const {  
138 Spectrum sample(BSDFSamplingRecord &bRec, const Point2 &sample) const {
```

Consider back-facing facet



```
Float pdfMirror(const BSDFSamplingRecord &bRec, EMeasure measure) const {
```

```
    BSDFSamplingRecord samplingQuery(*currentIts, NULL);  
    BSDFSamplingRecord samplingQuery(*currentIts, sampler);
```

→ Set originally nullified sampler

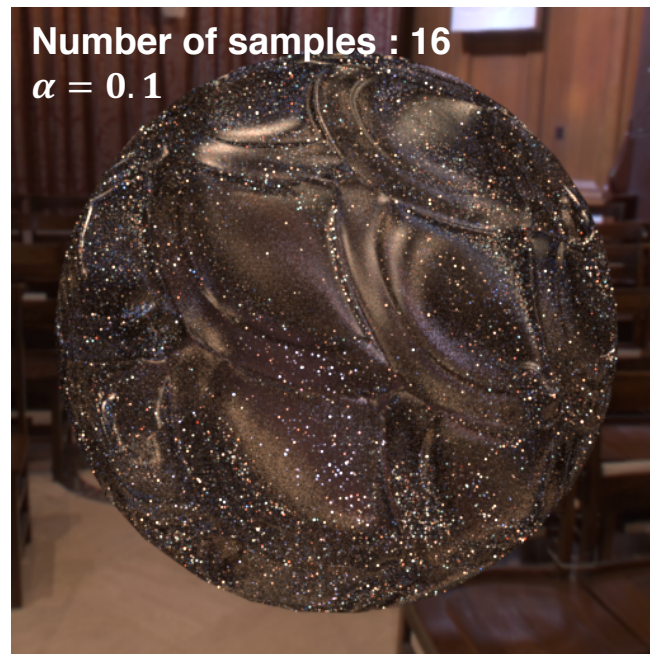
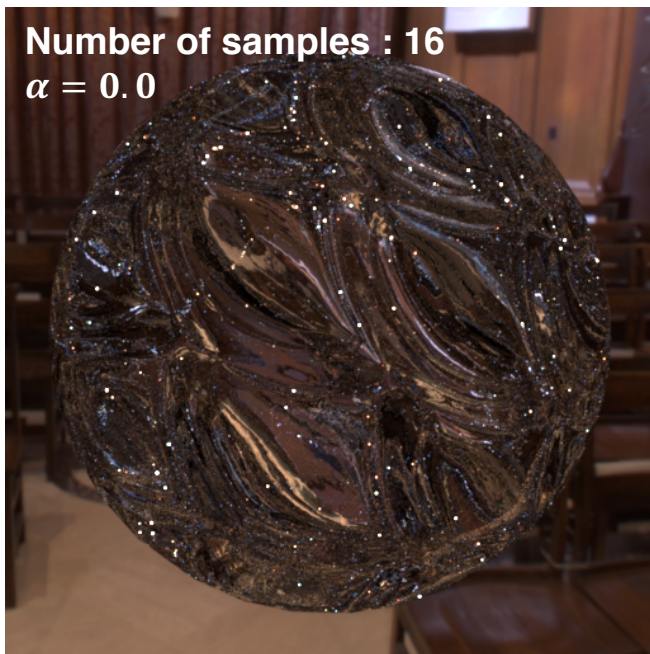
```
Spectrum sampleMirror(BSDFSamplingRecord &bRec, const Point2 &sample) const {
```

Sample for transmitting rays also

```
//when a ray go under ground, return 0  
//if (Frame::cosTheta(bRec.wo) <= 0.) {  
//    return Spectrum(0.f);  
//}  
return energy;
```

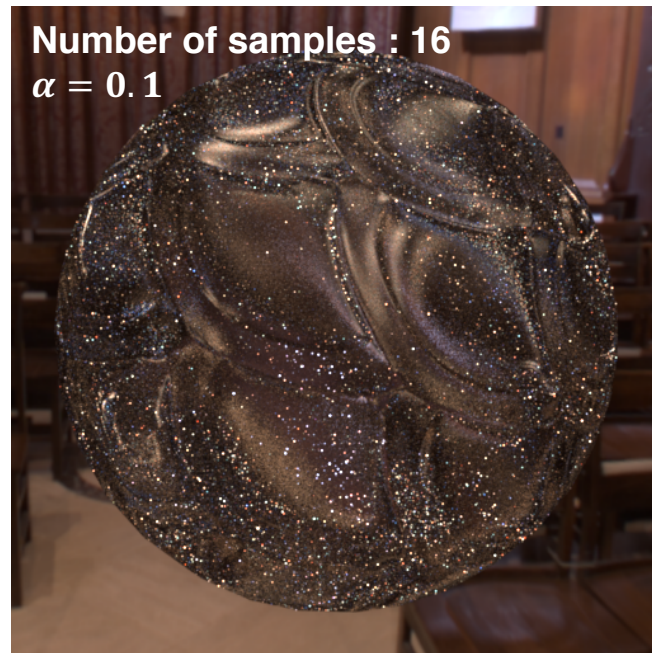
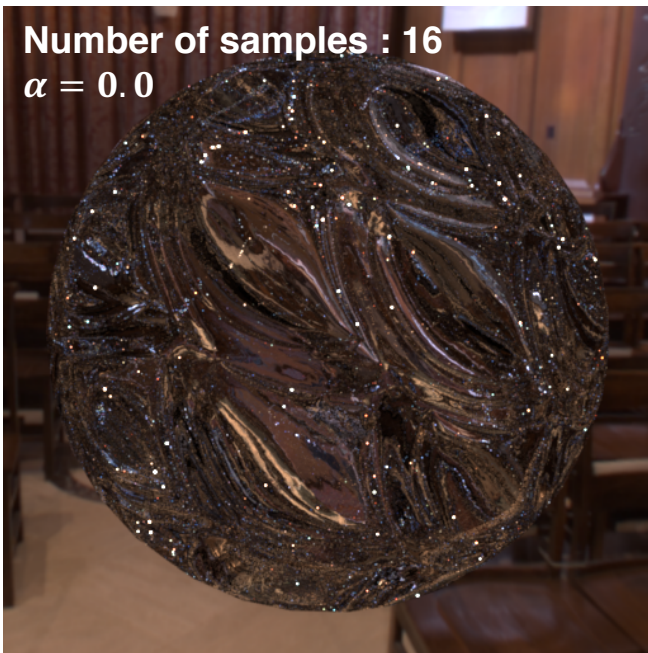
Result 1. Support Transmittance

Microfacet-based normal mapping of **rough dielectric material**



Result 1. Support Transmittance

Microfacet-based normal mapping of **rough dielectric material**



→ Supported transmittance term of micro-BSDF in microfacet-based normal mapping

Goal:

- improving speed in the random walk algorithm
- Reducing variance

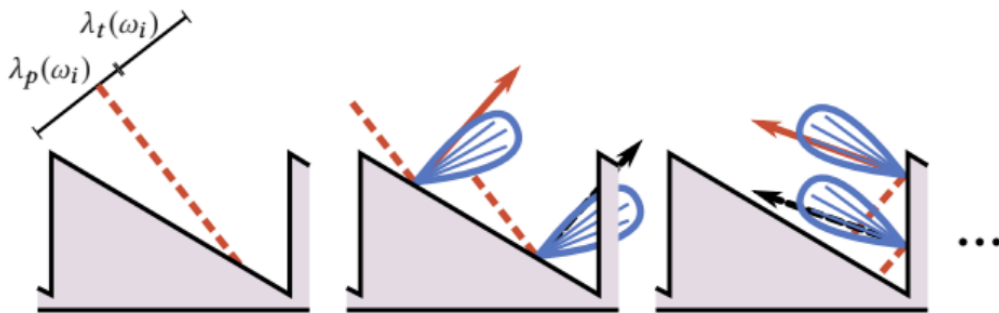


Figure x: Random walk on the microsurface

Default of the random walk algorithm:

- Rays bounce against the surface of the microsurface.
- The more bounces, the more **variance** is increased and the more **time consuming** the algorithm is !

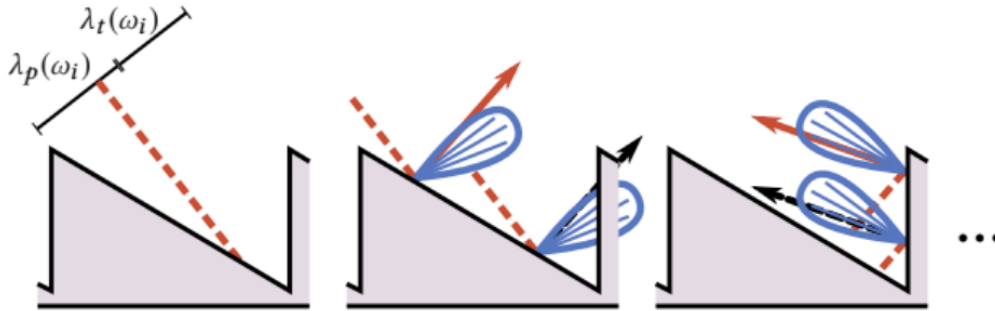
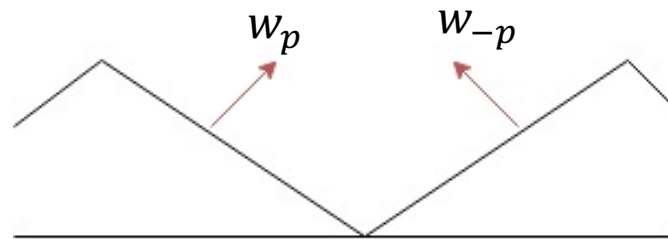
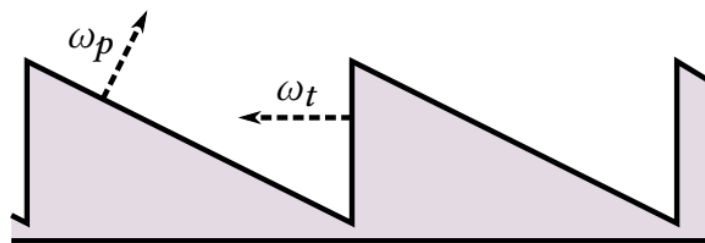


Figure x: Random walk on the microsurface

First modification: classic v-groove



$$G1(\omega_i, \omega_m) = H(\langle \omega_i, \omega_m \rangle) \min\left[1, \frac{\langle \omega_i, \omega_g \rangle}{a_p(\omega_i) + a_t(\omega_i)}\right]$$

$$G1(\omega_i, \omega_m) = \min\left[1, \frac{\langle \omega_i, \omega_p \rangle \langle \omega_p, \omega_g \rangle}{\langle \omega_i, \omega_g \rangle}\right]$$

Result 2. Microgeometry

First modification: classic v-groove

As expected, very bad result:

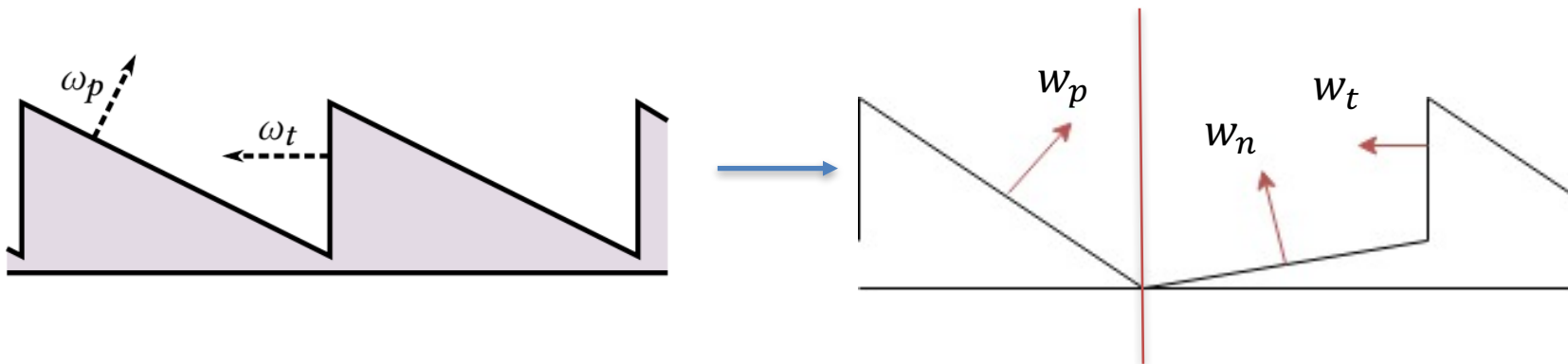
- not symmetric
- not energy conservative



Figure x: Golden sphere rendered using classic V-groove and random walk

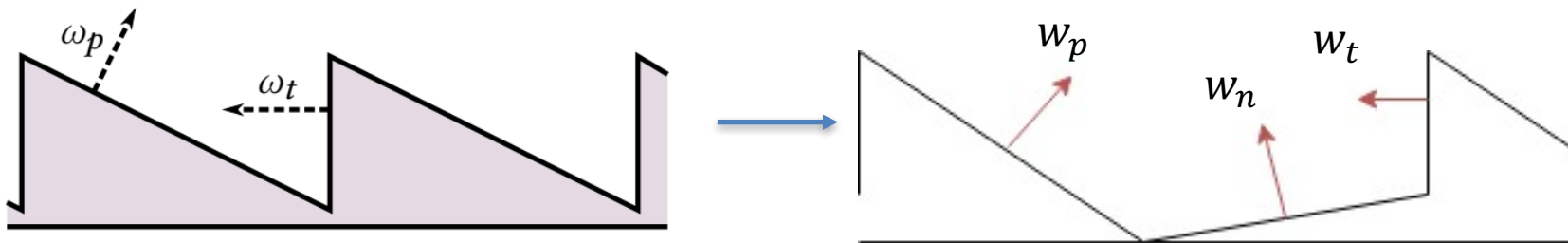
Study 2. Microgeometry

second modification: u-groove



Mix of the classic V-groove model
and the V-groove model introduced by the author

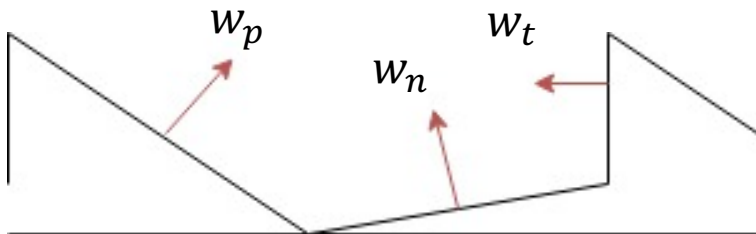
second modification: u-groove



$$G1(\omega_i, \omega_m) = H(\langle \omega_i, \omega_m \rangle) \min \left[1, \frac{\langle \omega_i, \omega_g \rangle}{a_p(\omega_i) + a_t(\omega_i)} \right]$$

$$G1(\omega_i, \omega_m) = H(\langle \omega_i, \omega_m \rangle) \min \left[1, 2 \frac{\langle \omega_i, \omega_g \rangle}{\frac{\langle \omega_i, \omega_p \rangle}{\langle \omega_p, \omega_g \rangle} + \frac{\langle \omega_i, \omega_n \rangle}{\langle \omega_n, \omega_g \rangle} + \frac{\langle \omega_i, \omega_t \rangle \sqrt{1 - \langle \omega_n, \omega_g \rangle^2}}{\langle \omega_n, \omega_g \rangle}} \right]$$

second modification: u-groove



Design a **Normal Distribution Function** by mixing the NDF from classic V-groove and the NDF from the modified V-groove

$$D(w_m) = \frac{1}{2} \frac{\delta_p(\omega_m)}{\langle \omega_p, \omega_g \rangle} + \frac{1}{2} \left(\frac{\delta_n(\omega_m)}{\langle \omega_n, \omega_g \rangle} + \frac{\delta_t(\omega_m) \sqrt{1 - \langle \omega_n, \omega_g \rangle^2}}{\langle \omega_n, \omega_g \rangle} \right)$$

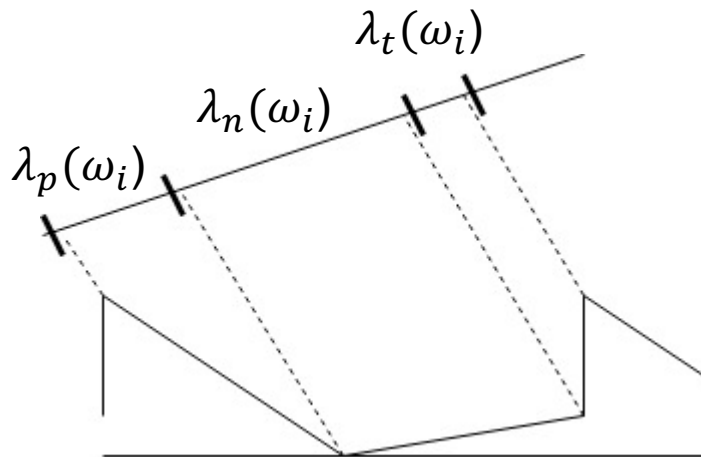
second modification: u-groove

Projected Areas and Intersection Probabilities

$$a_p(\omega_i) = \frac{1}{2} \frac{\langle \omega_i, \omega_p \rangle}{\langle \omega_p, \omega_g \rangle}$$

$$a_n(\omega_i) = \frac{1}{2} \frac{\langle \omega_i, \omega_n \rangle}{\langle \omega_n, \omega_g \rangle}$$

$$a_t(\omega_i) = \frac{1}{2} \frac{\langle \omega_i, \omega_p \rangle}{\langle \omega_p, \omega_g \rangle} \frac{\langle \omega_i, \omega_p \rangle \sqrt{1 - \langle \omega_n, \omega_g \rangle^2}}{\langle \omega_n, \omega_g \rangle}$$



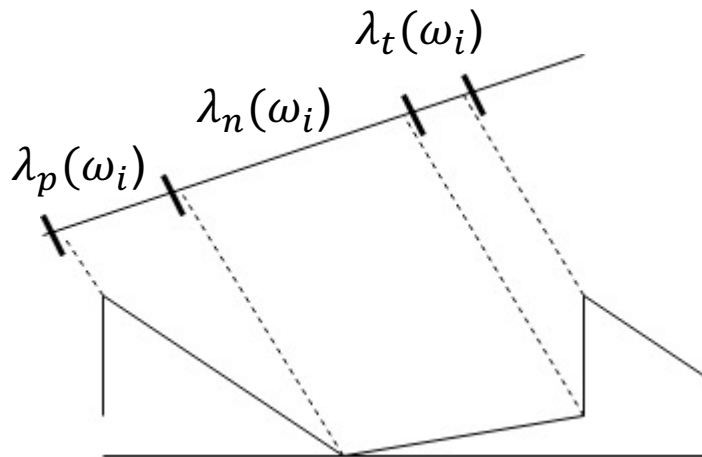
second modification: u-groove

Projected areas and Intersection Probabilities

$$\lambda_p(\omega_i) = \frac{a_p(\omega_i)}{a_p(\omega_i) + a_n(\omega_i) + a_t(\omega_i)}$$

$$\lambda_n(\omega_i) = \frac{a_n(\omega_i)}{a_p(\omega_i) + a_n(\omega_i) + a_t(\omega_i)}$$

$$\lambda_t(\omega_i) = \frac{a_t(\omega_i)}{a_p(\omega_i) + a_n(\omega_i) + a_t(\omega_i)}$$



second modification: u-groove

- With changing the microfacet model, the random walk algorithm has also to be modified.

Assuming the ray is still in the microfacet, we need to **determine which micronormal** it will hit

```
213     if (generateRandomNumber() > lambda_p(wp, bRec.wi)) {
214         std::swap(currentIts, nextIts);
215         std::swap(currentWo, nextWo);
216     }
```

Generate a random number g

If ($g > \lambda_p(\omega_i)$)

Then ω_t is hit

Else

ω_p is hit

Just have to swap from one face to another

Study 2. Microgeometry

second modification: u-groove

- With changing the microfacet model, the random walk algorithm has also to be modified.

```
243     int facet = 1; //w_p is chosen
244     if (generateRandomNumber() > lambda_p(wp, bRec.wi)) {
245         facet = 2; //w_n is chosen
246         currentIts = nextIts_n;
247         currentWo = nextWo_n;
248         if (generateRandomNumber() > lambda_n(wp, bRec.wi)) {
249             facet = 3; //w_t is chosen
250             currentIts = nextIts_t;
251             currentWo = nextWo_t;
252         }
253     }
```

We need to keep track of the current facet, and we have to compute the next to be hit among the two other.

second modification: u-groove

But the result were not good enough, and we lack time to estimate the improvement in speed or variance...



Our model

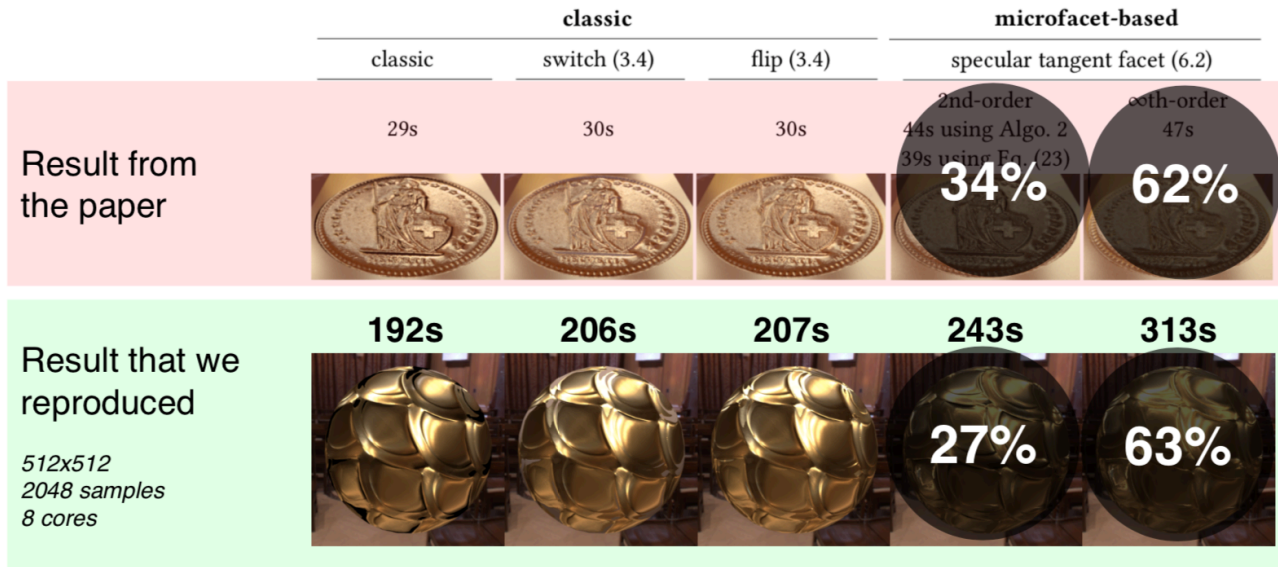


Model of Heitz et Al

Study 3. Multiple Scattering

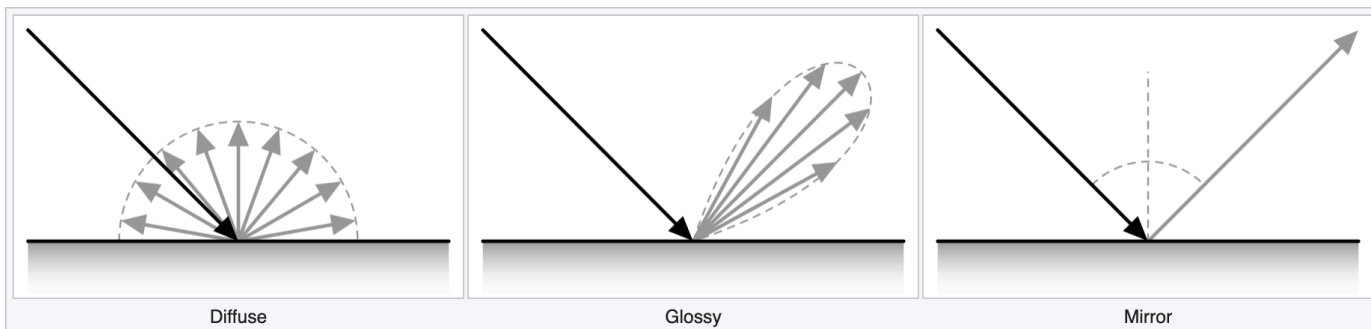
Motivation:

The slowdown is mainly because of random walk process.
(used to evaluate BRDF value)



Motivation:

How do we get the BRDF value at a fixed angles,
i.e. how do we evaluate the value of $f(\omega_i=\text{fixed}, \omega_o=\text{fixed})$?



Simple examples of BRDF

Study 3. Multiple Scattering

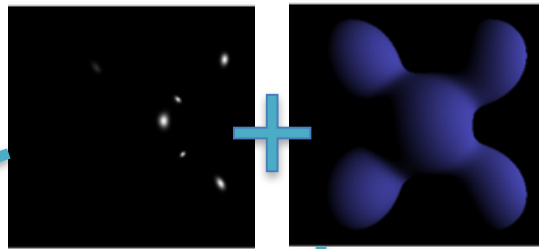
Motivation:

How do we get the BRDF value at a fixed angles,
i.e. how do we evaluate the value of $f(\omega_i = \text{fixed}, \omega_o = \text{fixed})$?

```
Spectrum result(0.0f);  
if (hasSpecular) {  
    Float alpha    = dot(bRec.wo, reflect(bRec.wi)),  
        exponent = m_exponent->eval(bRec.its).average();  
  
    if (alpha > 0.0f) {  
        result += m_specularReflectance->eval(bRec.its) *  
            ((exponent + 2) * INV_TWOPHI * std::pow(alpha, exponent));  
    }  
}  
  
if (hasDiffuse) {  
    result += m_diffuseReflectance->eval(bRec.its) * INV_PI;  
}  
  
return result * Frame::cosTheta(bRec.wo);
```

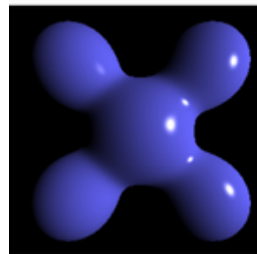
$O(1)$

$O(1)$



Specular

Diffuse

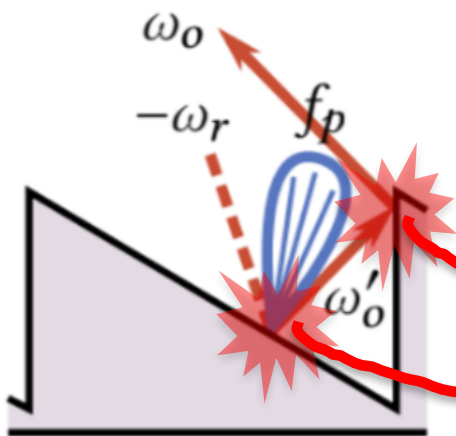


Phong Reflection

(quick)

Motivation:

How do we get the BRDF value at a fixed angles,
i.e. how do we evaluate the value of $f(\omega_i=\text{fixed}, \omega_o=\text{fixed})$?

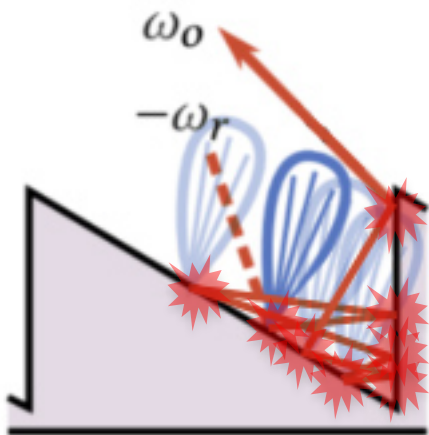


In microfacet-based normal map,
it is NOT evaluated by a single formula just as Phong.

It is evaluated considering **multiple bouncing**.

Motivation:

How do we get the BRDF value at a fixed angles,
i.e. how do we evaluate the value of $f(\omega_i=\text{fixed}, \omega_o=\text{fixed})$?

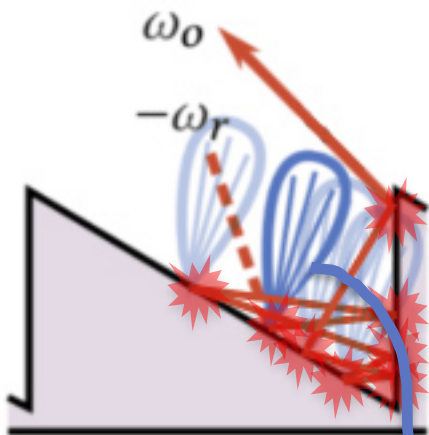


In microfacet-based normal map,
it is NOT evaluated by a single formula just as Phong.

It is evaluated considering **multiple bouncing**.
... and even more bounces.

Motivation:

How do we get the BRDF value at a fixed angles,
i.e. how do we evaluate the value of $f(\omega_i=\text{fixed}, \omega_o=\text{fixed})$?



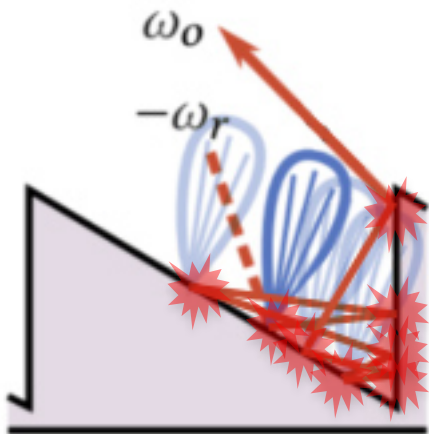
In microfacet-based normal map,
it is NOT evaluated by a single formula just as Phong.

It is evaluated considering **multiple bouncing**.

In code, it loops through `do-while`,
and that loop includes micro-brdf sampling. (**expensive**)
Of course, this should be evaluated stochastically.

Motivation:

How do we get the BRDF value at a fixed angles,
i.e. how do we evaluate the value of $f(\omega_i=\text{fixed}, \omega_o=\text{fixed})$?



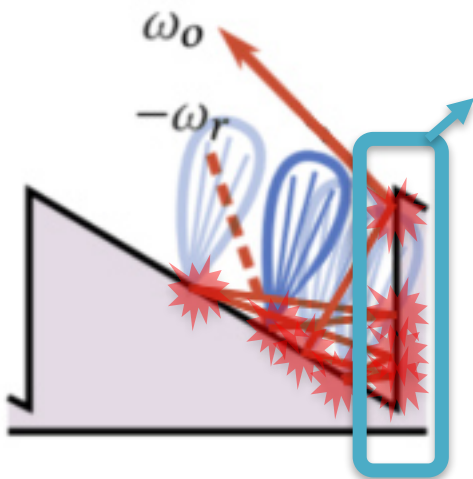
But our model has strong assumptions:

1. Microgeometry is super simple.

→ Only two kinds of facets.(V-Groove)

Motivation:

How do we get the BRDF value at a fixed angles,
i.e. how do we evaluate the value of $f(\omega_i=\text{fixed}, \omega_o=\text{fixed})$?

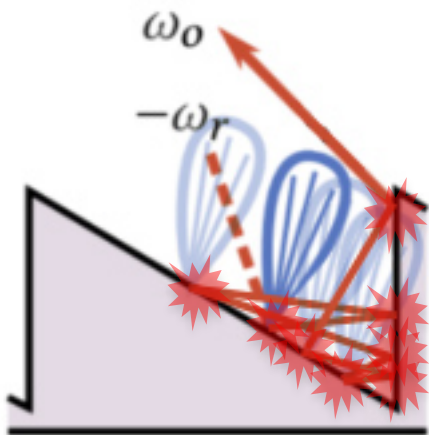


But our model has strong assumptions:

1. **Microgeometry is super simple.**
2. **Tangent facets always do perfect mirror reflection.**
 - Reflection on tangent facets is deterministic.
 - Thus the `do-while` loop is just consecutive sampling of the same micro-BRDF.

Motivation:

How do we get the BRDF value at a fixed angles,
i.e. how do we evaluate the value of $f(\omega_i=\text{fixed}, \omega_o=\text{fixed})$?



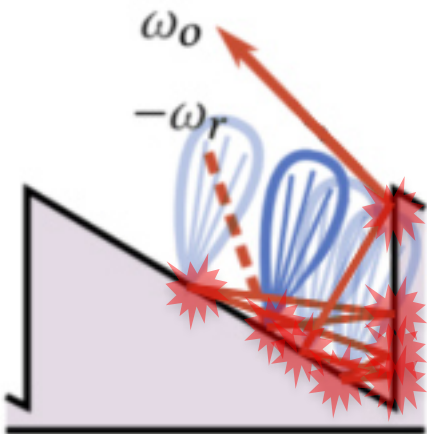
But our model has strong assumptions:

1. **Microgeometry is super simple.**
2. **Tangent facets always do perfect mirror reflection.**
3. **Masking-shadowing function is separable.**

- They do NOT compute “explicit ray-facet intersection”(e.g. depth) during random walk.
- Instead, they simply use the average intersection probability. Evidence of simplicity.

Motivation:

How do we get the BRDF value at a fixed angles,
i.e. how do we evaluate the value of $f(\omega_i=\textit{fixed}, \omega_o=\textit{fixed})$?



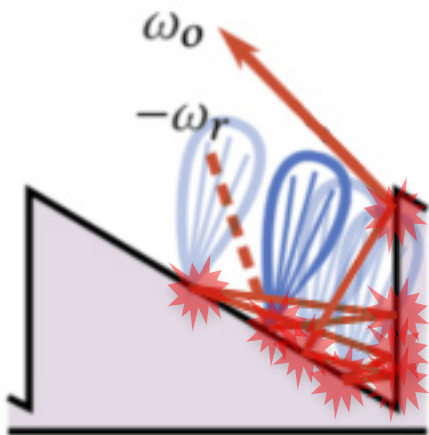
But our model has strong assumptions:

1. **Microgeometry is super simple.**
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3. **Masking-shadowing function is separable.**

MAYBE, those strong assumptions can give some kind of
*“**practical & (more optimistically,) analytic relationship** between microBRDF and random-walked macroBRDF”.*

Motivation:

How do we get the BRDF value at a fixed angles,
i.e. how do we evaluate the value of $f(\omega_i=\text{fixed}, \omega_o=\text{fixed})$?



“practical & (more optimistically,) analytic relationship between microBRDF and random-walked macroBRDF”.

Devil: “Hey dreamer, it's impossible, no doubts!”

Angel: “But the assumptions may make things easier!”

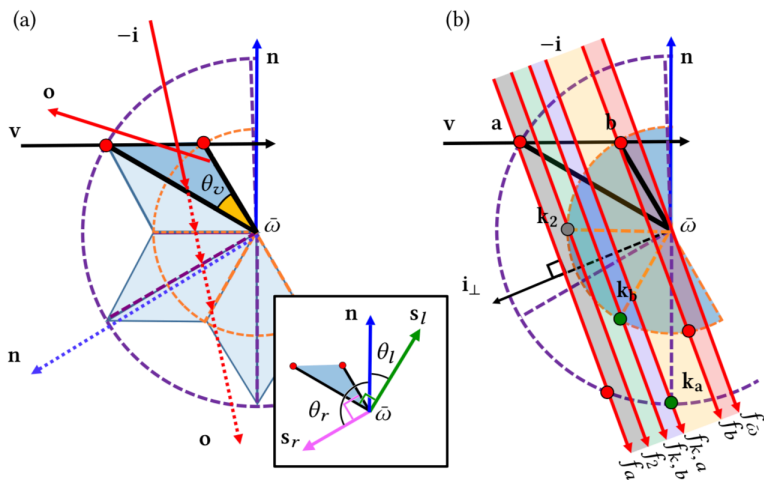
If it exist, and if we can derive it for this specific problem, we can reduce time for random walk and will be happy 😊

Survey:

There was recent SIGGRAPH paper in similar perspective:

<Practical Multiple Scattering for Rough Surfaces>

<Multiple Scattering from Distributions of Specular V-Grooves>



They derived analytic formula to calculate higher-order scattering in the V-groove microfacets.
(**with enormous maths**)

(What we exactly dreamed)

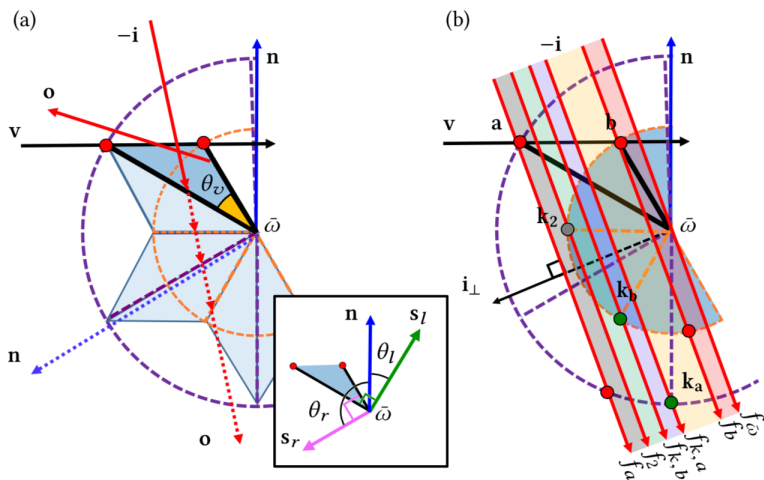
Study 3. Multiple Scattering

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*(**with enormous maths**)*

But with different assumptions, mainly that **all facets are mirror**.

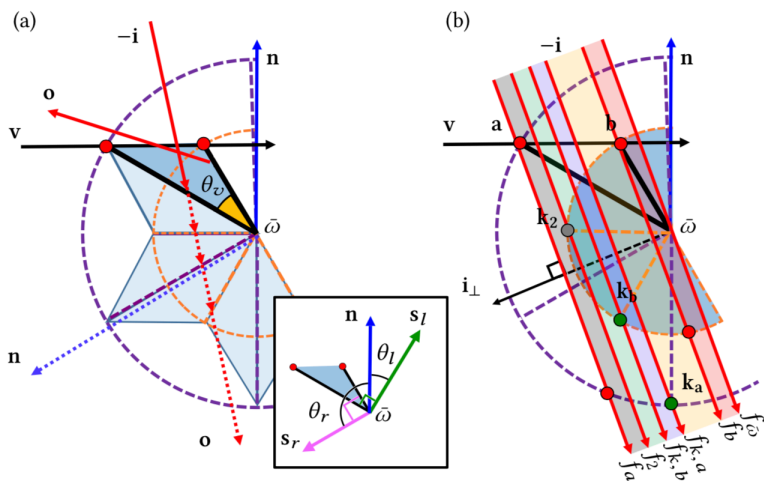
Study 3. Multiple Scattering

Survey:

There was recent SIGGRAPH paper in similar perspective:

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With even stronger assumption (**all facets are mirror**), their derivation is already full of math.

Sadly, we concluded that we are hopeless. However we feel this experience of hypothesizing was valuable to us.



1. Support transmittance term

- We succeeded to change implementation of the original paper .. with massive struggling against Mitsuba framework.

2. Change microgeometry

- There was a reason why the author decided to do so 😊
- Original microgeometry is the best.

3. Explore analytic solution for multiple scattering

- We dreamed but concluded that there is no hope.

Gaspard

- Huge contribution on exploring various theories & ideas
- Experiments on changing micro-geometry

Dahyun

- Manage environments for experiment & co-working
- Study on multiple scattering

Hakyeong

- Main implementation of transmission stuffs
- Support us with a firm theoretical foundation of micro-facets

Implementation is available at https://github.com/313usually/cs580_team4