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CS588: Image Search

# Scale Invariant Region Selection and SIFT

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Course URL:

<http://sgvr.kaist.ac.kr/~sungeui/IR>

**KAIST**



# Class Objectives (Ch. 2.2 and Ch. 2.3)

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- **Scale invariant region selection**
  - Automatic scale selection
  - Laplacian of Gradients (LoG)  $\approx$  Difference of Gradients (DoG)
  - SIFT as a local descriptor
  
- **At last time, we discussed:**
  - Different conferences
  - Image descriptors that are invariant to various changes
  - Harris corner detector

# From Points to Regions...

- The Harris and Hessian operators define interest points.
  - Precise localization
  - High repeatability

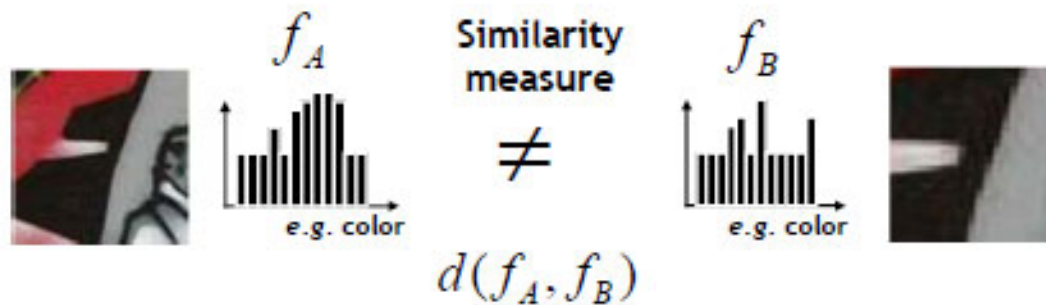


- In order to compare those points, we need to compute a descriptor over a region.
  - How can we define such a region in a scale invariant manner?
- *I.e. how can we detect scale invariant interest regions?*

Source: Bastian Leibe

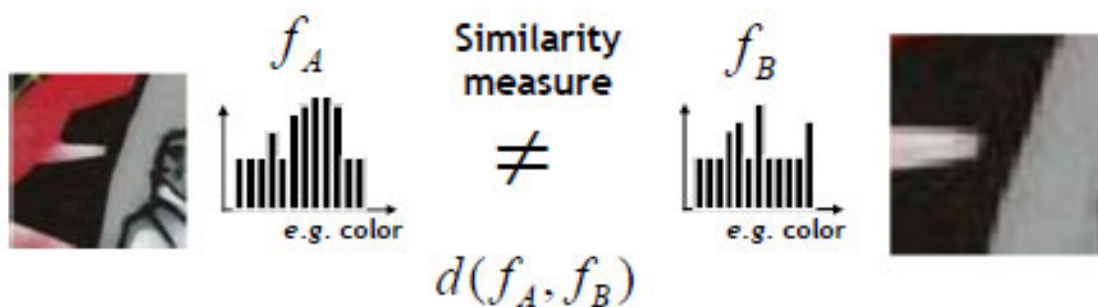
# Naïve Approach: Exhaustive Search

- Multi-scale procedure
  - Compare descriptors while varying the patch size



# Naïve Approach: Exhaustive Search

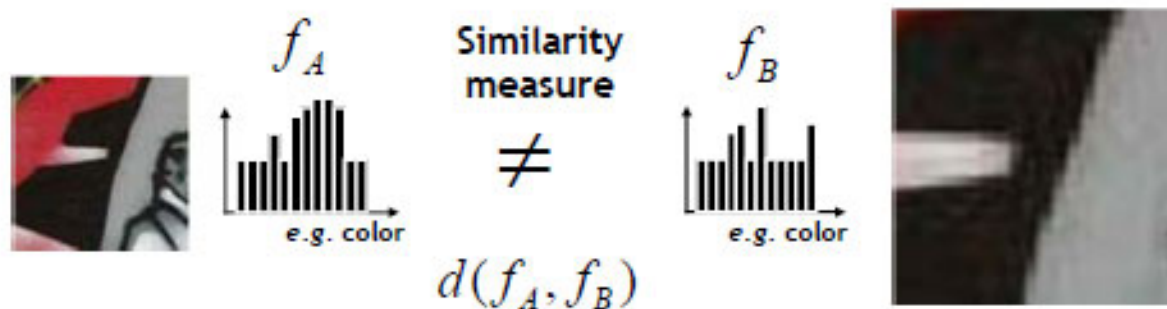
- Multi-scale procedure
  - Compare descriptors while varying the patch size



Slide credit: Krystian Mikolajczyk

# Naïve Approach: Exhaustive Search

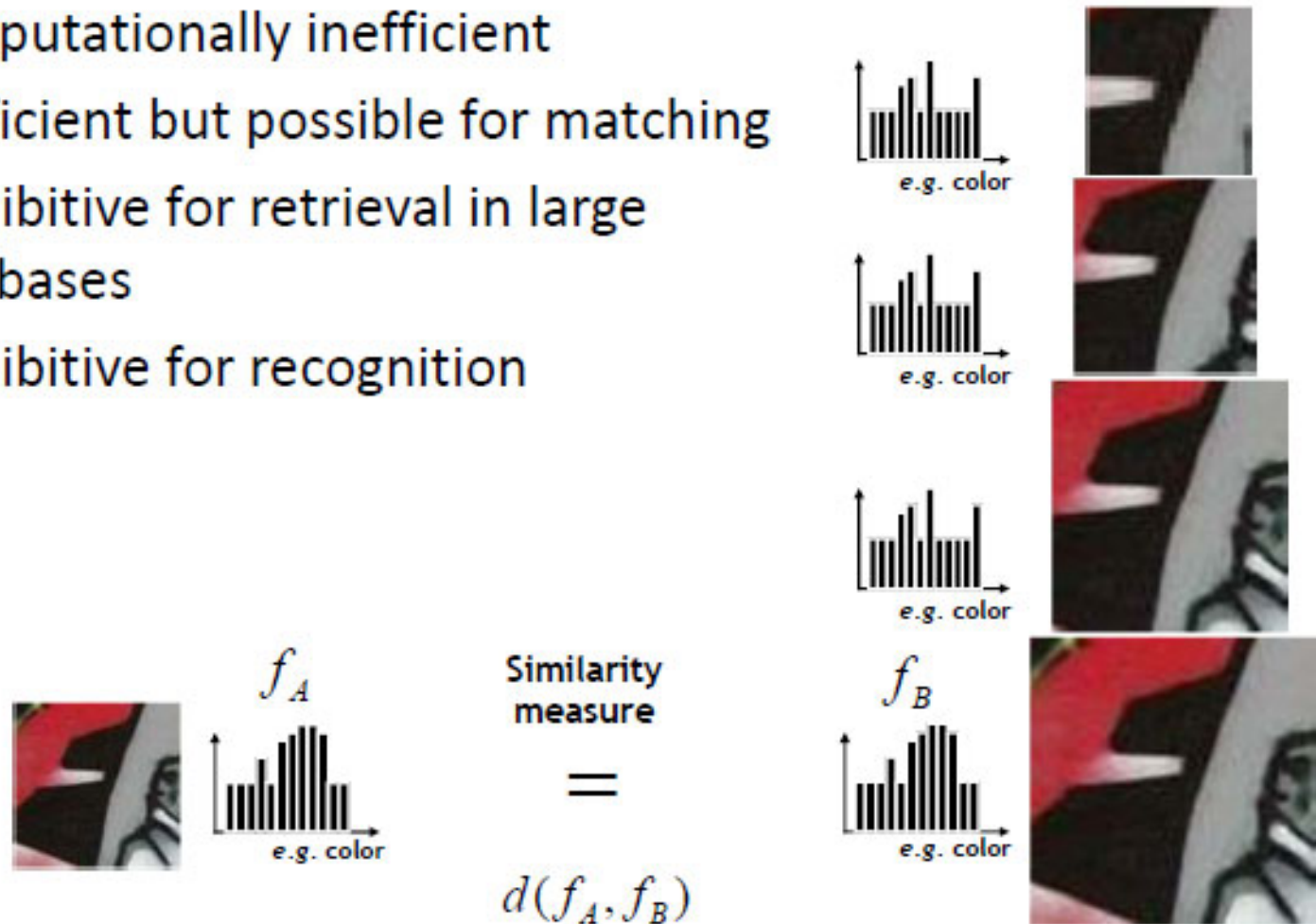
- Multi-scale procedure
  - Compare descriptors while varying the patch size



Slide credit: Krystian Mikolajczyk

# Naïve Approach: Exhaustive Search

- Comparing descriptors while varying the patch size
  - Computationally inefficient
  - Inefficient but possible for matching
  - Prohibitive for retrieval in large databases
  - Prohibitive for recognition



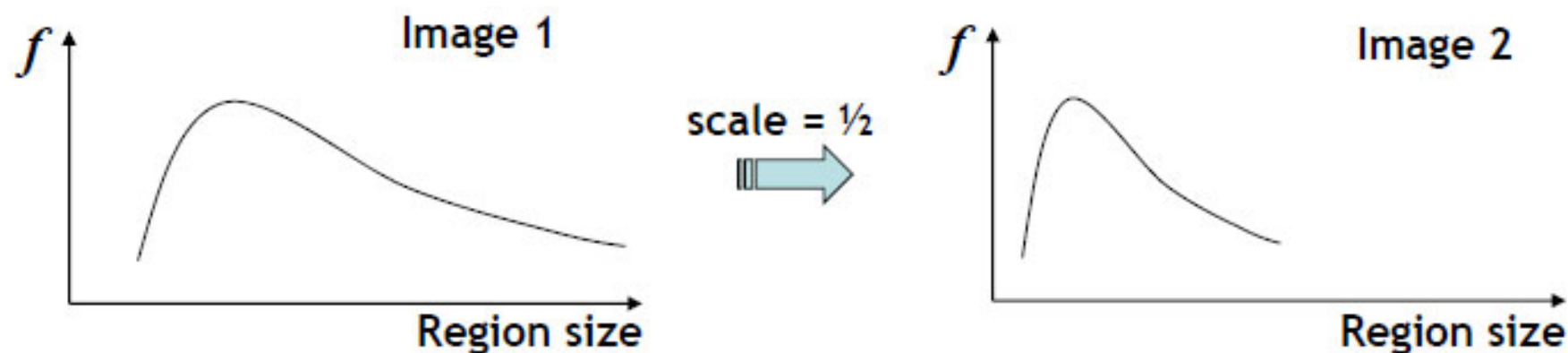
Slide credit: Krystian Mikolajczyk

# Automatic Scale Selection

- Solution:
  - Design a function on the region, which is “scale invariant”  
(*the same for corresponding regions, even if they are at different scales*)

Example: average intensity. For corresponding regions (even of different sizes) it will be the same.

- For a point in one image, we can consider it as a function of region size (patch width)

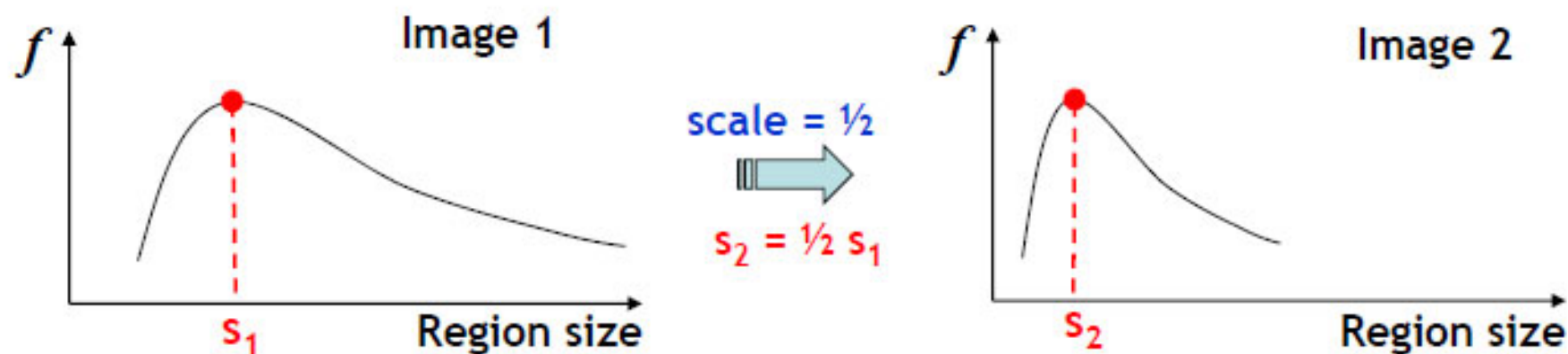


Slide credit: Kristen Grauman



# Automatic Scale Selection

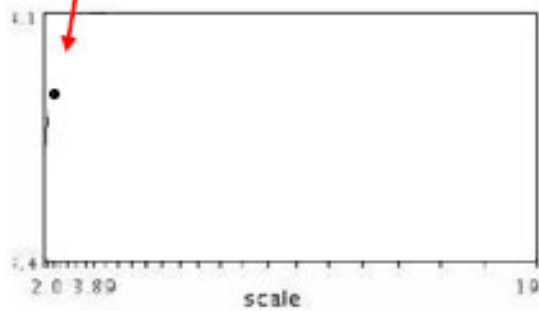
- Common approach:
  - Take a local maximum of this function.
  - Observation: region size for which the maximum is achieved should be *invariant* to image scale.



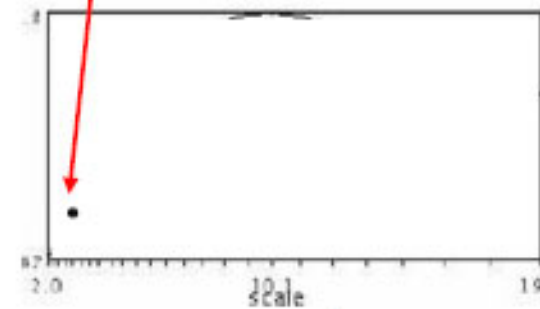
Slide credit: Kristen Grauman

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1 \dots i_m}(x, \sigma))$$

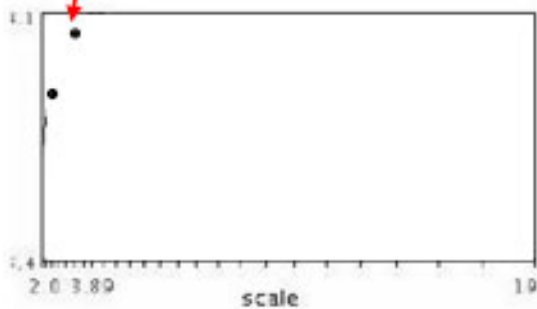


$$f(I_{i_1 \dots i_m}(x', \sigma))$$

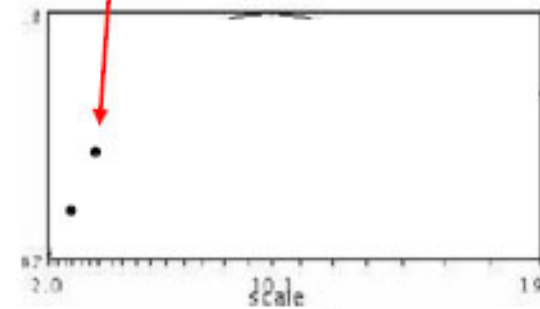
Slide credit: Krystian Mikolajczyk

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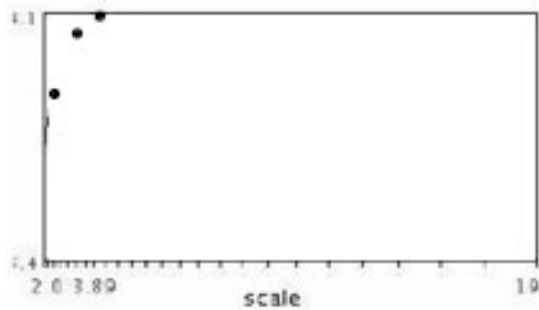


$$f(I_{i_1 \dots i_m}(x', \sigma))$$

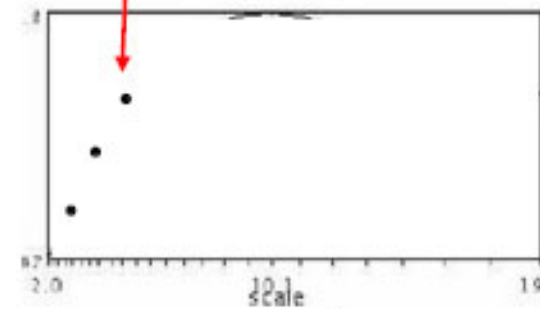
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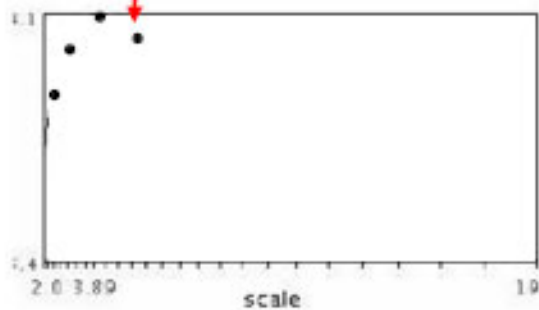


$$f(I_{i_1...i_m}(x', \sigma))$$

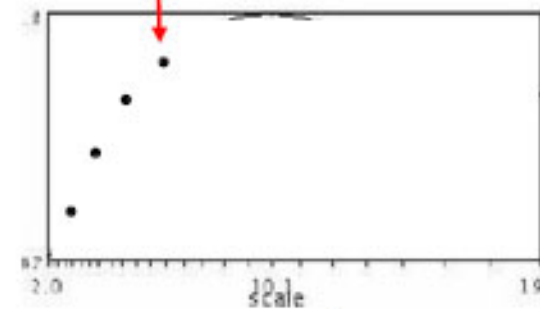
Slide credit: Krystian Mikolajczyk

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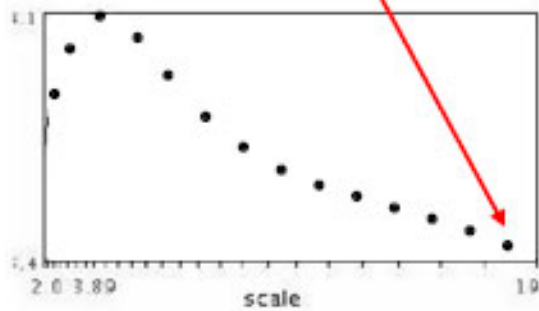


$$f(I_{i_1 \dots i_m}(x', \sigma))$$

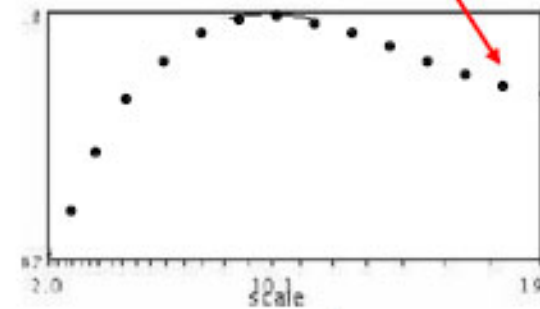
Slide credit: Krystian Mikolajczyk

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$$f(I_{i_1...i_m}(x, \sigma))$$

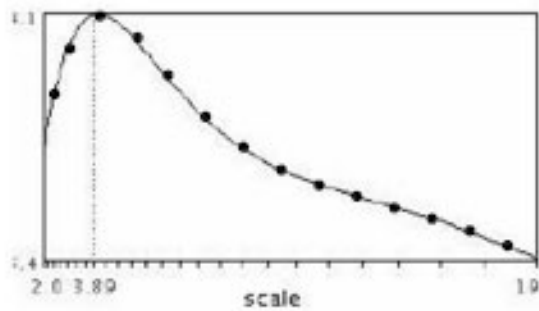


$$f(I_{i_1...i_m}(x', \sigma))$$

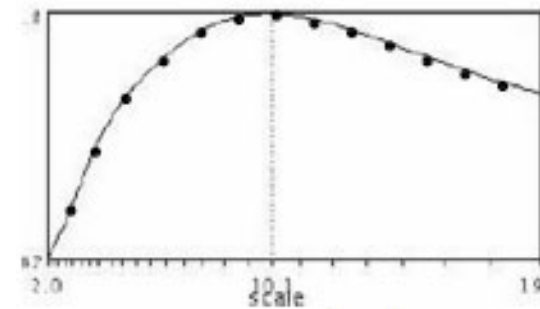
Slide credit: Krystian Mikolajczyk

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1...i_m}(x, \sigma))$$

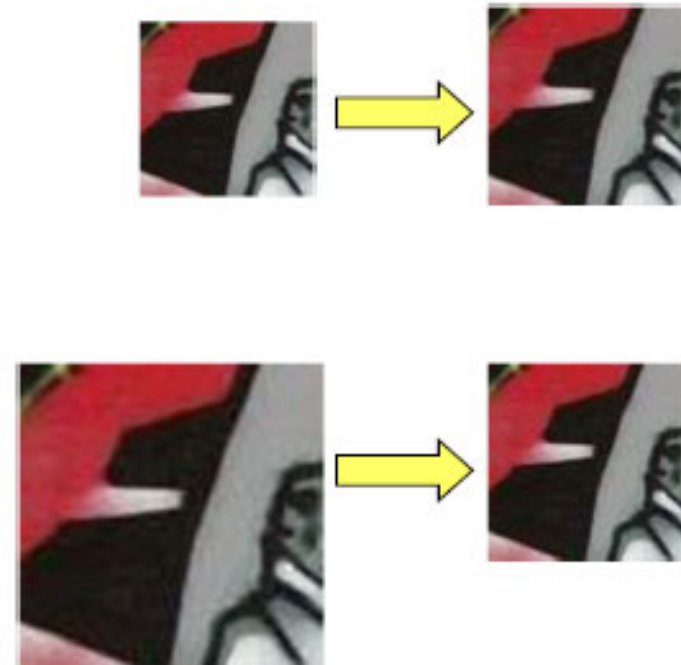
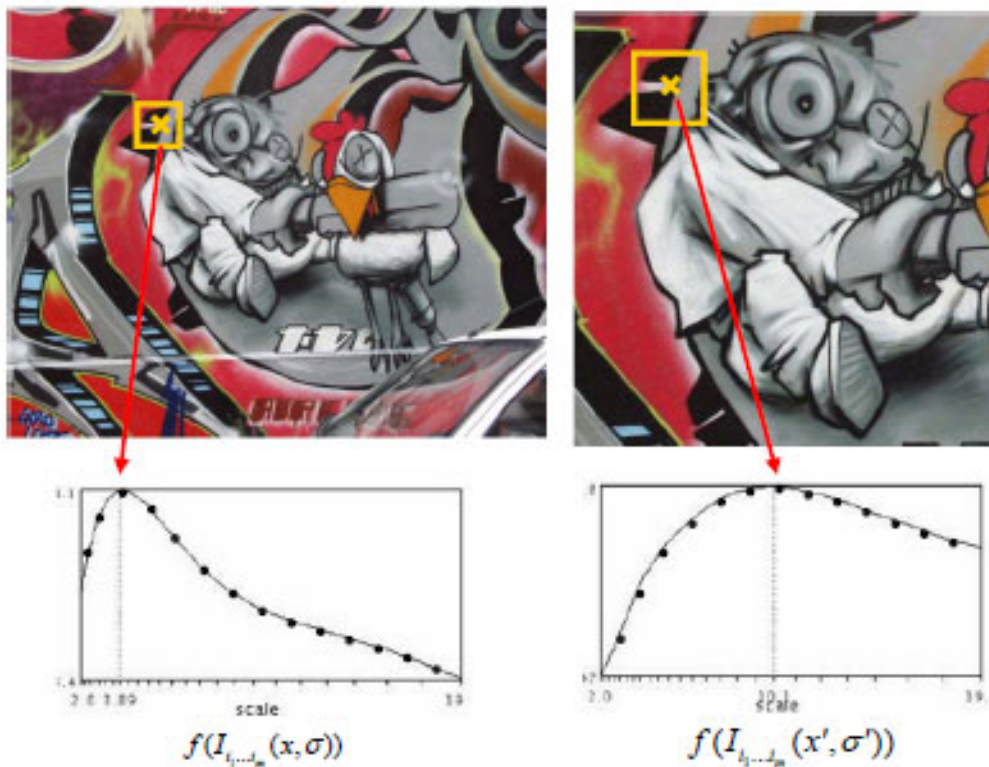


$$f(I_{i_1...i_m}(x', \sigma'))$$

Slide credit: Krystian Mikolajczyk

# Automatic Scale Selection

- Normalize: Rescale to fixed size

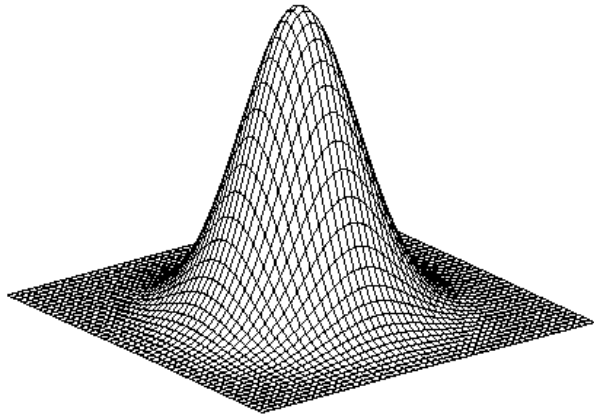


Slide credit: Timne Tuytelaars



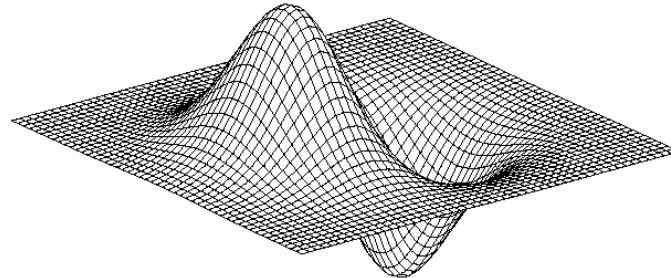
# What Is A Useful Signature Function?

- Laplacian-of-Gaussian = “blob” detector



**Gaussian**

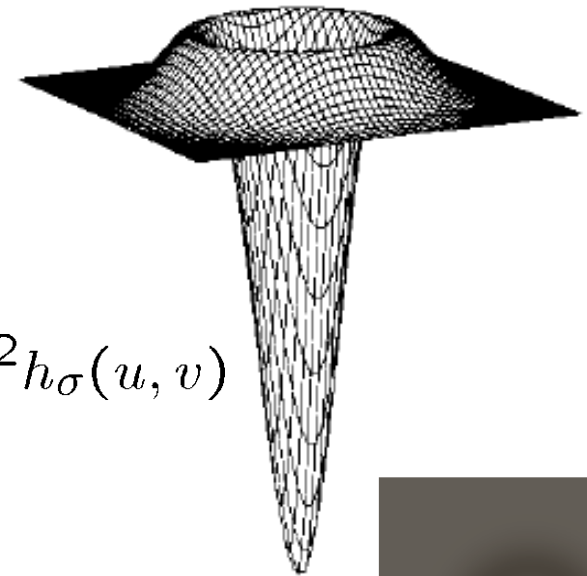
$$h_{\sigma}(u, v) = \frac{1}{2\pi\sigma^2} e^{-\frac{u^2+v^2}{2\sigma^2}}$$



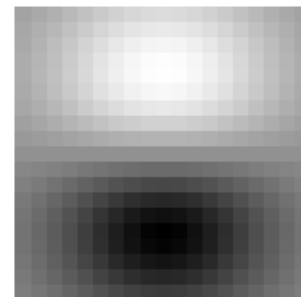
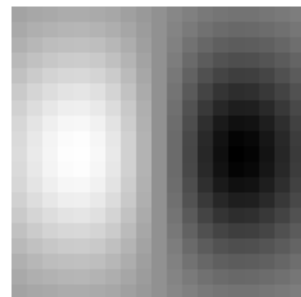
**Derivative of Gaussian**

$$\frac{\partial}{\partial x} h_{\sigma}(u, v)$$

**Laplacian of Gaussian**



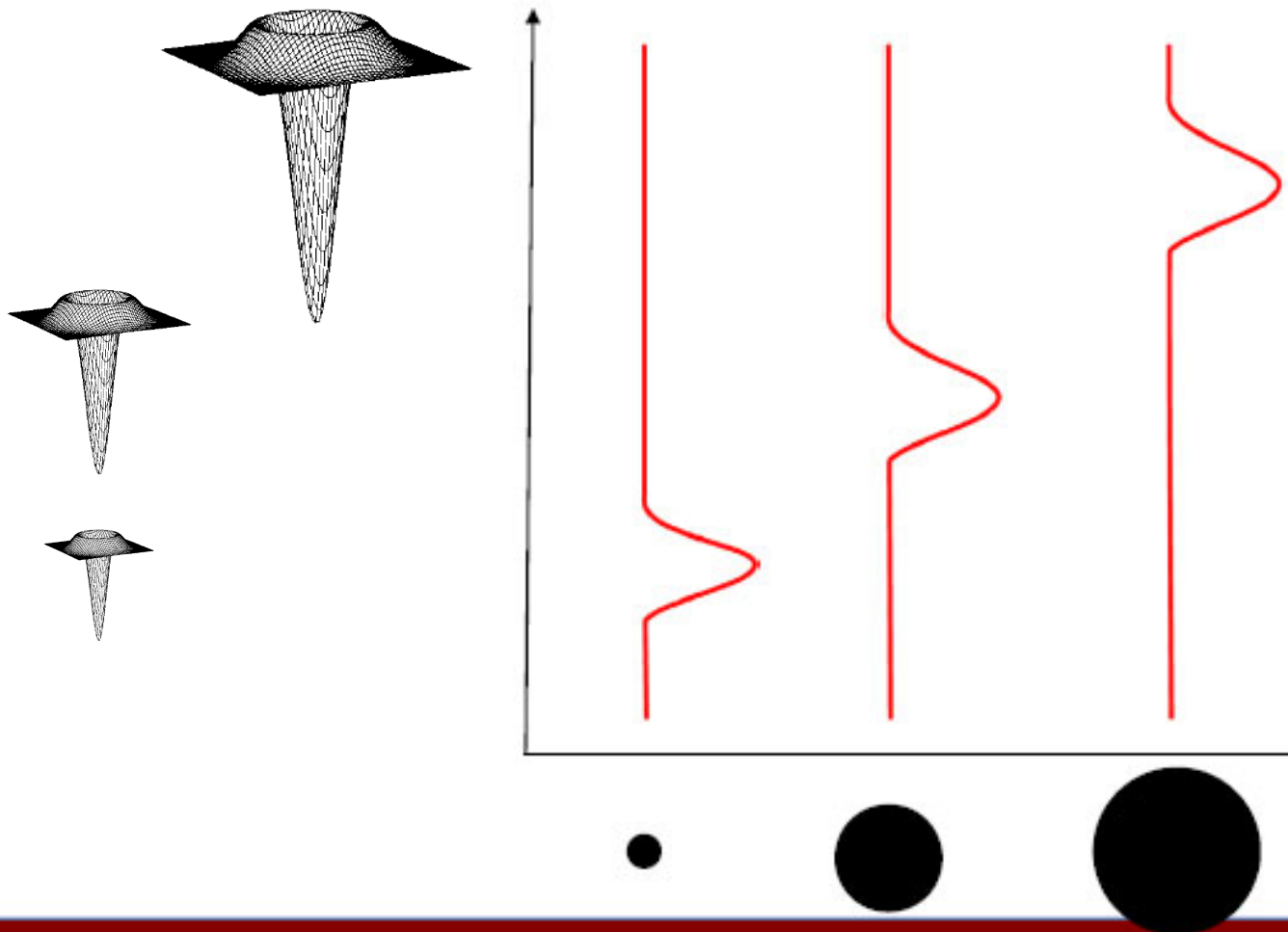
$$\nabla^2 h_{\sigma}(u, v)$$



Adapted from Steve Seitz, U of Washington

# What Is A Useful Signature Function?

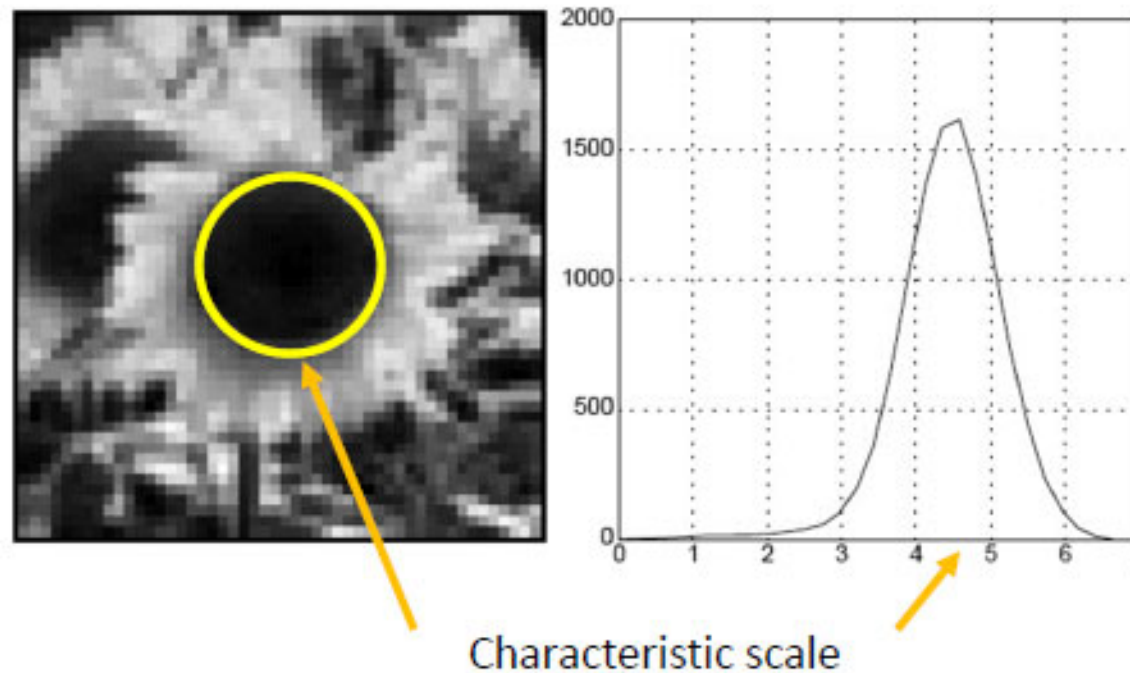
- Laplacian-of-Gaussian = “blob” detector



Slide credit: Bastian Leibe

# Characteristic Scale

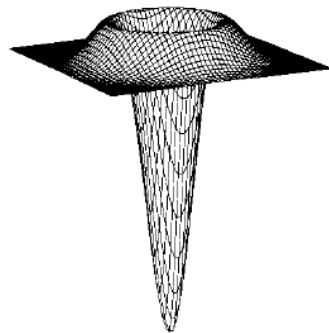
- We define the *characteristic scale* as the scale that produces peak of Laplacian response



T. Lindeberg (1998). "[Feature detection with automatic scale selection.](#)" *International Journal of Computer Vision* 30 (2): pp 77–116.

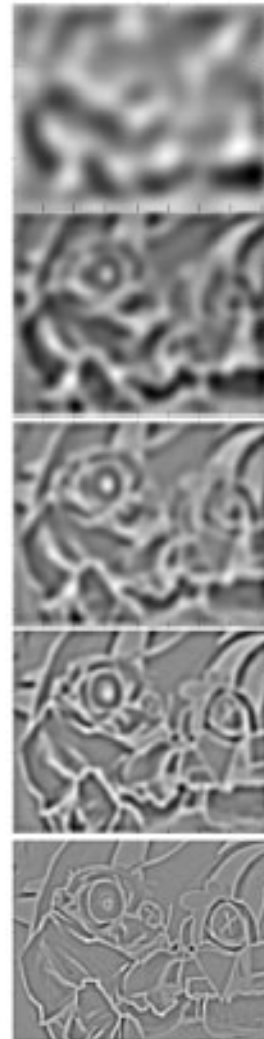
# Laplacian-of-Gaussian (LoG)

- Interest points:
  - Local maxima in scale space of Laplacian-of-Gaussian



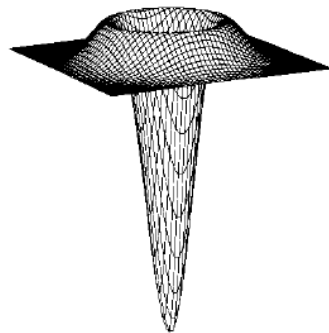
$$L_{xx}(\sigma) + L_{yy}(\sigma)$$

$\sigma_5$   
 $\sigma_4$   
 $\sigma_3$   
 $\sigma_2$   
 $\sigma$



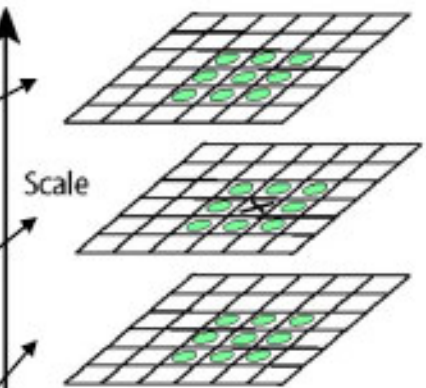
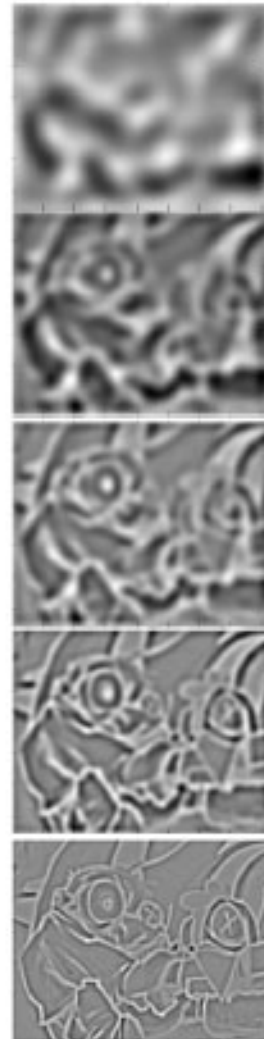
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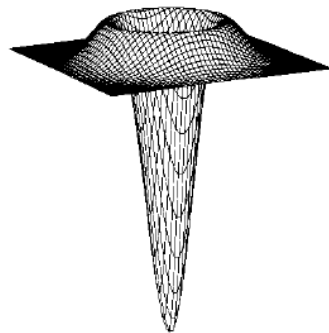


Slide adapted from



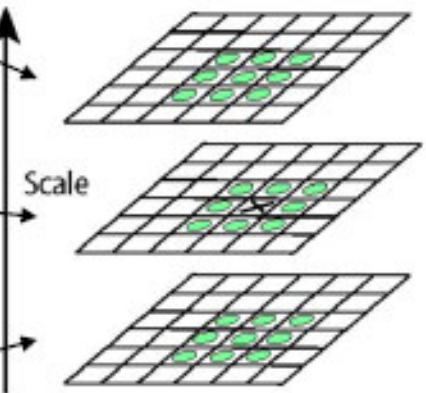
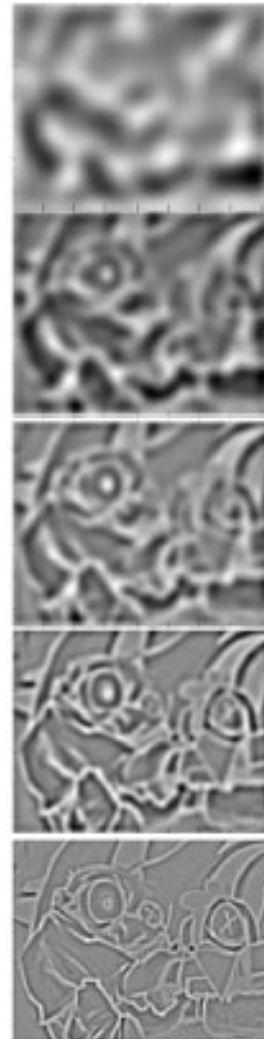
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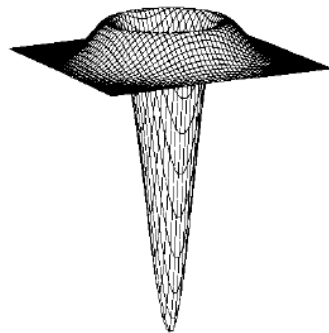
$\sigma_5$   
 $\sigma_4$   
 $\sigma_3$   
 $\sigma_2$   
 $\sigma$



Slide adapted from

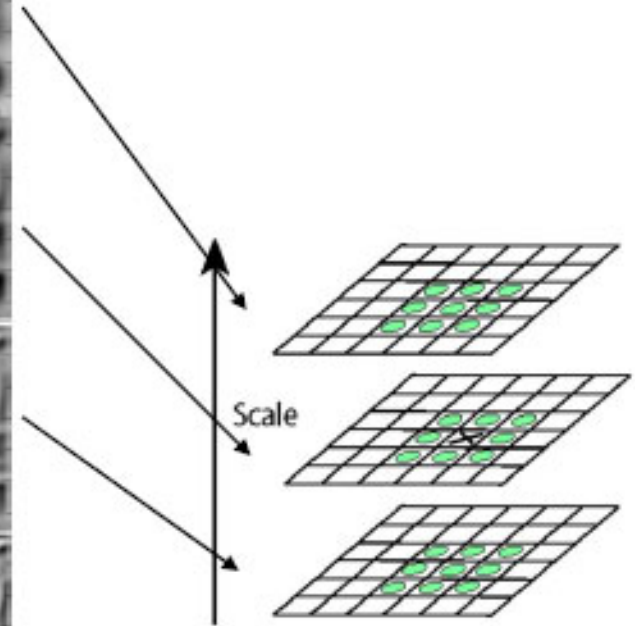
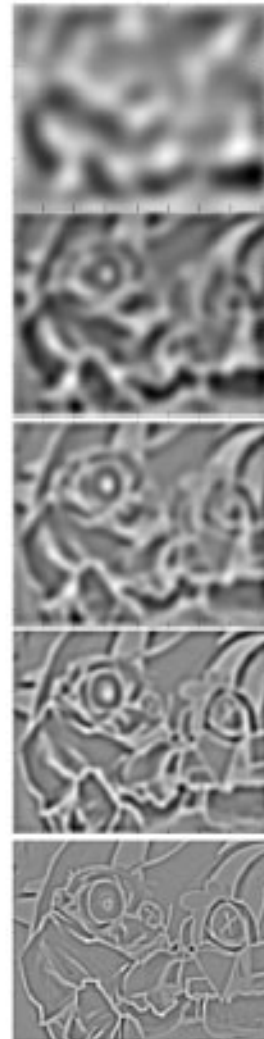
# Laplacian-of-Gaussian (LoG)

- Interest points:
  - Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma)$$

$\sigma_5$   
 $\sigma_4$   
 $\sigma_3$   
 $\sigma_2$   
 $\sigma$



$\Rightarrow$  List of  $(x, y, \sigma)$

Slide adapted from

# LoG Detector: Workflow



Slide credit: Svetlana Lazebnik



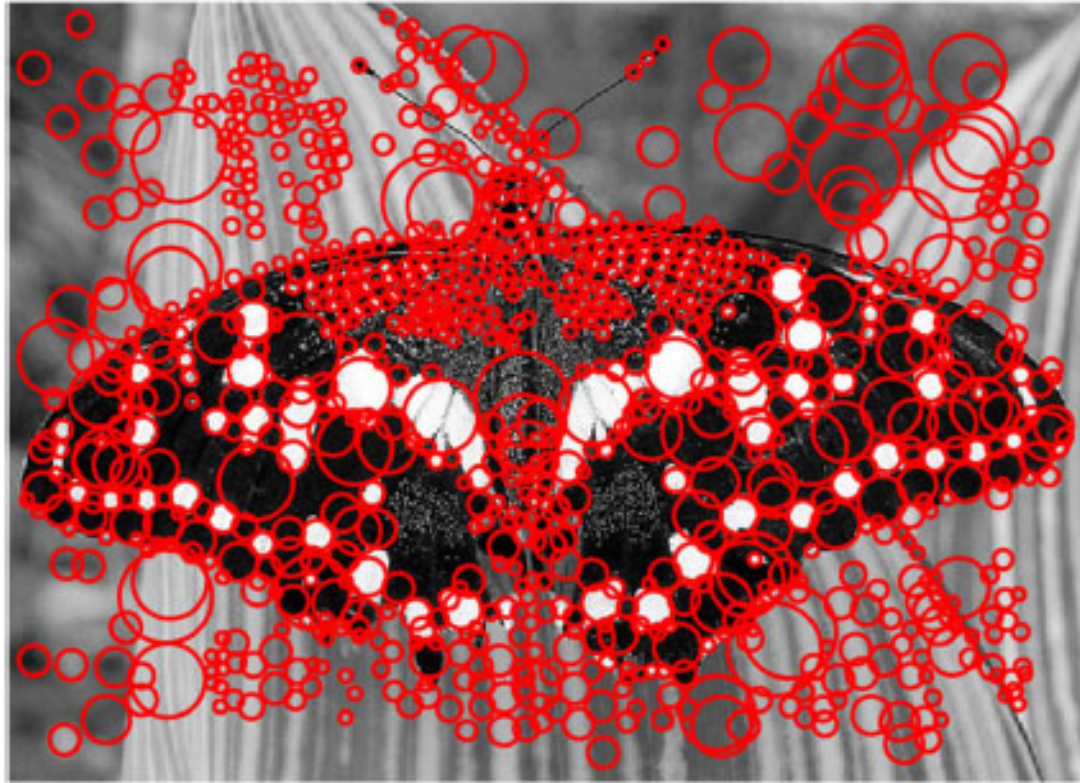


# LoG Detector: Workflow



sigma = 11.9912

# LoG Detector: Workflow



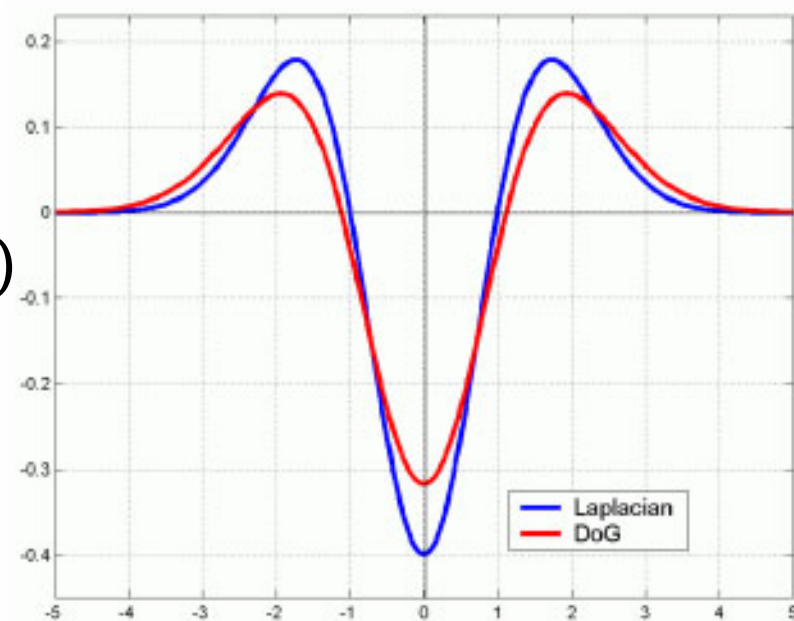
Slide credit: Svetlana Lazebnik

# Approximating LoG

- Efficiently approximate LoG with a Difference of Gaussian (DoG)

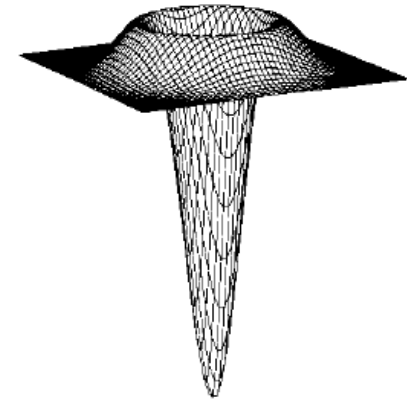
$$LoG = \sigma^2 (L_{xx}(x, y, \sigma) + L_{yy}(x, y, \sigma))$$

$$DoG = (G(x, y, k\sigma) - G(x, y, \sigma))$$



# Difference-of-Gaussian (DoG)

- Difference of Gaussians as approximation of the LoG
  - This is used e.g. in Lowe's SIFT pipeline for feature detection.
- Advantages
  - No need to compute 2<sup>nd</sup> derivatives
  - Gaussians are computed anyway, e.g. in a Gaussian pyramid.



-



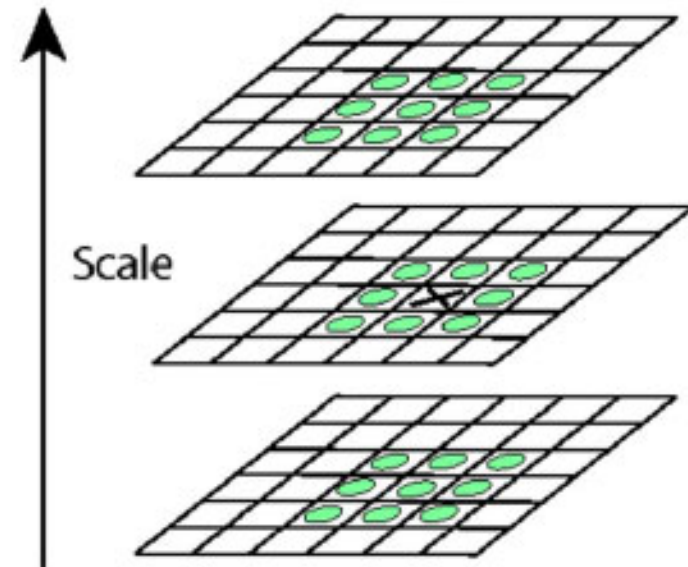
=



Slide credit: Bastian Leibe

# Key point localization with DoG

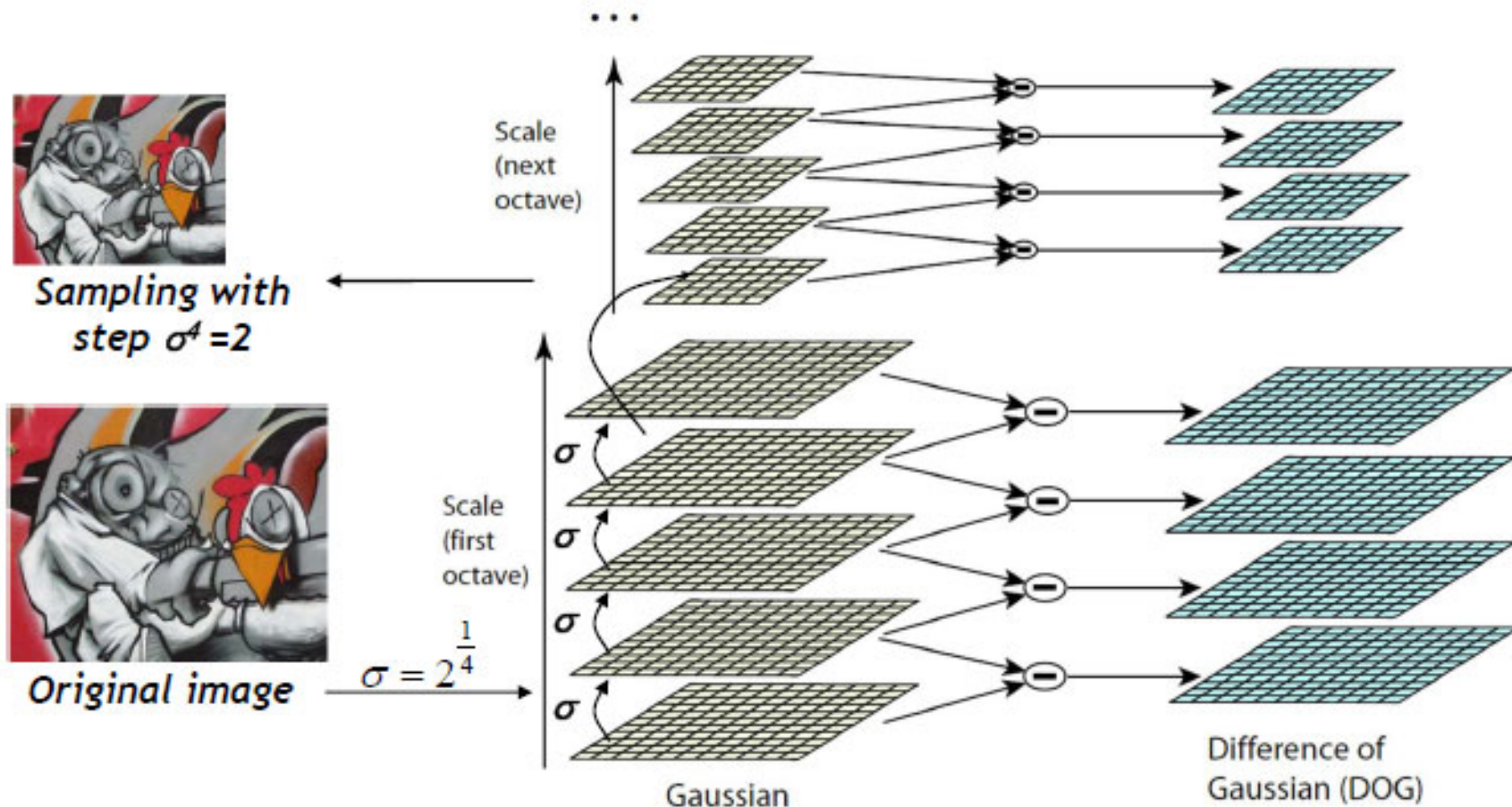
- Detect maxima of difference-of-Gaussian (DoG) in scale space
- Then reject points with low contrast (threshold)
- Eliminate edge responses



Candidate keypoints:  
list of  $(x, y, \sigma)$

# DoG – Efficient Computation

- Computation in Gaussian scale pyramid



Slide adapted from Krystian Mikolajczyk

# Results: Lowe's DoG



Slide credit: Bastian Leibe

# Example of Keypoint Detection



(a) 233x189 image

(b) 832 DoG extrema

(c) 729 left after peak value threshold

(d) 536 left after testing ratio of principle curvatures (removing edge responses)

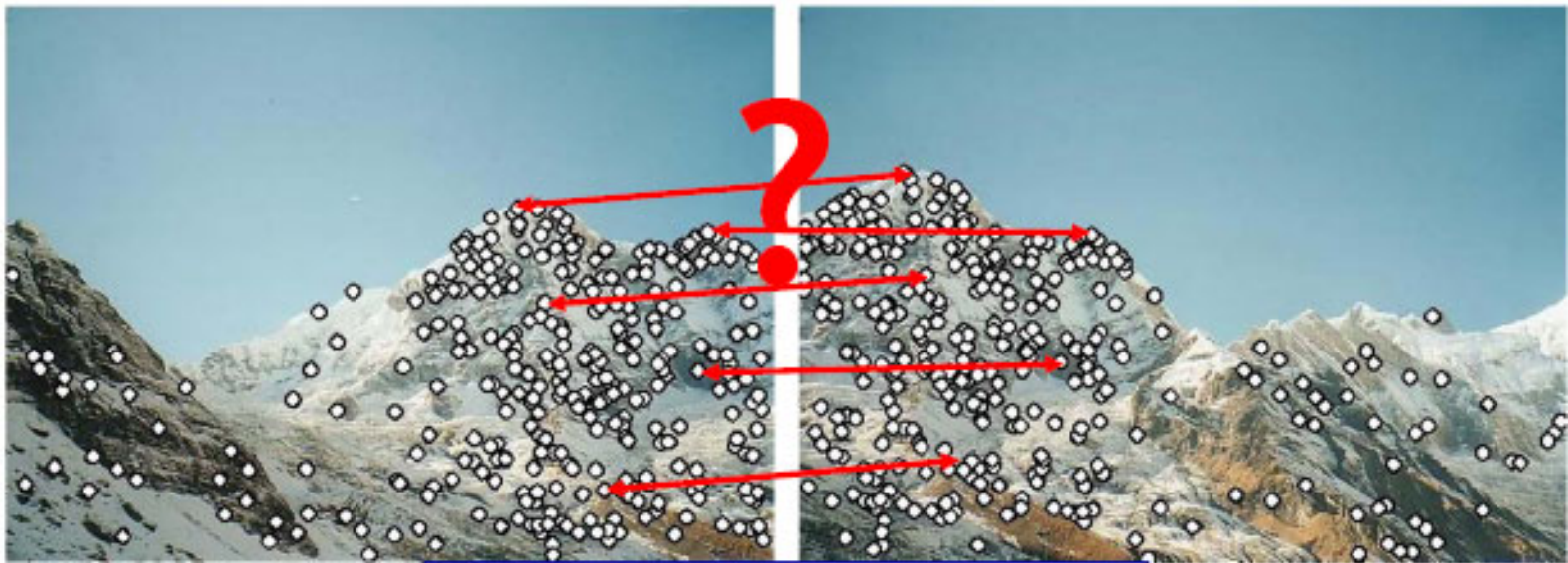
Slide credit: David Lowe



# Local Descriptors

- We know how to detect points
- Next question:

How to *describe* them for matching?



Point descriptor should be:

1. Invariant
2. Distinctive

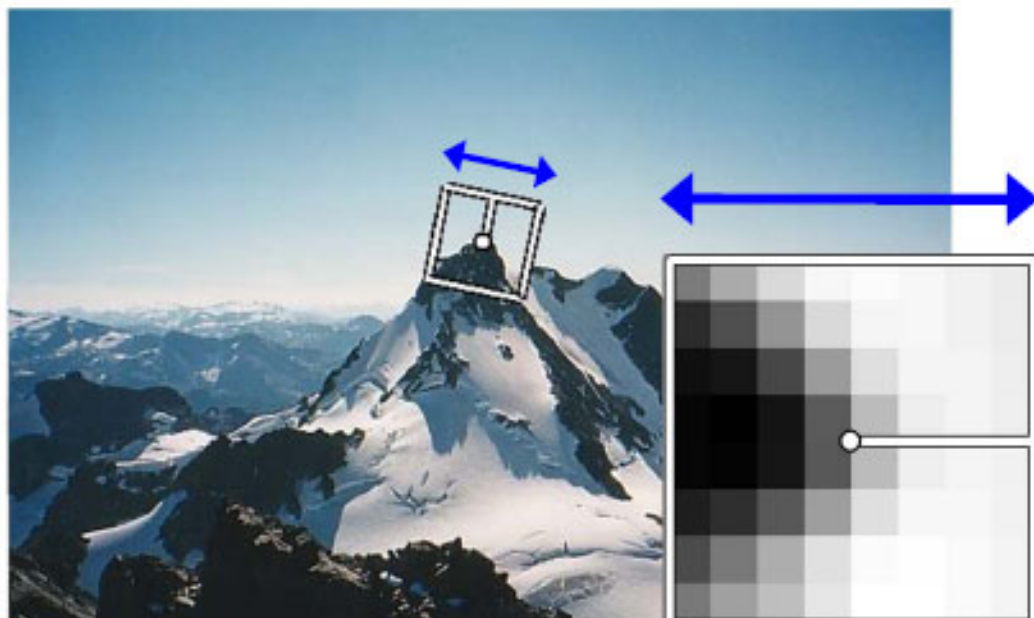
Slide credit: Kristen Grauman

# Rotation Invariant Descriptors

- Find local orientation
  - Dominant direction of gradient for the image patch



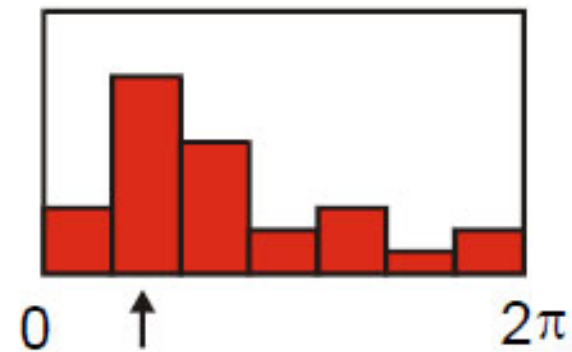
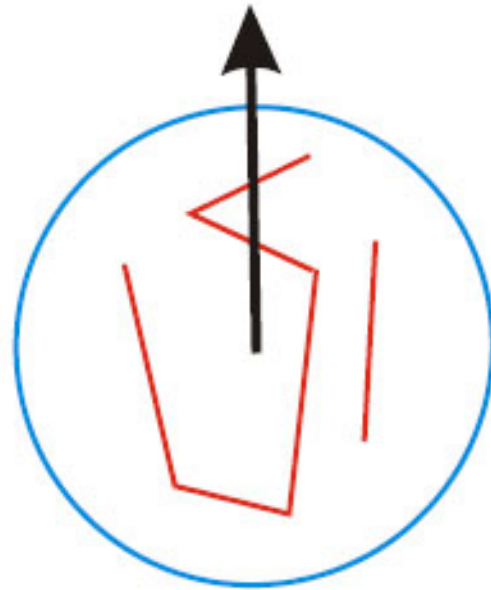
- Rotate patch according to this angle
  - This puts the patches into a canonical orientation.



# Orientation Normalization: Computation

[Lowe, SIFT, 1999]

- Compute orientation histogram
- Select dominant orientation
- Normalize: rotate to fixed orientation

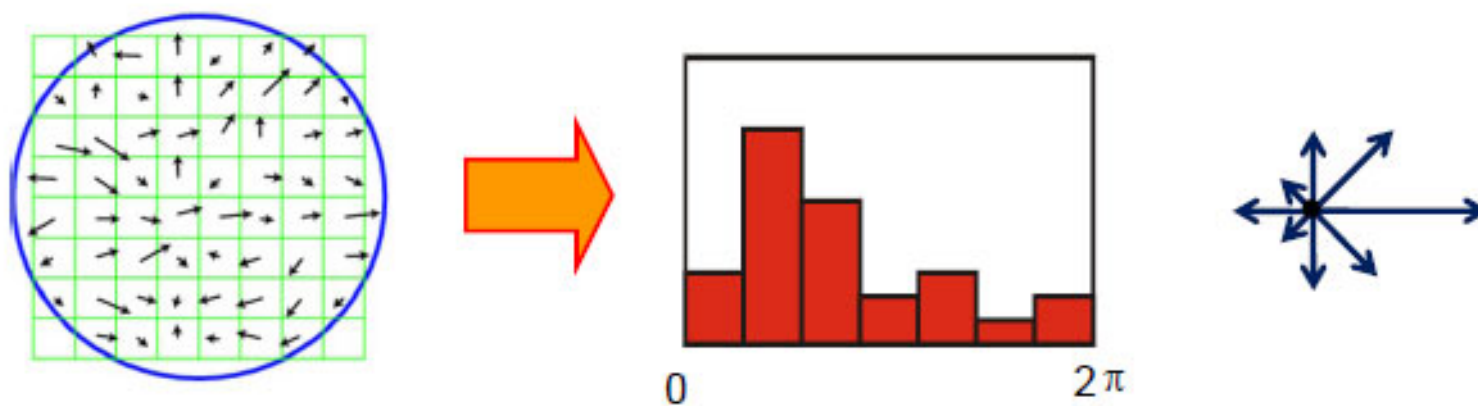


# Feature Descriptors

- Disadvantage of patches as descriptors:
  - Small shifts can affect matching score a lot

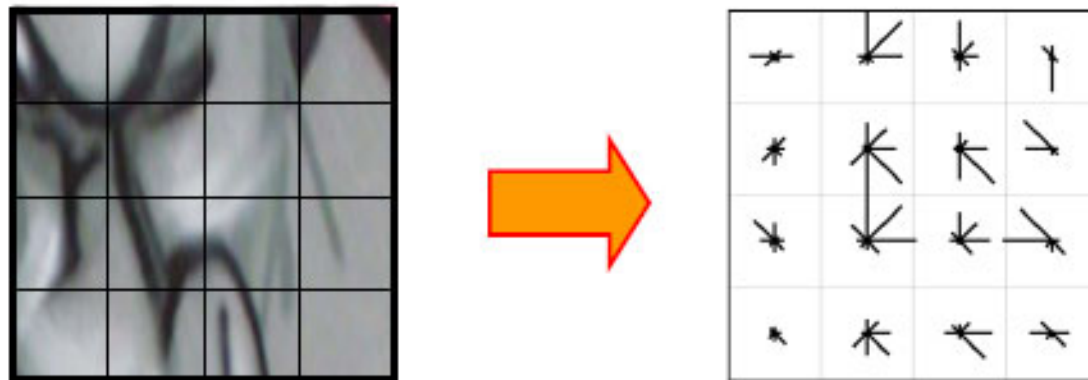


- Solution: histograms



# Feature Descriptors: SIFT

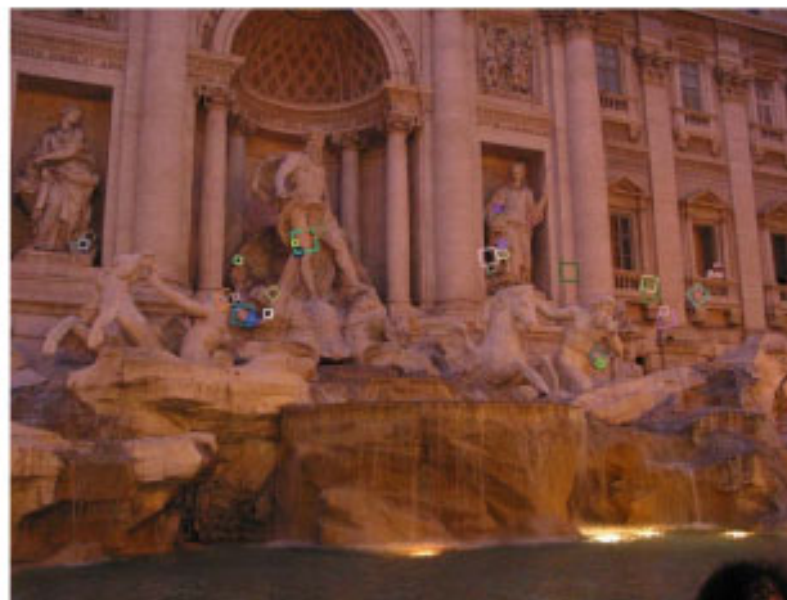
- Scale Invariant Feature Transform
- Descriptor computation:
  - Divide patch into 4x4 sub-patches: 16 cells
  - Compute histogram of gradient orientations (8 reference angles) for all pixels inside each sub-patch
  - Resulting descriptor:  $4 \times 4 \times 8 = 128$  dimensions



David G. Lowe. "[Distinctive image features from scale-invariant keypoints.](#)" *IJCV* 60 (2), pp. 91-110, 2004.

# Overview: SIFT

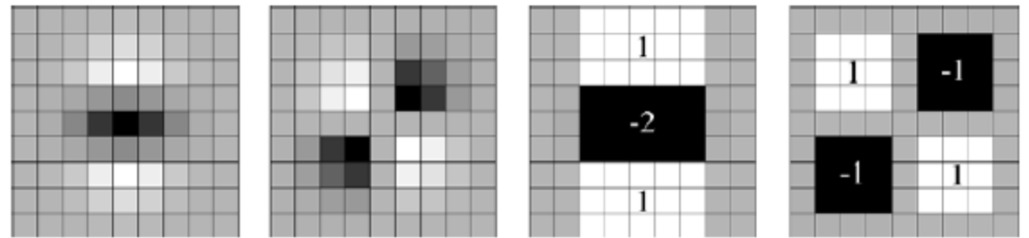
- Extraordinarily robust matching technique
  - Can handle changes in viewpoint up to  $\sim 60$  deg. out-of-plane rotation
  - Can handle significant changes in illumination
    - Sometimes even day vs. night (below)
  - Fast and efficient—can run in real time
  - Lots of code available
    - [http://people.csail.mit.edu/albert/ladypack/wiki/index.php/Known\\_implementations\\_of\\_SIFT](http://people.csail.mit.edu/albert/ladypack/wiki/index.php/Known_implementations_of_SIFT)



# Other Descriptors

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- **GIST: a kind of SIFT in a global scale**
- **SURF: an acceleration using the integral image, i.e., summed area table**

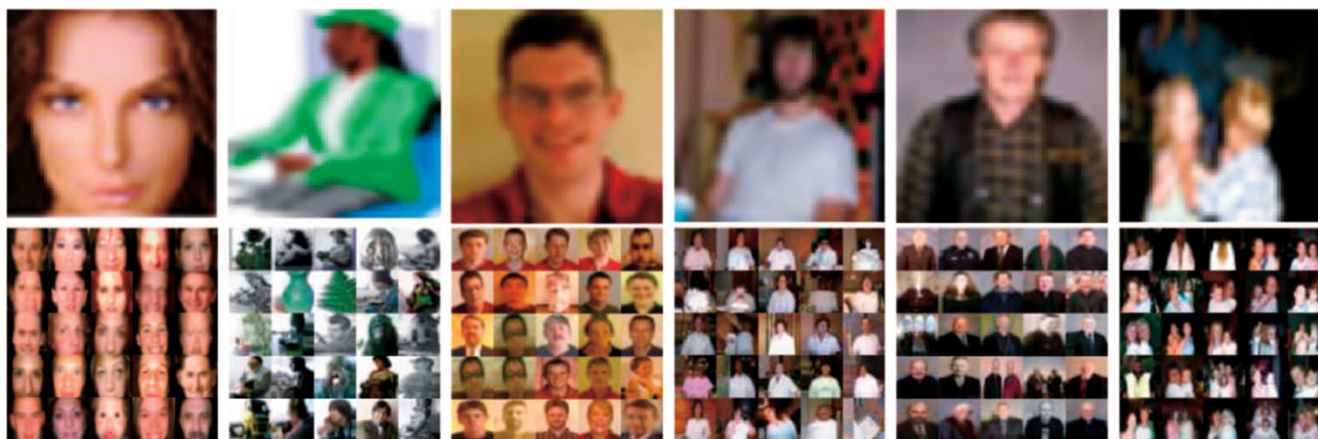


- **CNN features**

# 80M Tiny Images

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- **Just use 32 by 32 images**
- **It works well even for recognition with a simple recognition method (nearest neighbor search) with using 80M data**



- **Indicates the importance of data**



# PA1 (Optional)

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- **Objective**

- **Understand how to extract SIFT features and to use related libraries (OpenCV, vlfeat, ... )**



# Class Objectives (Ch. 2.2 & 2.3) were:

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- **Scale invariant region selection**
  - **Automatic scale selection**
  - **Laplacian of Gradients (LoG)  $\approx$  Difference of Gradients (DoG)**
  - **SIFT as a local descriptor**

# Next Time...

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- **Deep learning based image search**

# Homework for Every Class

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- **Go over the next lecture slides**
- **Come up with one question on what we have discussed today**
  - 1 for typical questions (that were answered in the class)
  - 2 for questions with thoughts or that surprised me
- **Write questions 3 times before the mid-term exam**
  - Write a question about one out of every four classes
  - Multiple questions in one time will be counted as one time
- **Common questions are compiled at [the Q&A file](#)**
  - Some of questions will be discussed in the class
- **If you want to know the answer of your question, ask me or TA [on person](#)**