
CS688: Web-Scale Image Search
Scale Invariant Region Selection and
SIFT

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Course URL:
<http://sglab.kaist.ac.kr/~sungeui/IR>

KAIST



Class Objectives

- **Scale invariant region selection**
 - Automatic scale selection
 - Laplacian of Gradients (LoG) \approx Difference of Gradients (DoG)
 - SIFT as a local descriptor

From Points to Regions...

- The Harris and Hessian operators define interest points.
 - Precise localization
 - High repeatability

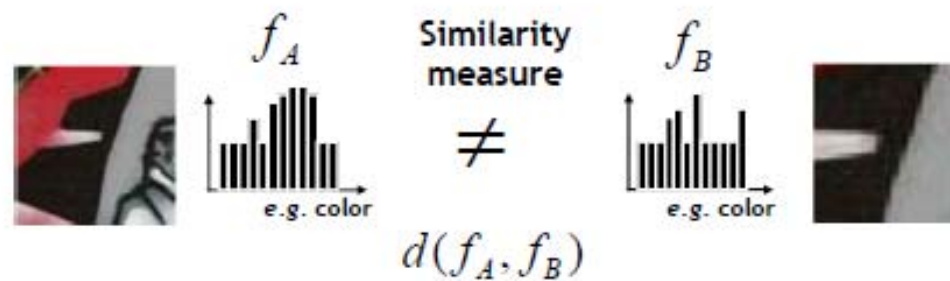


- In order to compare those points, we need to compute a descriptor over a region.
 - How can we define such a region in a scale invariant manner?
- *I.e. how can we detect scale invariant interest regions?*

Source: Bastian Leibe

Naïve Approach: Exhaustive Search

- Multi-scale procedure
 - Compare descriptors while varying the patch size

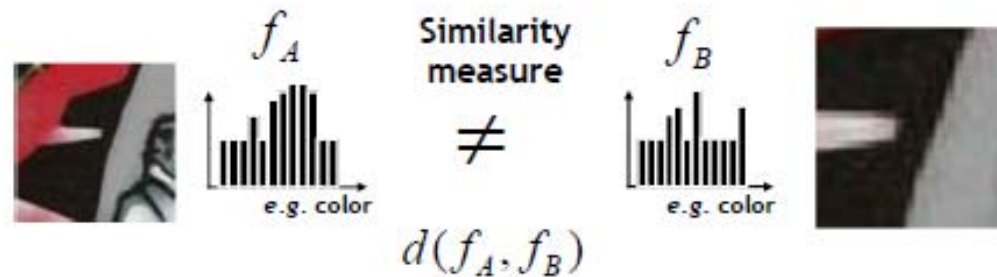


Slide credit: Krystian Mikolajczyk



Naïve Approach: Exhaustive Search

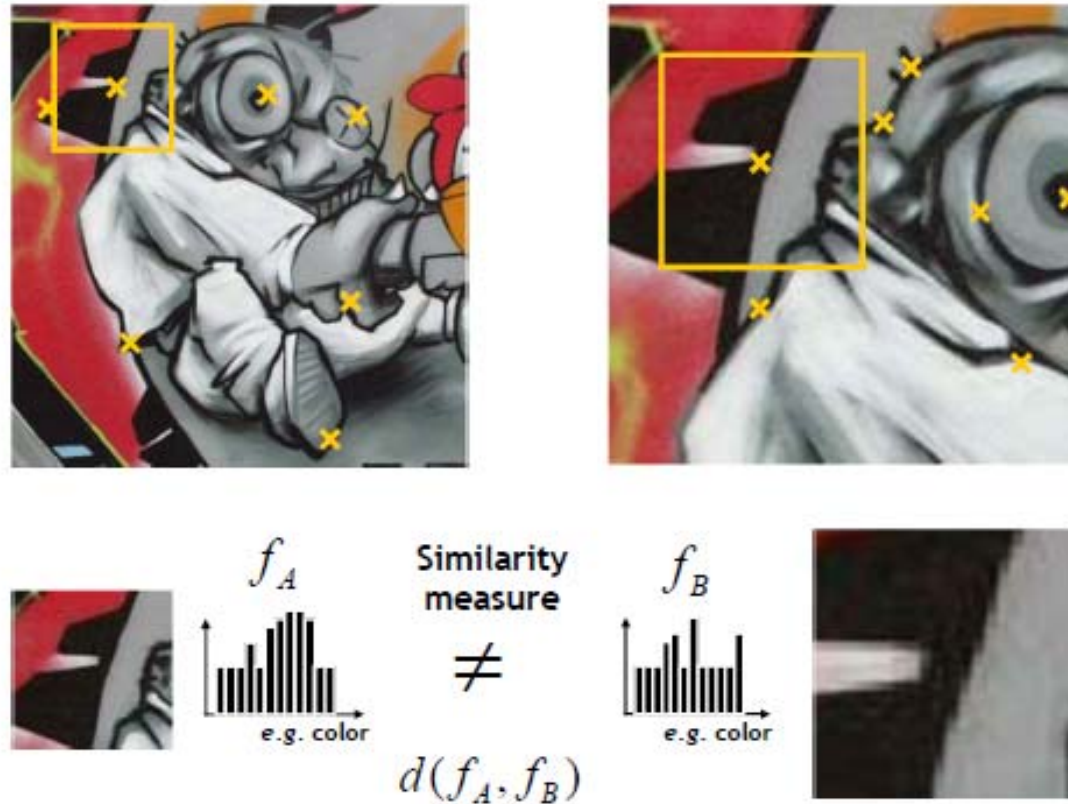
- Multi-scale procedure
 - Compare descriptors while varying the patch size



Slide credit: Krystian Mikolajczyk

Naïve Approach: Exhaustive Search

- Multi-scale procedure
 - Compare descriptors while varying the patch size



Slide credit: Krystian Mikolajczyk

Naïve Approach: Exhaustive Search

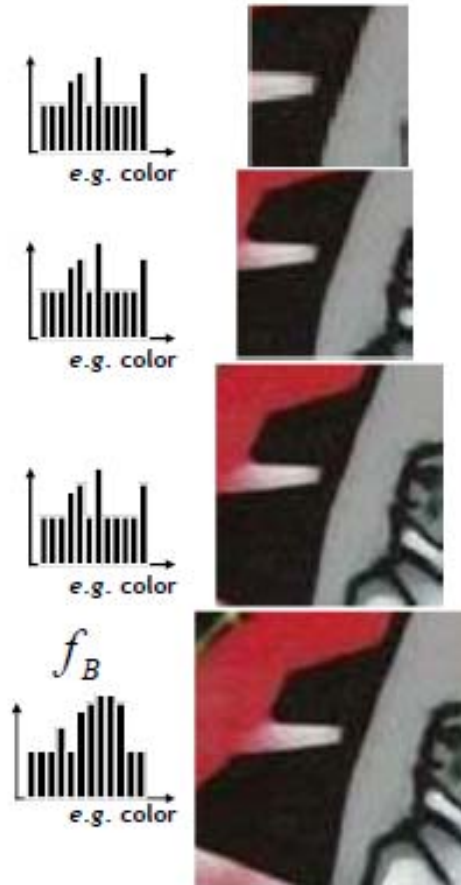
- Comparing descriptors while varying the patch size
 - Computationally inefficient
 - Inefficient but possible for matching
 - Prohibitive for retrieval in large databases
 - Prohibitive for recognition



Similarity
measure

=

$d(f_A, f_B)$



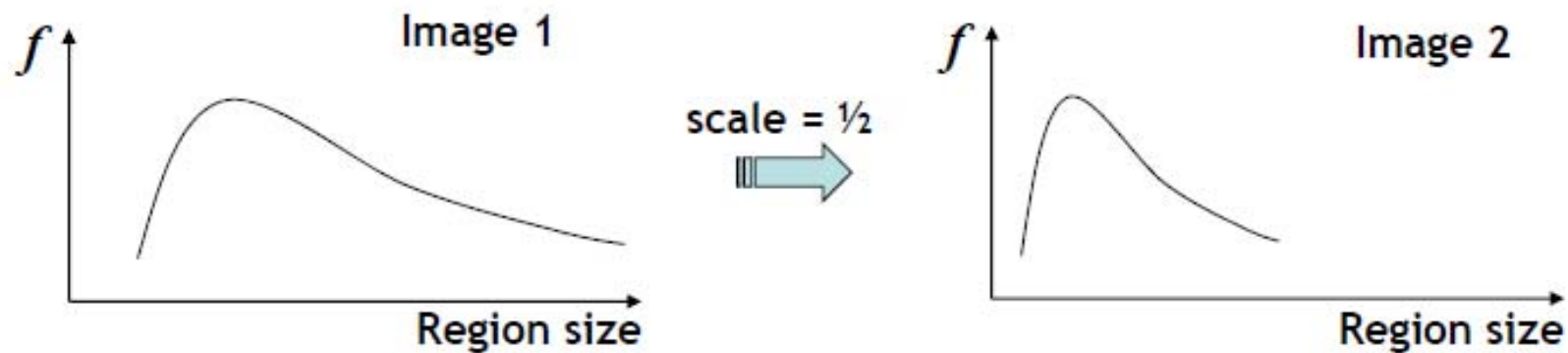
Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

- Solution:
 - Design a function on the region, which is “scale invariant”
(the same for corresponding regions, even if they are at different scales)

Example: average intensity. For corresponding regions (even of different sizes) it will be the same.

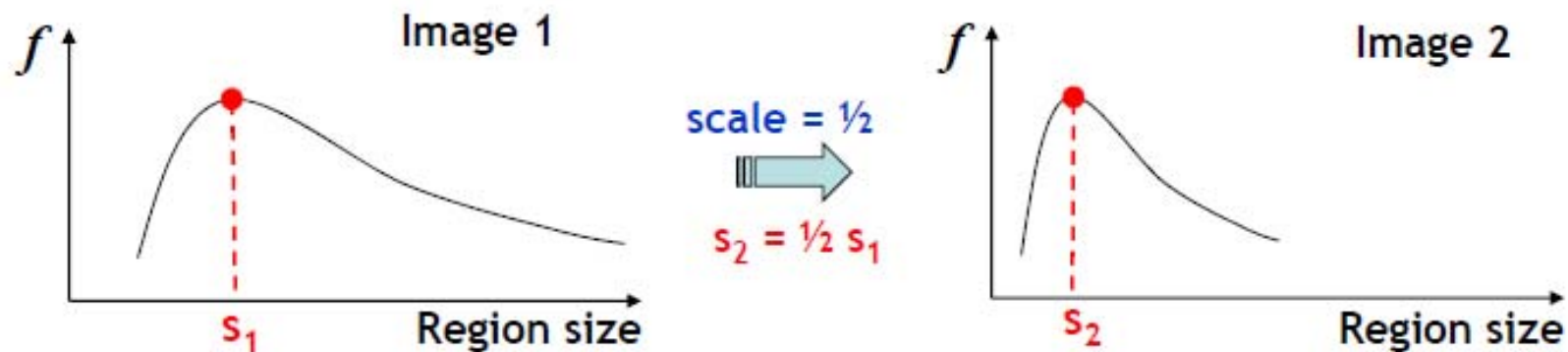
- For a point in one image, we can consider it as a function of region size (patch width)



Slide credit: Kristen Grauman

Automatic Scale Selection

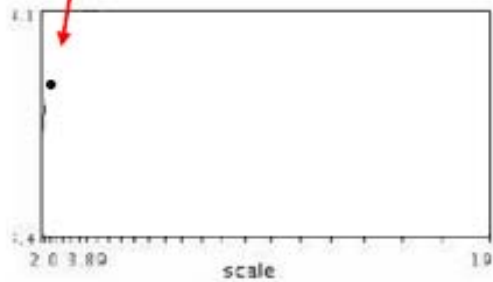
- Common approach:
 - Take a local maximum of this function.
 - Observation: region size for which the maximum is achieved should be *invariant* to image scale.



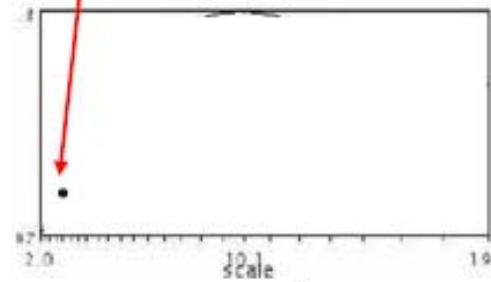
Slide credit: Kristen Grauman

Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1...i_m}(x, \sigma))$$

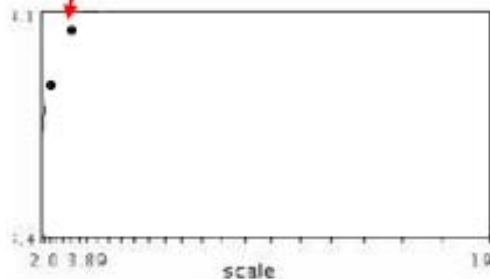


$$f(I_{i_1...i_m}(x', \sigma))$$

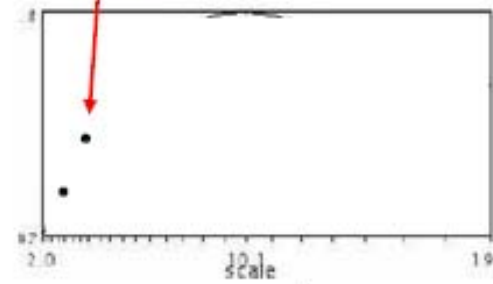
Slide credit: Krystian Mikolajczyk

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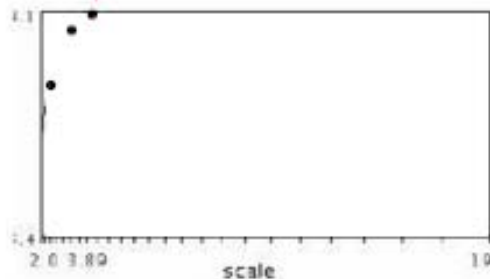


$$f(I_{i_1...i_m}(x', \sigma))$$

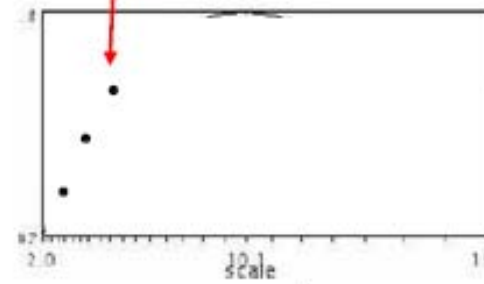
Slide credit: Krystian Mikolajczyk

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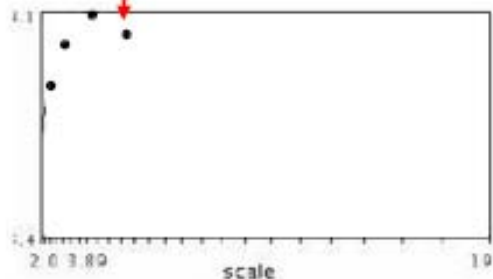


$$f(I_{i_1...i_m}(x', \sigma))$$

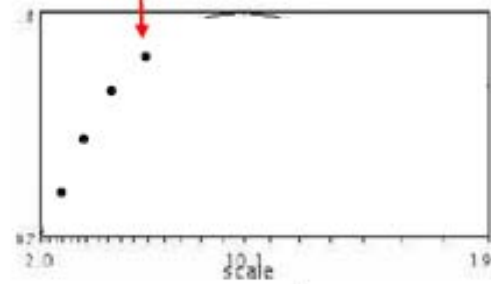
Slide credit: Krystian Mikolajczyk

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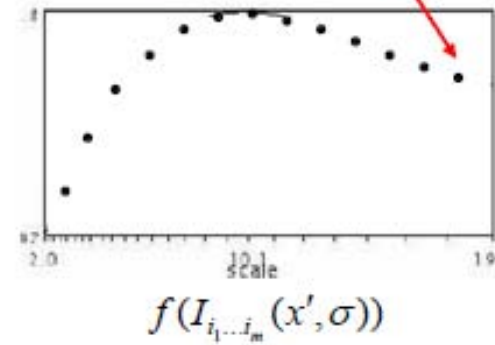
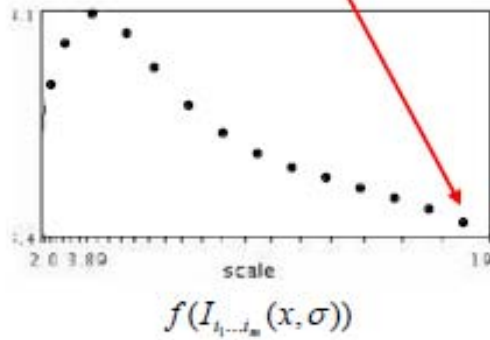


$$f(I_{i_1...i_m}(x', \sigma))$$

Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

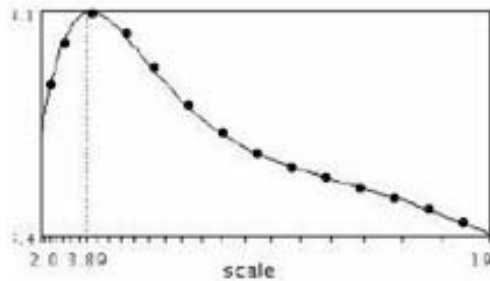
- Function responses for increasing scale (scale signature)



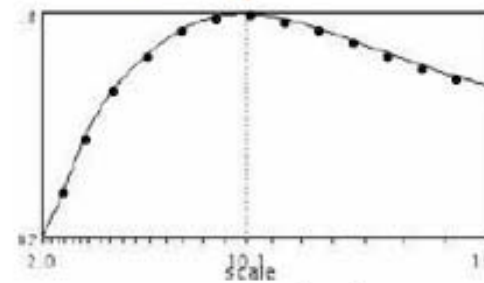
Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1 \dots i_m}(x, \sigma))$$

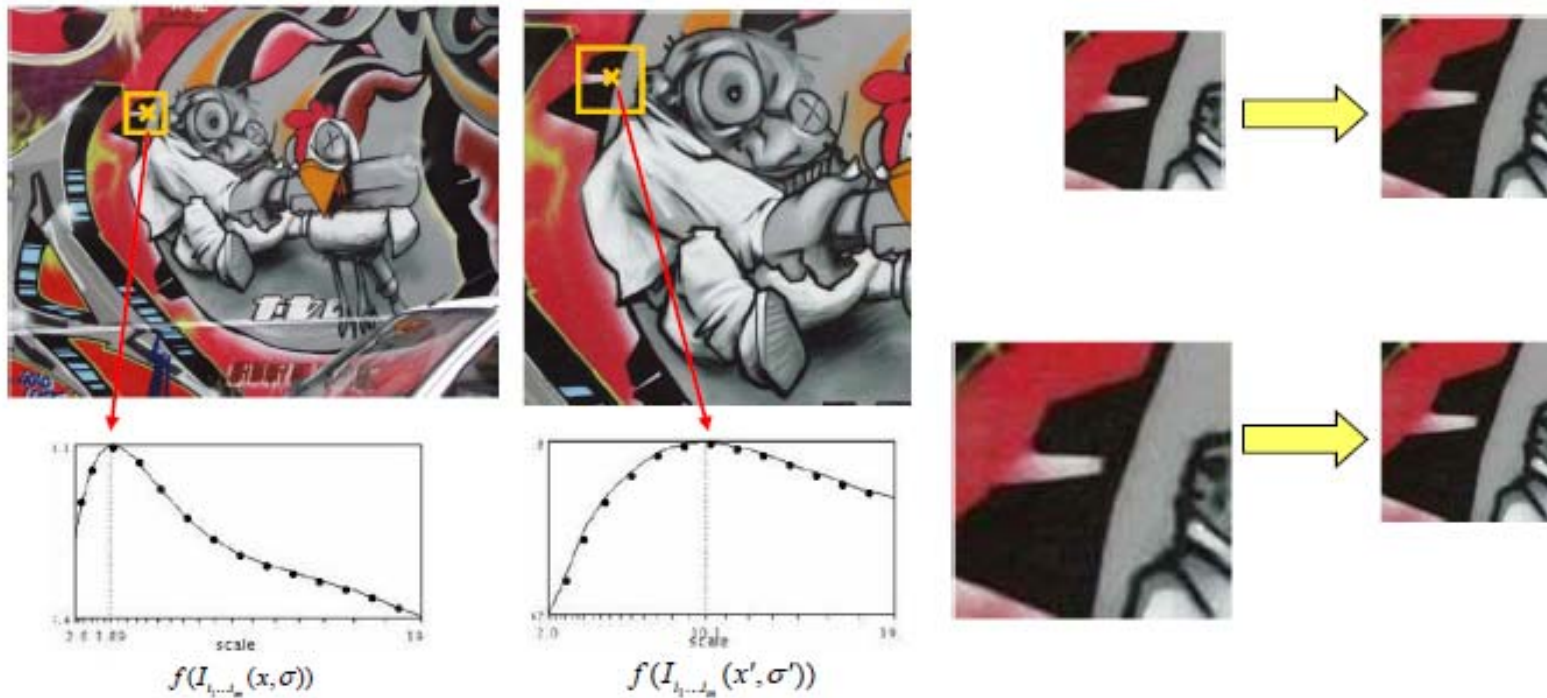


$$f(I_{i_1 \dots i_m}(x', \sigma'))$$

Slide credit: Krystian Mikolajczyk

Automatic Scale Selection

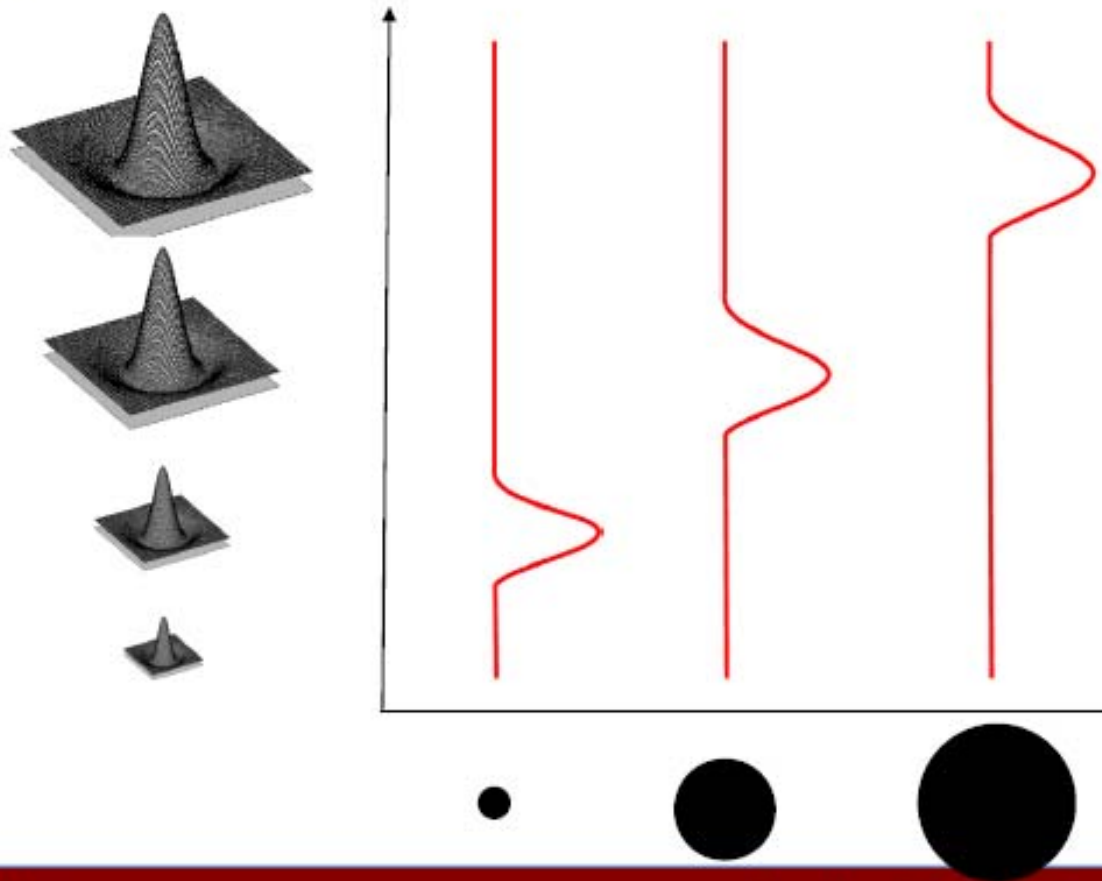
- Normalize: Rescale to fixed size



Slide credit: Tinne Tuytelaars

What Is A Useful Signature Function?

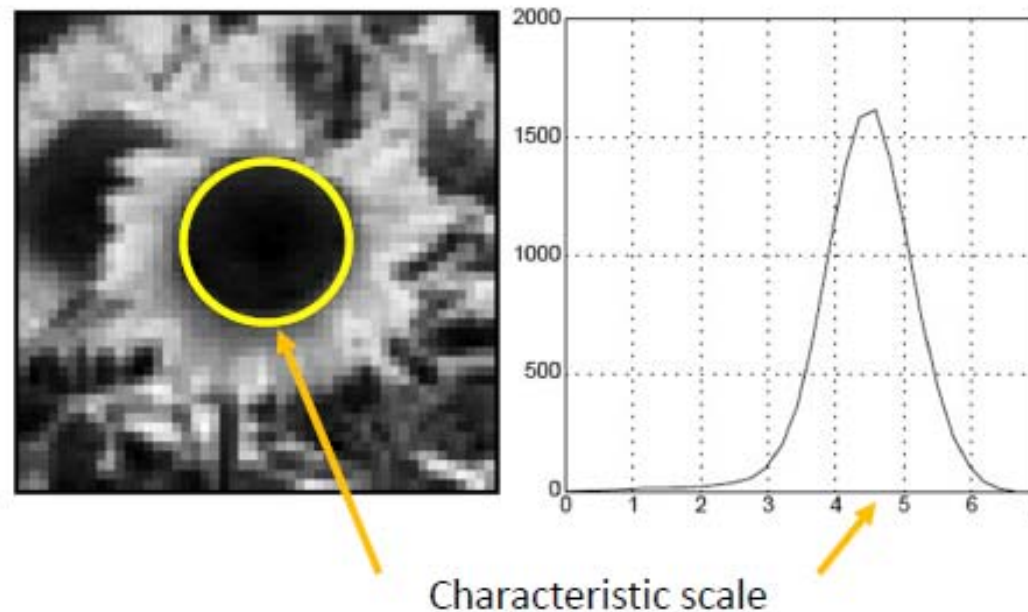
- Laplacian-of-Gaussian = “blob” detector



Slide credit: Bastian Leibe

Characteristic Scale

- We define the *characteristic scale* as the scale that produces peak of Laplacian response

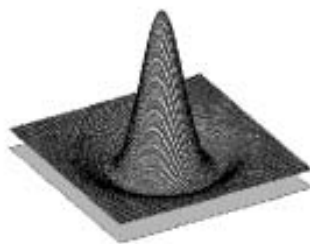


T. Lindeberg (1998). "[Feature detection with automatic scale selection.](#)" *International Journal of Computer Vision* 30 (2): pp 77–116.

Slide credit: Svetlana Lazebnik

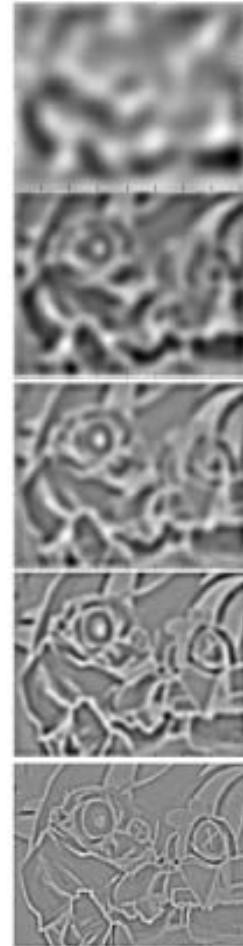
Laplacian-of-Gaussian (LoG)

- Interest points:
 - Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma)$$

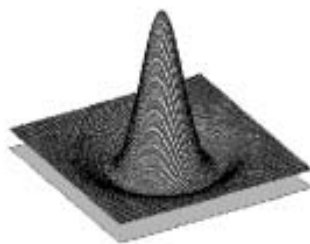
σ_5
 σ_4
 σ_3
 σ_2
 σ_1



Slide adapted from Krystian Mikolajczyk

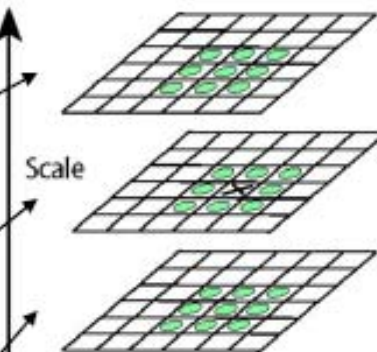
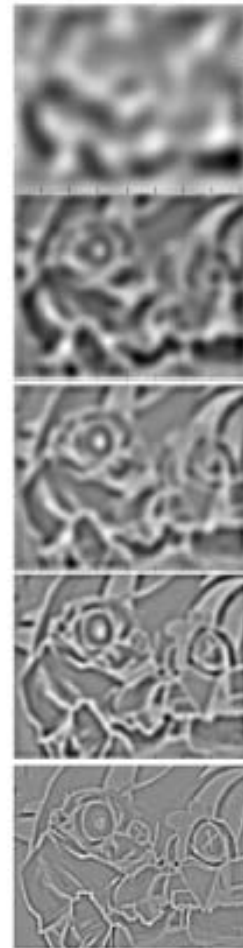
Laplacian-of-Gaussian (LoG)

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$$L_{xx}(\sigma) + L_{yy}(\sigma)$$

σ_5
 σ_4
 σ_3
 σ_2
 σ

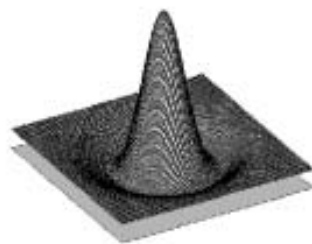


Slide adapted from



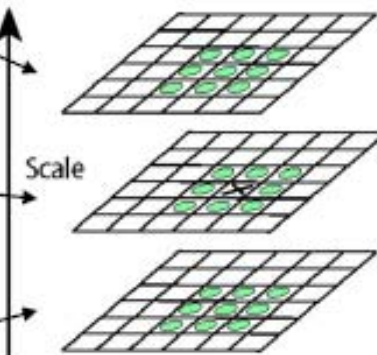
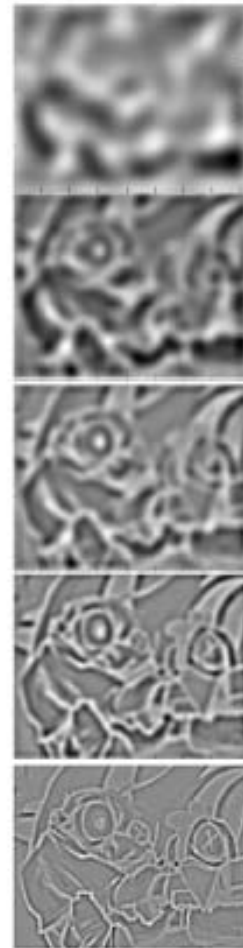
Laplacian-of-Gaussian (LoG)

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$$L_{xx}(\sigma) + L_{yy}(\sigma)$$

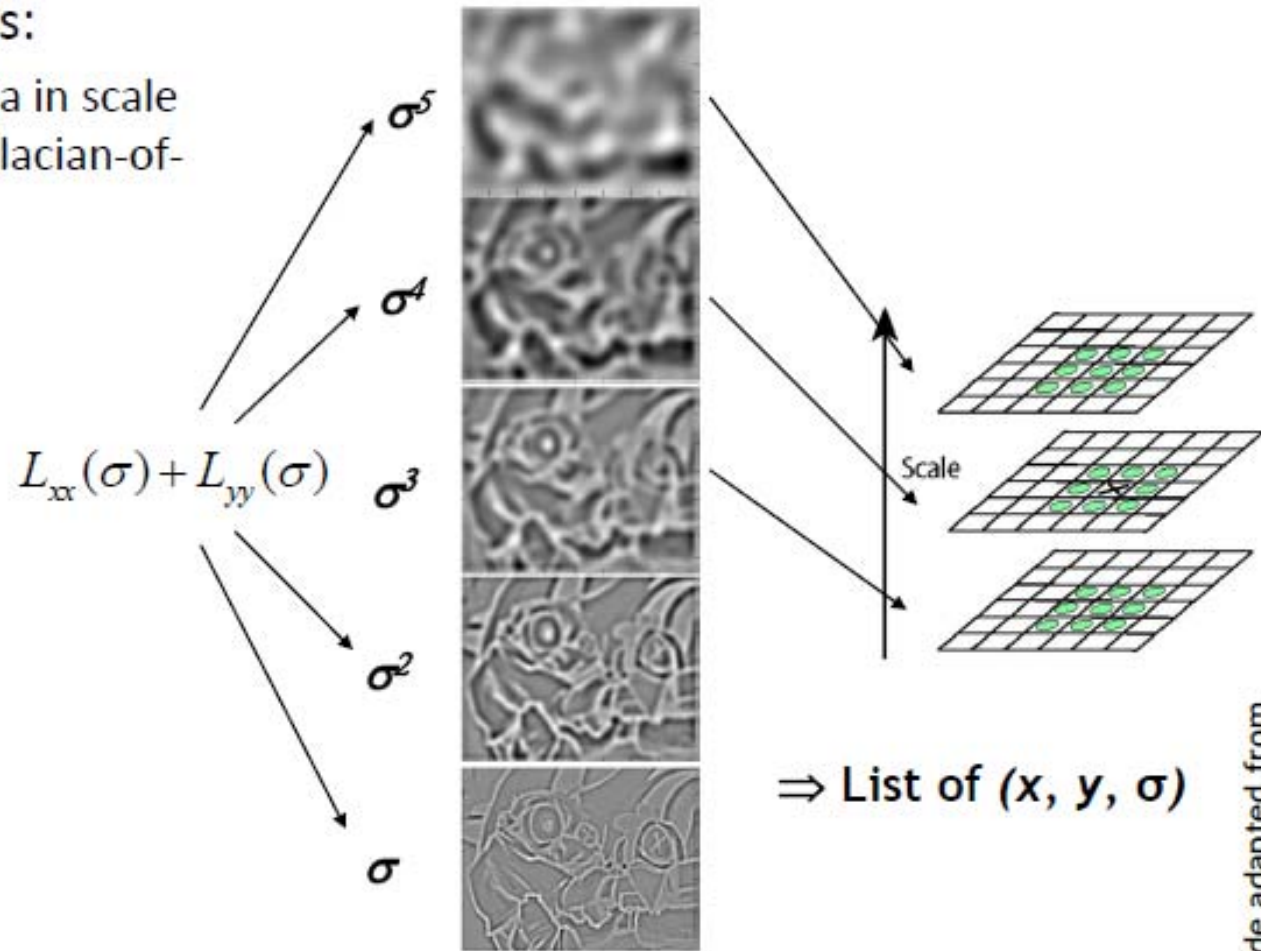
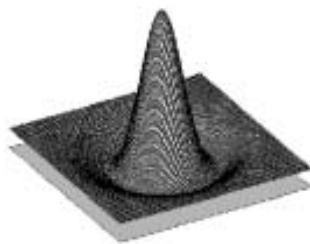
σ_5
 σ_4
 σ_3
 σ_2
 σ_1



Slide adapted from

Laplacian-of-Gaussian (LoG)

- Interest points:
 - Local maxima in scale space of Laplacian-of-Gaussian



Slide adapted from

LoG Detector: Workflow



Slide credit: Svetlana Lazebnik



LoG Detector: Workflow

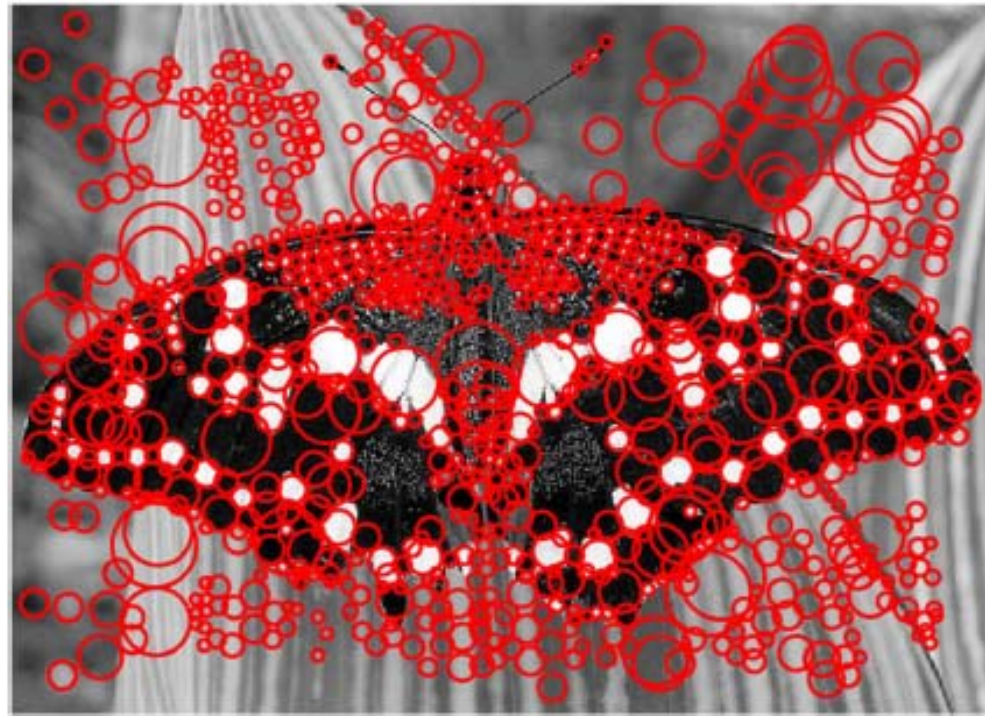


sigma = 11.9912

Slide credit: Svetlana Lazebnik



LoG Detector: Workflow



Slide credit: Svetlana Lazebnik

Technical Detail

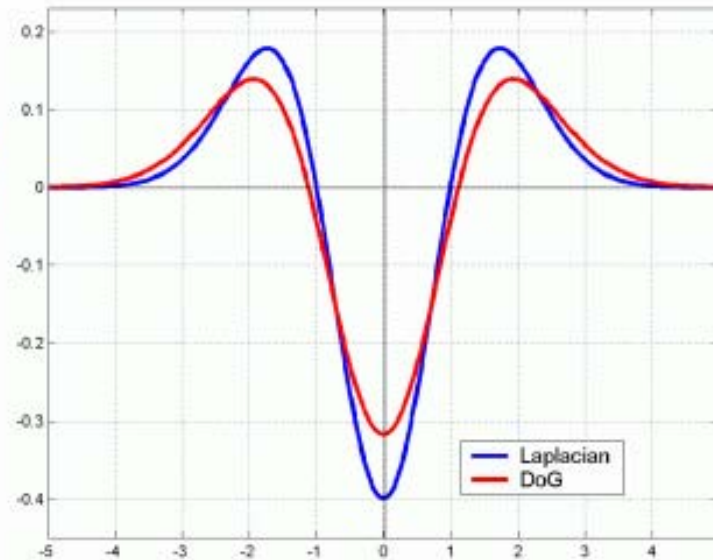
- We can efficiently approximate the Laplacian with a difference of Gaussians:

$$L = \sigma^2 \left(G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma) \right)$$

(Laplacian)

$$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$$

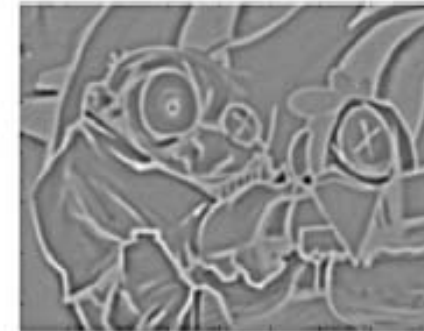
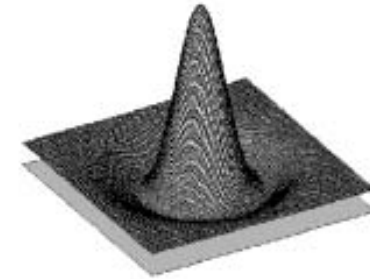
(Difference of Gaussians)



Slide credit: Bastian Leibe

Difference-of-Gaussian (DoG)

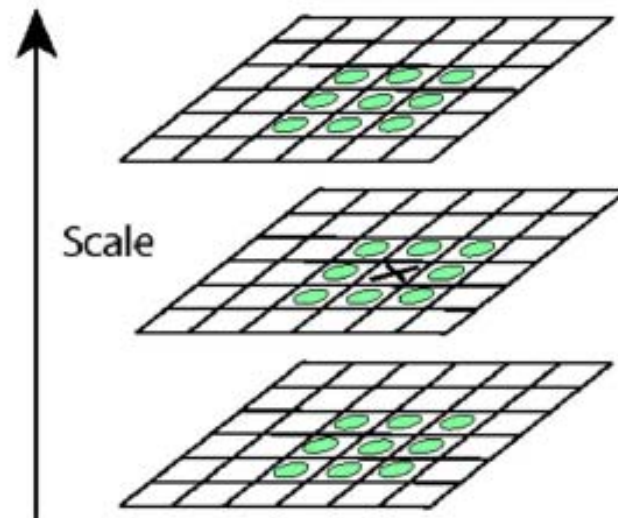
- Difference of Gaussians as approximation of the LoG
 - This is used e.g. in Lowe's SIFT pipeline for feature detection.
- Advantages
 - No need to compute 2nd derivatives
 - Gaussians are computed anyway, e.g. in a Gaussian pyramid.



Slide credit: Bastian Leibe

Key point localization with DoG

- Detect maxima of difference-of-Gaussian (DoG) in scale space
- Then reject points with low contrast (threshold)
- Eliminate edge responses

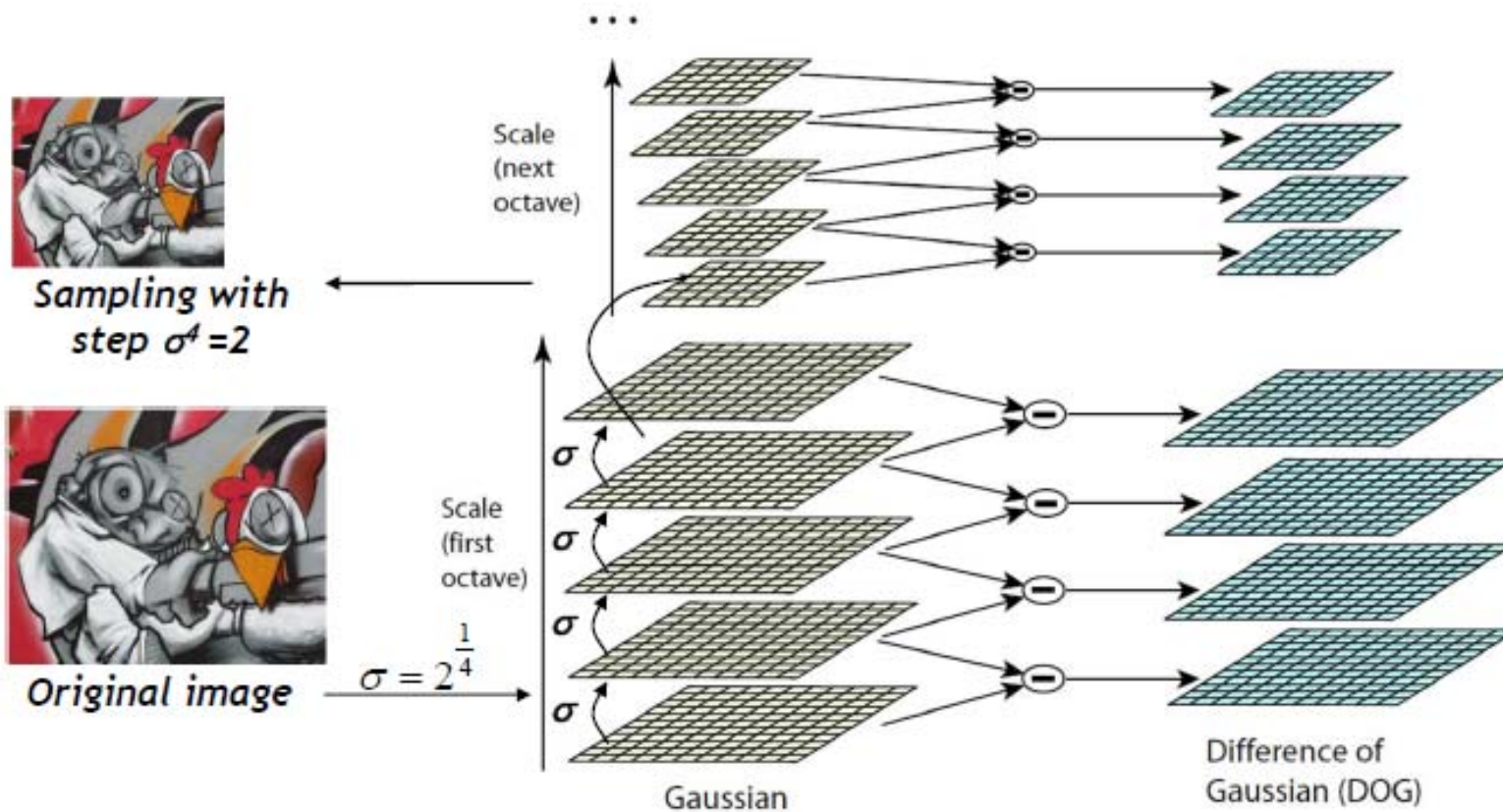


Candidate keypoints:
list of (x, y, σ)

Slide credit: David Lowe

DoG – Efficient Computation

- Computation in Gaussian scale pyramid



Slide adapted from Krystian Mikolajczyk



Results: Lowe's DoG



Slide credit: Bastian Leibe

Example of Keypoint Detection



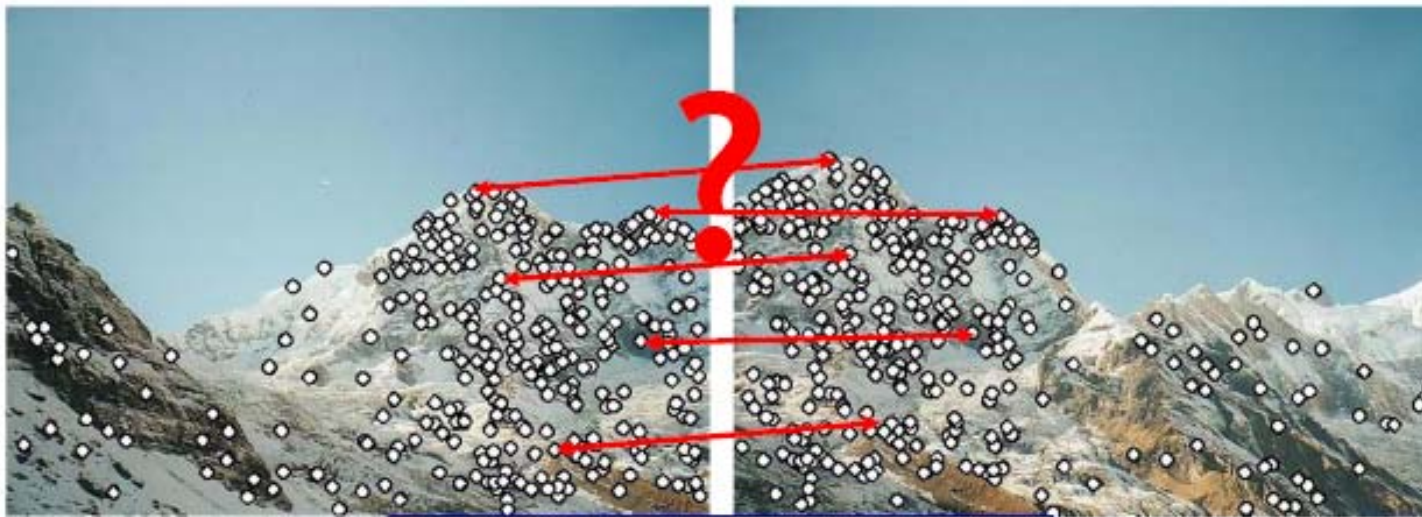
- (a) 233x189 image
- (b) 832 DoG extrema
- (c) 729 left after peak value threshold
- (d) 536 left after testing ratio of principle curvatures (removing edge responses)

Slide credit: David Lowe

Local Descriptors

- We know how to detect points
- Next question:

How to describe them for matching?



Point descriptor should be:

1. Invariant
2. Distinctive

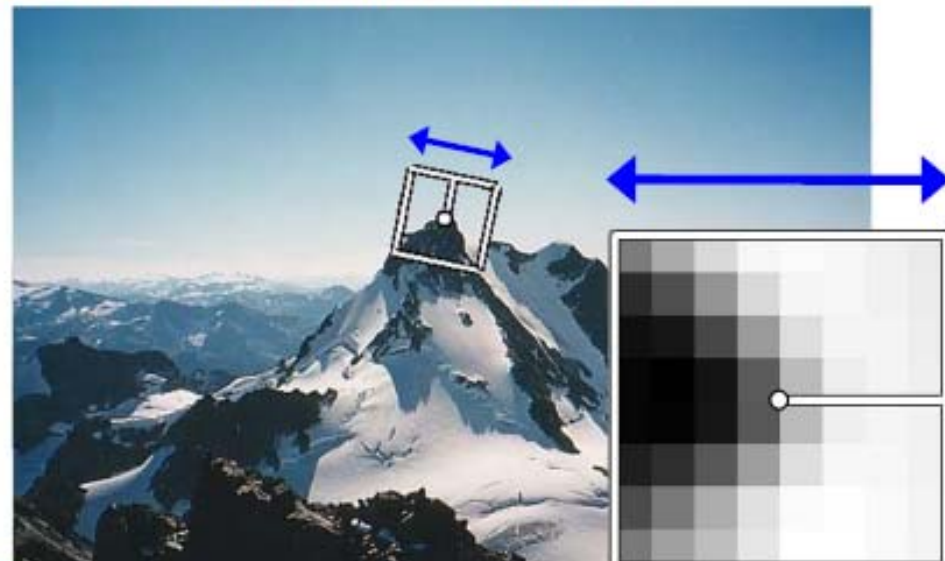
Slide credit: Kristen Grauman

Rotation Invariant Descriptors

- Find local orientation
 - Dominant direction of gradient for the image patch



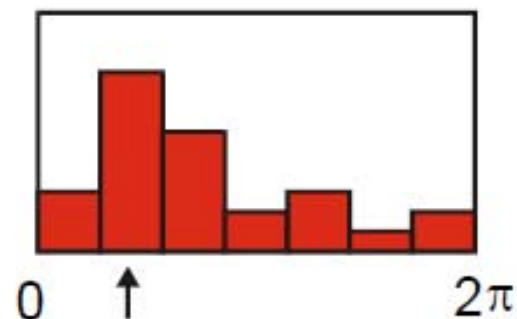
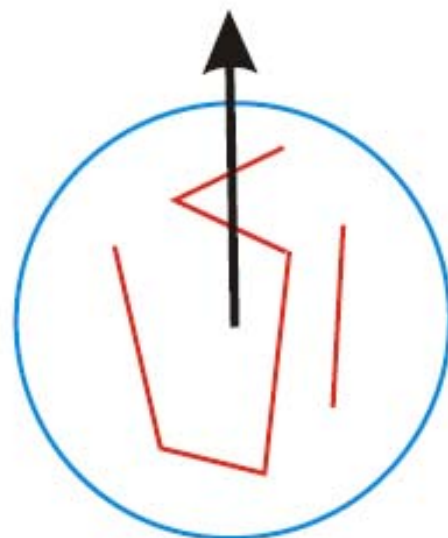
- Rotate patch according to this angle
 - This puts the patches into a canonical orientation.



Orientation Normalization: Computation

[Lowe, SIFT, 1999]

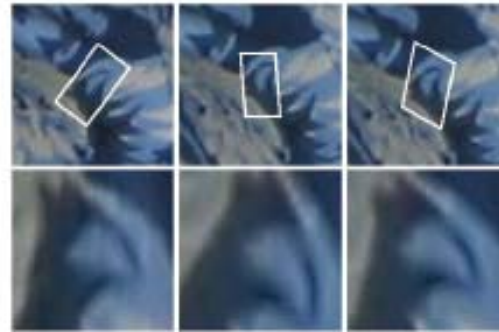
- Compute orientation histogram
- Select dominant orientation
- Normalize: rotate to fixed orientation



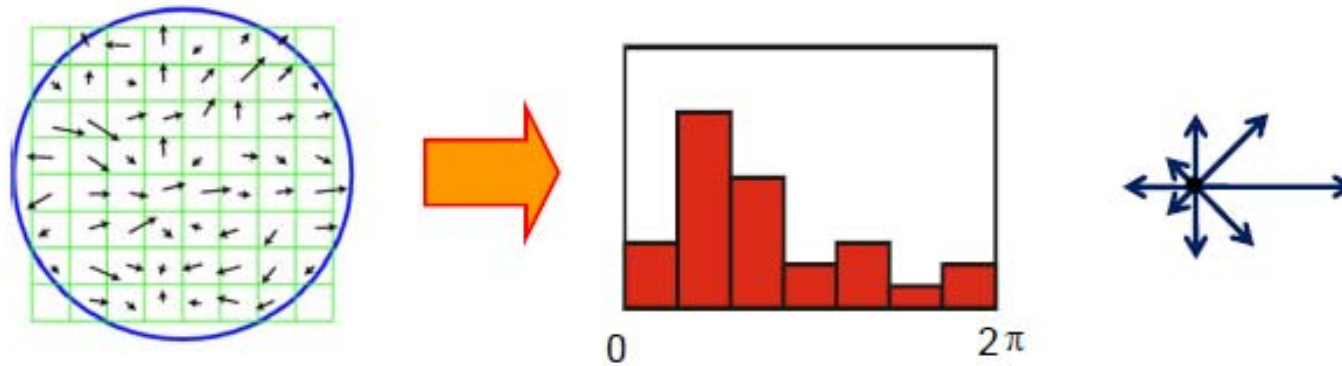
Slide adapted from David Lowe

Feature Descriptors

- Disadvantage of patches as descriptors:
 - Small shifts can affect matching score a lot

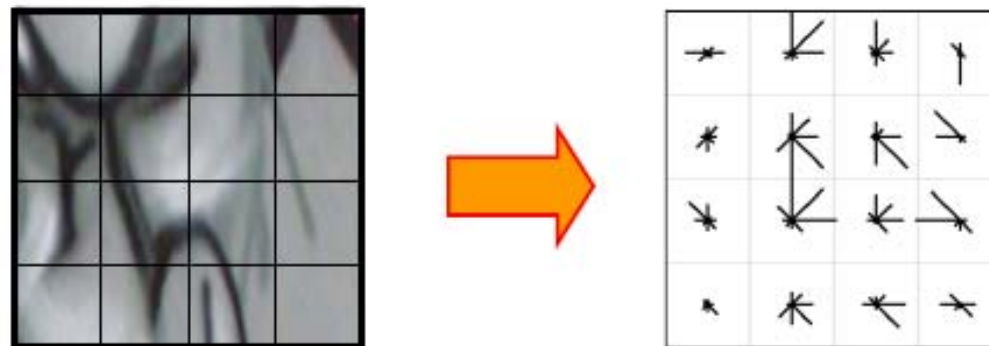


- Solution: histograms



Feature Descriptors: SIFT

- Scale Invariant Feature Transform
- Descriptor computation:
 - Divide patch into 4x4 sub-patches: 16 cells
 - Compute histogram of gradient orientations (8 reference angles) for all pixels inside each sub-patch
 - Resulting descriptor: $4 \times 4 \times 8 = 128$ dimensions



David G. Lowe. "[Distinctive image features from scale-invariant keypoints.](#)" *IJCV* 60 (2), pp. 91-110, 2004.

Overview: SIFT

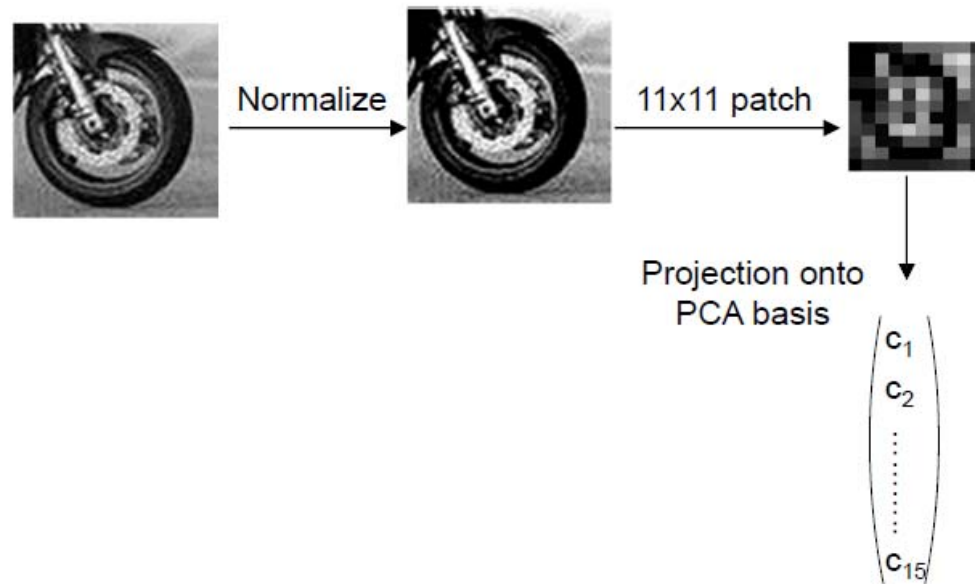
- Extraordinarily robust matching technique
 - Can handle changes in viewpoint up to ~ 60 deg. out-of-plane rotation
 - Can handle significant changes in illumination
 - Sometimes even day vs. night (below)
 - Fast and efficient—can run in real time
 - Lots of code available
 - http://people.csail.mit.edu/albert/ladypack/wiki/index.php/Known_implementations_of_SIFT



Slide credit: Steve Seitz

Other Descriptors

- Gray-scale intensity

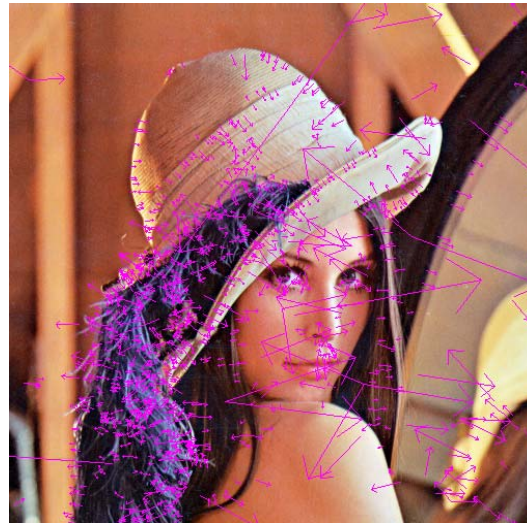


- GIST
- CNN features

PA1

- **Objective**

- **Understand how to extract SIFT features and to use related libraries**



- **Deadline**

- **Sep-29 (Thur.) (before 11:59pm)**

Class Objectives were:

- **Scale invariant region selection**
 - Automatic scale selection
 - Laplacian of Gradients (LoG) \approx Difference of Gradients (DoG)
 - SIFT as a local descriptor

Next Time...

- Object recognition
- Bag-of-Words (BoW) models

Homework for Every Class

- **Go over the next lecture slides**
- **Come up with one question on what we have discussed today**
 - 1 for typical questions (that were answered in the class)
 - 2 for questions with thoughts or that surprised me
- **Write questions at least 4 times**
 - Write a question about one out of every four classes
 - Multiple questions in one time will be counted as one time
- **Common questions are compiled at [the Q&A file](#)**
 - Some of questions will be discussed in the class
- **If you want to know the answer of your question, ask me or TA [on person](#)**