

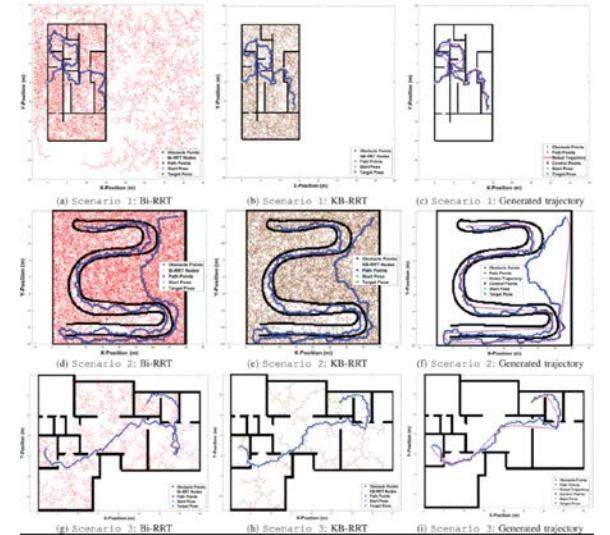
# Recap: Sampling based Kinodynamic Planning

CS686

Seungwook Lee, 11/12/2019

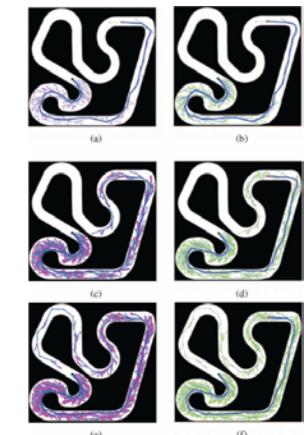
## ● Kinematic Constraints Based Bi-directional RRT: KB-RRT (ICRA 2019)

- For efficient computation are needed for real time operation of autonomous mobile robots
- Bidirectional-RRT(Bi-RRT) based path planning algorithms + kinodynamic constraints
- They proposed a kinematically constrained Bi-RRT (KB-RRT) algorithm
  - In order to restrict the number of nodes



## ● Sampling-based Algorithms for optimal motion planning using closed-loop prediction (ICRA 2017)

- Leverages ideas from the RRT# algorithm
- RRT# + closed-loop prediction = CL-RRT#



# Occupancy Mapping using two different methods

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CS686 Paper Presentation

20195487

Wonho Song  
송원호

2019. 11. 14.

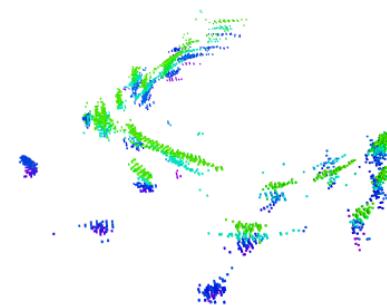
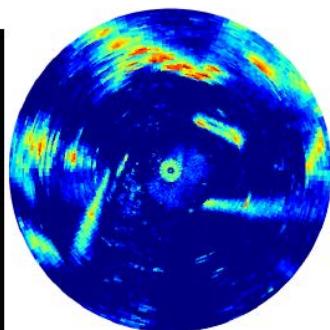
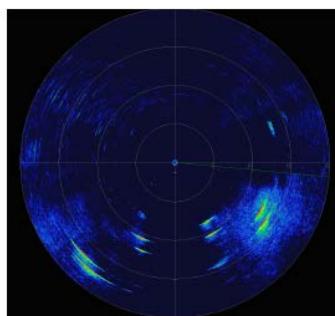


한국과학기술원  
Korea Advanced Institute of Science and Technology

## Motivation

- Applications of mobile robots warrant reliable planning and navigation, but sensors often give sparse and noisy readings. Additionally it should be real-time, taking place online

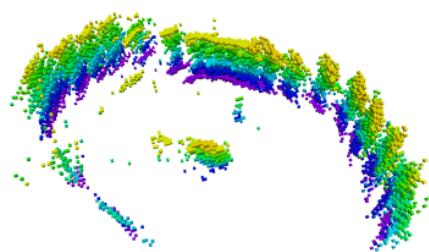
- Underwater navigation using sonar
  - Environmental disturbances
  - Low resolution
  - Multiple returns



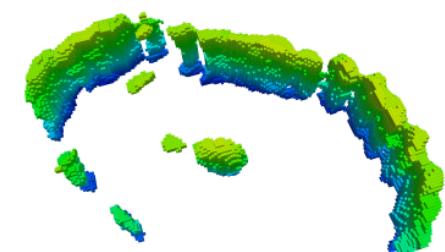
(a) Pier 84 OctoMap



(b) Pier 84 GP OctoMap



(a) USMMA OctoMap



(b) USMMA GP OctoMap

- Traditional occupancy grid mapping is limited by strong spatial independence assumptions

## Background

- Applications of mobile robots warrant reliable planning and navigation, but sensors often give sparse and noisy readings. Additionally it should be real-time, taking place online

- We can derive the recursive update as follows:

$$p(m_i|z_{1:t}, x_{1:t}) = \frac{p(z_t|m_i, z_{1:t-1}, x_{1:t})p(m_i|z_{1:t-1}, x_{1:t})}{p(z_t|z_{1:t-1}, x_{1:t})}$$

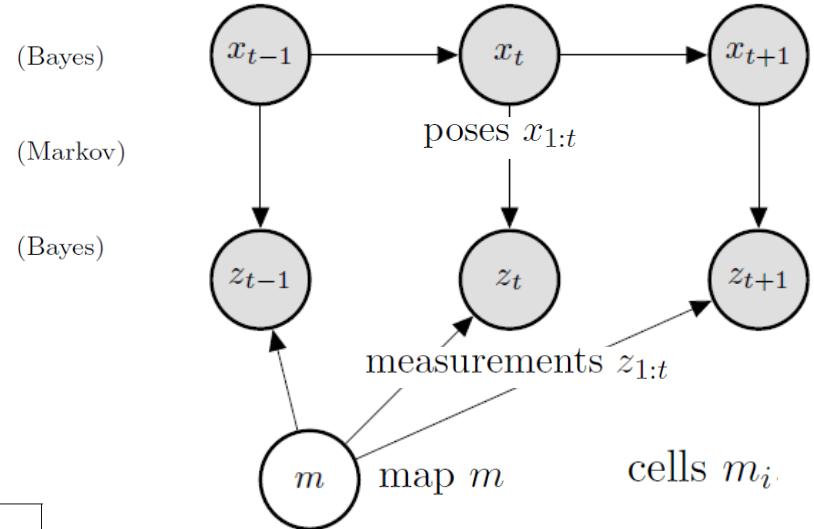
$$= \frac{p(z_t|m_i, x_t)p(m_i|z_{1:t-1}, x_{1:t-1})}{p(z_t|z_{1:t-1}, x_{1:t})}$$

$$= \frac{p(m_i|z_t, x_t)p(z_t|x_t)p(m_i|z_{1:t-1}, x_{1:t-1})}{p(m_i)p(z_t|z_{1:t-1}, x_{1:t})}$$

$$p(\neg m_i|z_{1:t}, x_{1:t}) = \frac{p(\neg m_i|z_t, x_t)p(z_t|x_t)p(\neg m_i|z_{1:t-1}, x_{1:t-1})}{p(\neg m_i)p(z_t|z_{1:t-1}, x_{1:t})}$$

$$\frac{p(m_i|z_{1:t}, x_{1:t})}{p(\neg m_i|z_{1:t}, x_{1:t})} = \frac{p(m_i|z_t, x_t)}{p(\neg m_i|z_t, x_t)} \frac{p(m_i|z_{1:t-1}, x_{1:t-1})}{p(\neg m_i|z_{1:t-1}, x_{1:t-1})} \frac{p(\neg m_i)}{p(m_i)}$$

$$\log \frac{p(m_i|z_t, x_t)}{1 - p(m_i|z_t, x_t)} + \log \frac{p(m_i|z_{1:t-1}, x_{1:t-1})}{1 - p(m_i|z_{1:t-1}, x_{1:t-1})} - \log \frac{p(m_i)}{1 - p(m_i)} \\ = l_{t,i} + l_{1:t-1,i} - l_0$$



- Why not just use Gaussian process occupancy maps?
  - Prediction requires inversion of a matrix the size of the training data; in O(N^3)
  - Too slow for real-time mapping scenarios

## Background

- **Paper 1 : Overlapping Hilbert Maps**

- K. Doherty, J. Wang, and B. Englot, "Probabilistic map fusion for fast, incremental occupancy mapping with 3D Hilbert maps," Proceedings of the IEEE International Conference on Robotics and Automation, pp. 1011-1018, 2016.

- **Paper 2: Gaussian Process Occupancy Maps**

- J. Wang and B. Englot, "Fast, accurate Gaussian process occupancy maps via test-data octrees and nested Bayesian fusion," Proceedings of the IEEE International Conference on Robotics and Automation, pp. 1003-1010, 2016.

## [Paper 1] Historically

- Original Hilbert Maps

- Need some modifications on parameters

- ▶ Nonlinear logistic regression

$$p(y_* = 1|x_*, x, w) = \frac{1}{1 + \exp(w^T k(x_*, x))}$$

- ▶ Approximate radial basis function kernel (Nyström method)

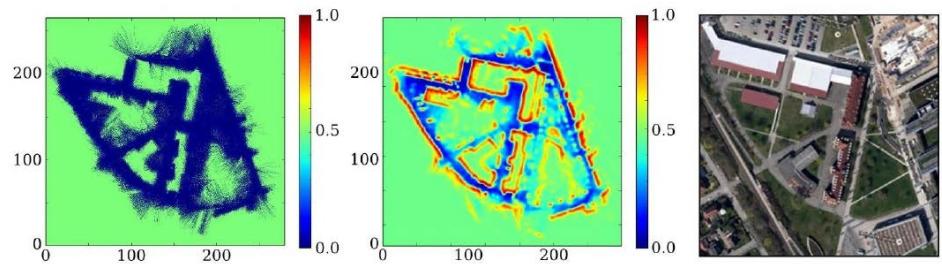
$$k(x, x') = \exp(-\gamma \|x - x'\|^2)$$

$$\phi_{\text{Nyström}}(x) = D^{-1/2} V^T (k(x, \hat{x}_1), \dots, k(x, \hat{x}_m))$$

- ▶ Train iteratively with stochastic gradient descent: minimize

$$E(w, b) = \frac{1}{n} \sum_{i=1}^n L(y_i, f(x_i)) + \alpha \|w\|_1$$

$$L(y_i, f(x_i)) = \log(\exp(-y_i(x_i^T w + b)) + 1)$$



Pros:

- ▶ Faster than GPOM (Linear time complexity, but big coefficient attached)
- ▶ Comparable accuracy

Cons:

- ▶ No uncertainty estimates
- ▶ Still intractable for real-time 3D mapping

# Overlapping Hilbert Maps (ICRA 2016)

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## [Paper 1] Overall plan

- Overall plan

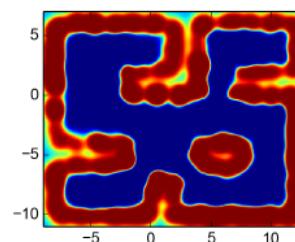
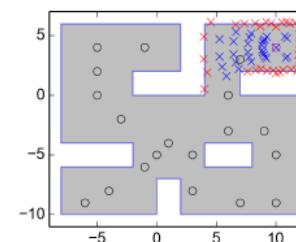
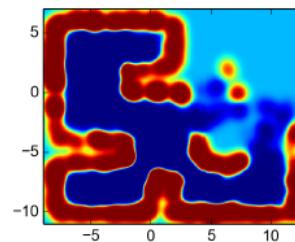
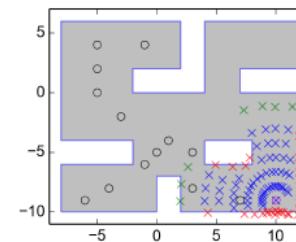
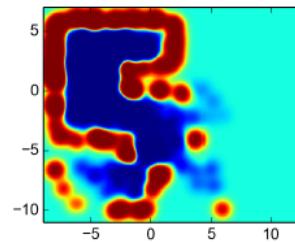
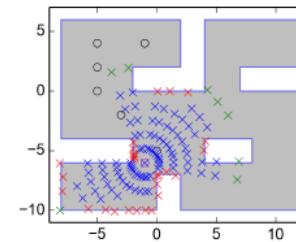
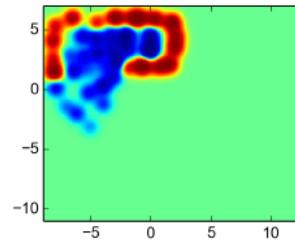
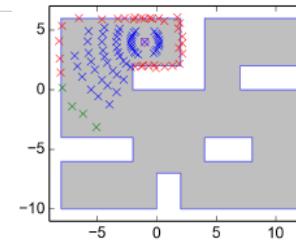
Probabilistic Local Map Fusion



Combining Logistic Regression Classifiers



Computational Results



[Paper 1] Step 1

## Probabilistic Local Map Fusion

- ▶ Assume discretized grid map  $m_i \in \mathcal{M}$
- ▶ Estimate the probability of occupancy of map cell  $m_i$  given the data by combining logistic regression outputs  $p(m_i|\mathcal{D}_{1:t})$

$$p(m_i|\mathcal{D}_{1:t}) = \left[ 1 + \frac{1 - p(m_i|\mathcal{D}_{1:t-1})}{p(m_i|\mathcal{D}_{1:t-1})} \frac{1 - p(m_i|\mathcal{D}_t)}{p(m_i|\mathcal{D}_t)} \frac{p(m_i)}{1 - p(m_i)} \right]^{-1}$$

- ▶ Doesn't this assume grid cell independence?
- ▶ Spatial dependence accounted for by logistic regression classifier
- ▶ We don't *need* to discretize this; treat the logistic regression as spatial interpolation, combine predictions at query time

[Paper 1] Step 2

## Combining Logistic Regression Classifiers

$$p(m_i|\mathcal{D}_1) = \frac{1}{1 + \exp(w_1^T k(X_1, x_*))}$$

$$p(\neg m_i|\mathcal{D}_1) = 1 - p(m_i|\mathcal{D}) = \frac{\exp(w_1^T k(X_1, x_*))}{1 + \exp(w_1^T k(X_1, x_*))}$$

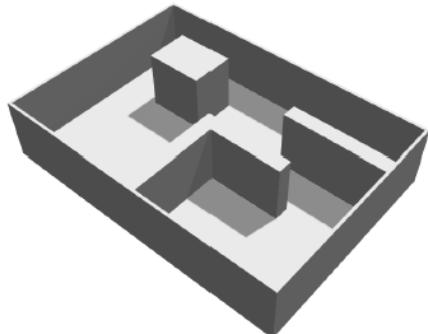
$$\begin{aligned} p(m_i|\mathcal{D}_{1:2}) &= \left[ 1 + \frac{1 - p(m_i|\mathcal{D}_1)}{p(m_i|\mathcal{D}_1)} \frac{1 - p(m_i|\mathcal{D}_2)}{p(m_i|\mathcal{D}_2)} \frac{p(m_i)}{1 - p(m_i)} \right]^{-1} \\ &= \left[ 1 + \exp(w_1^T k(X_1, x_*)) \exp(w_2^T k(X_2, x_*)) \right]^{-1} \\ &= \frac{1}{1 + \exp(w_{new}^T k(X_{new}, x_*))} \end{aligned}$$

where  $w_{new} = [w_1, w_2]$  and  $X_{new} = [X_1; X_2]$ .

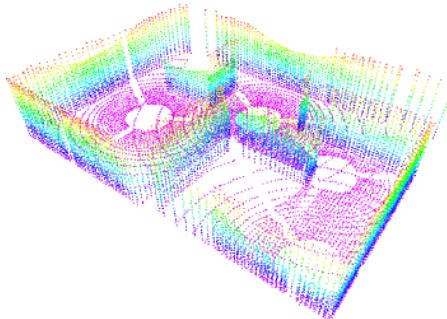
## [Paper 1] Result

### ● Computational Results

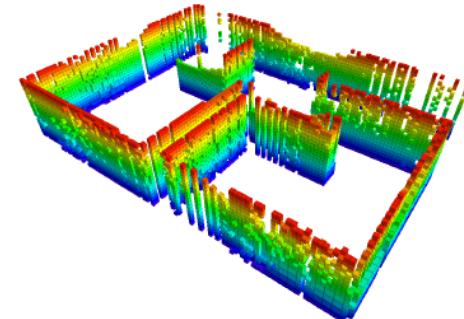
- Simulated datasets 1: "structured" in Gazebo



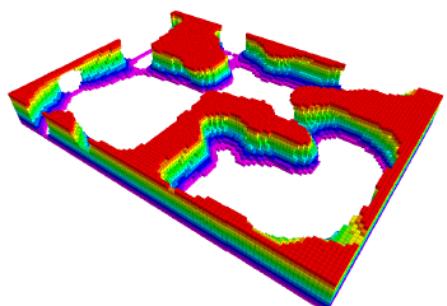
(a) The ground truth map



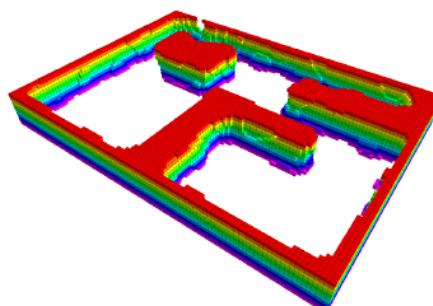
(b) The raw sensor data



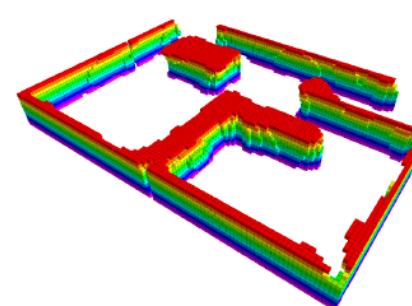
(c) The result of OctoMap



(d) The result of global Hilbert maps  
 $(m = 100)$



(e) The result of global Hilbert maps  
 $(m = 1000)$

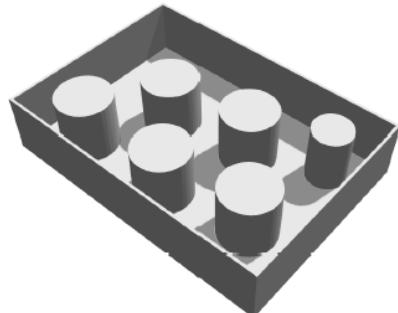


(f) The result after incrementally applying  
overlapping Hilbert maps

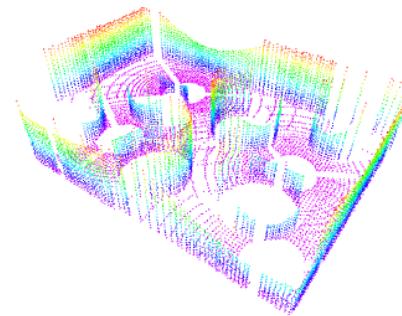
## [Paper 1] Result

### ● Computational Results

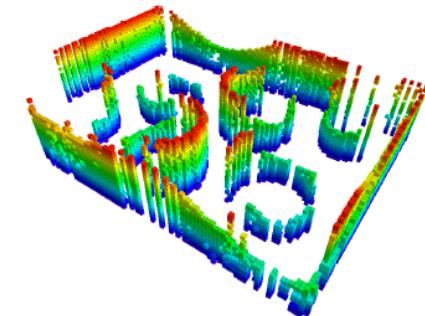
- Simulated datasets 2: "unstructured" in Gazebo



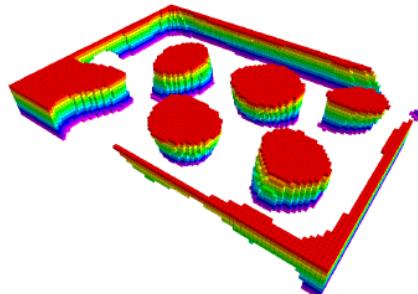
(a) The ground truth map



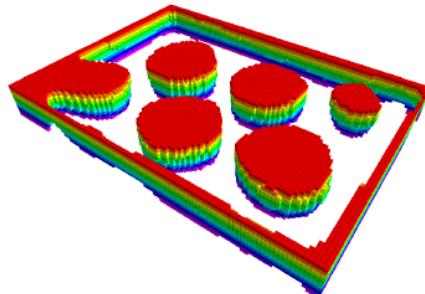
(b) The raw sensor data



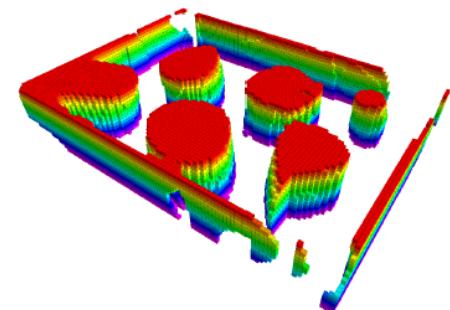
(c) The result of OctoMap



(d) The result of global Hilbert maps  
( $m = 100$ )



(e) The result of global Hilbert maps  
( $m = 1000$ )



(f) The result after incrementally applying  
overlapping Hilbert maps

# Overlapping Hilbert Maps (ICRA 2016)

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## [Paper 1] Result

### ● Computational Results

- Computation times for mapping the three environments examined

Dataset	Scans	Points/Scan	Test Points/Scan	Method	Time/Scan (s)	Time (s)
Structured Simulation	12	3500	29892	Overlapping Hilbert Maps	1.89	22.68
				Global Hilbert Map ( $m = 100$ )	N/A	8.70
				Global Hilbert Map ( $m = 1000$ )	N/A	331.64
				OctoMap	0.02	0.2
Unstructured Simulation	12	3500	29892	Overlapping Hilbert Maps	1.83	21.96
				Global Hilbert Map ( $m = 100$ )	N/A	8.52
				Global Hilbert Map ( $m = 1000$ )	N/A	332.82
				OctoMap	0.01	0.14
Freiburg Corridor FR-079	66	4943	371170	Overlapping Hilbert Maps	14.6	963.6
				Global Hilbert Map ( $m = 100$ )	N/A	1656.95
				Global Hilbert Map ( $m = 1000$ )	N/A	11914.96
				OctoMap	0.1	6.7

## [Paper 1] Conclusion & future work

- Conclusion

- Local approximation to Hilbert maps
- Combine predictions from multiple classifiers
- Faster, but not quite there (!!)
  - Implemented pretty naively in Python

- What next?

- How can we do this in real-time?

# Gaussian Process Occupancy Maps (ICRA 2016) CS686

## [Paper 2] Overall plan

- Overall plan

SPATIAL PARTITIONING WITH TEST-DATA OCTREES



NESTED UPDATES WITH BCMS



Computational Results

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**Algorithm 1** GPOctoMap-NBCM-P

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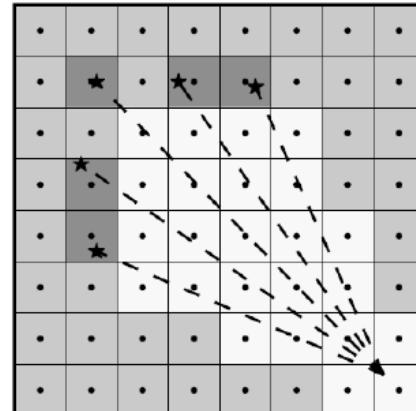
```
1:  $\mathcal{M} \leftarrow \{\mathcal{B}_i = \emptyset\}, i = 1, \dots, K;$ 
2:  $\mathcal{G} \leftarrow \{g_i = \emptyset\}, i = 1, \dots, K;$ 
3: while !MappingComplete do
4:    $\mathcal{Z}_n \leftarrow SensorHits();$ 
5:    $\mathcal{M}_n \leftarrow \emptyset;$  # local blocks need to be updated
6:   for  $\mathcal{B}_i \in \mathcal{M}$  do
7:     if Intersect( $\mathcal{B}_i, \mathcal{Z}_n$ ) then
8:        $\mathcal{M}_n \leftarrow \mathcal{M}_n \cup \mathcal{B}_i$ 
9:     end if
10:   end for
11:   for  $\mathcal{B}_i \in \mathcal{M}_n$  do # training in blocks
12:     if IsEmptyOctree( $\mathcal{B}_i$ ) then
13:        $\mathcal{B}_i \leftarrow CreateOctreeInBlock(\mathcal{B}_i);$ 
14:     end if
15:      $X, y \leftarrow GetTrainingPoints(\mathcal{Z}_n);$ 
16:      $g_i \leftarrow GPRegression(X, y);$ 
17:   end for
18:   for  $\mathcal{B}_i \in \mathcal{M}_n$  do # BCM fusion in extended blocks
19:     for  $\mathcal{B}_e \in FindExtendedBlocks(\mathcal{B}_i)$  do
20:        $X_* \leftarrow GetOctreeLeafNodes(\mathcal{B}_e);$ 
21:        $f_*, var_* \leftarrow GPPredict(g_e, X_*);$ 
22:        $\mathcal{B}_i \leftarrow BCMUpdate(\mathcal{B}_e, f_*, var_*);$ 
23:     end for
24:   end for
25:   for  $\mathcal{B}_i \in \mathcal{M}_n$  do
26:     PruneNodes( $\mathcal{B}_i$ );
27:   end for
28: end while
29:  $OccupancyProbs \leftarrow \emptyset;$ 
30: for  $\mathcal{B}_i \in \mathcal{M}$  do
31:   if !IsEmptyOctree( $\mathcal{B}_i$ ) then
32:      $x_*, f_*, var \leftarrow GetOctreeLeafNodes(\mathcal{B}_i);$ 
33:      $\{x_*, p\} \leftarrow BinaryClassification(f_*, var_*);$ 
34:      $OccupancyProbs \leftarrow OccupancyProbs \cup \{x_*, p\};$ 
35:   end if
36: end for
37: return  $OccupancyProbs;$ 
```

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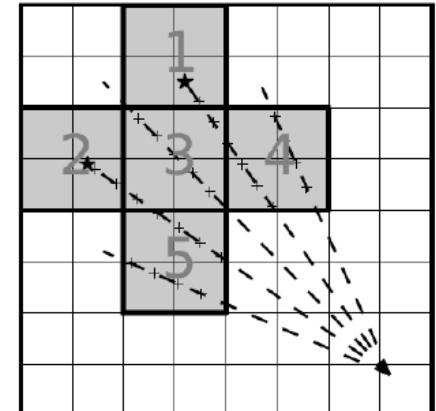
## [Paper 2] Contribution

- **Test-data Octrees**

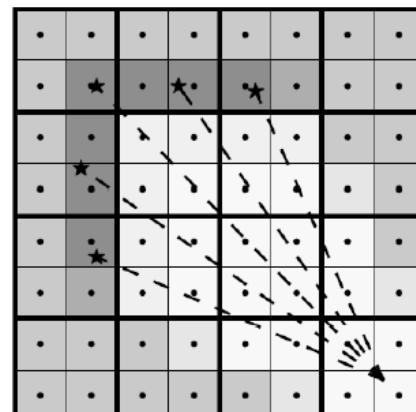
- Consider only points in "extended block"
- Quickly retrieve all relevant grid cells (and all relevant training data)
- Prune neighboring grid cells sharing the same state



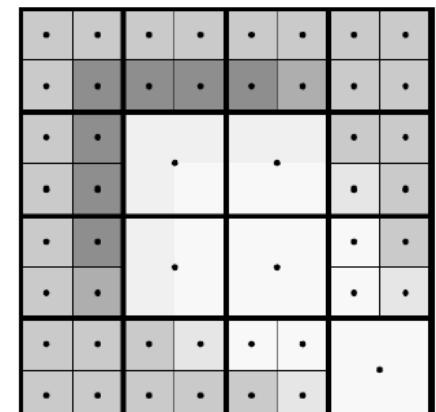
Standard occupancy grid mapping



predicting the occupancy probability



GP occupancy mapping with test-data octrees before pruning

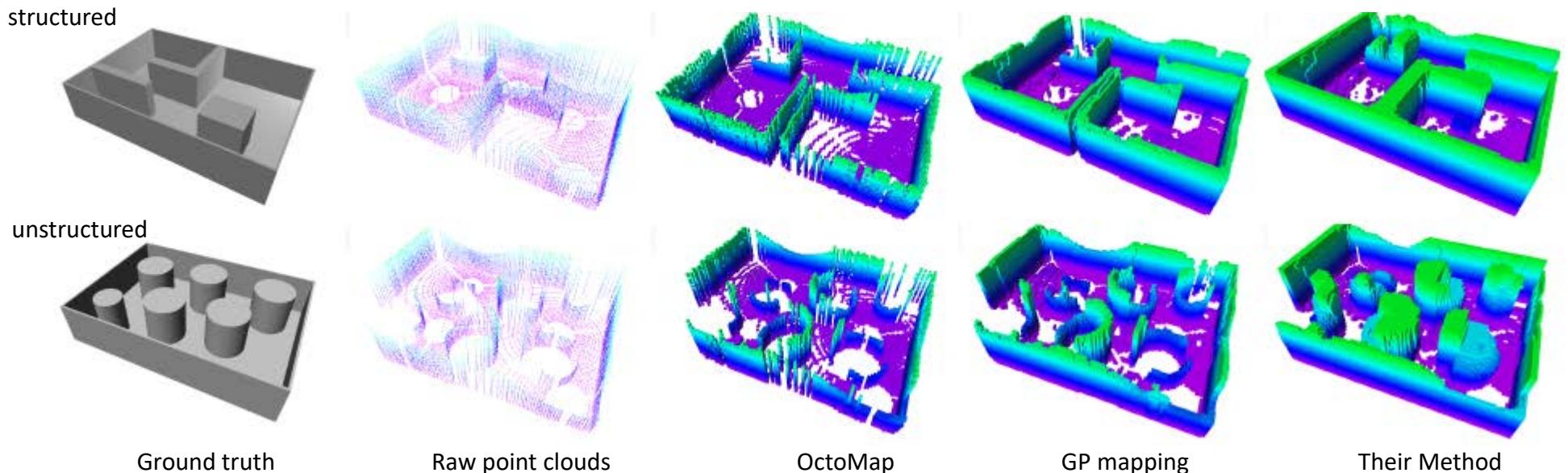


Final map after pruning

## [Paper 2] Result

### ● Computational Results

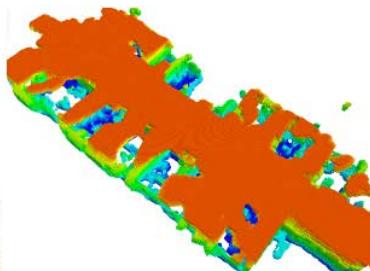
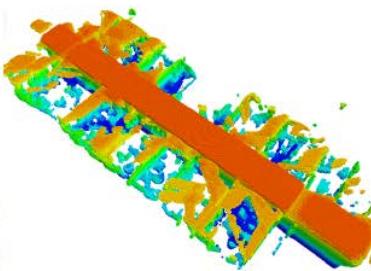
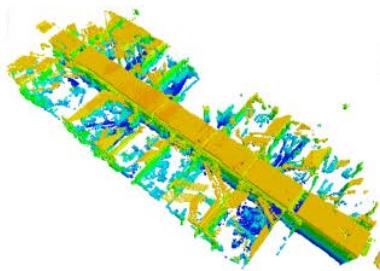
- Simulated datasets in Gazebo



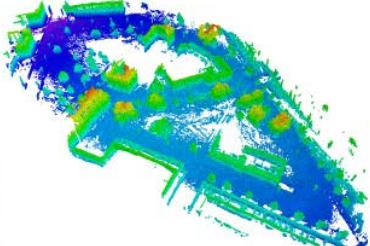
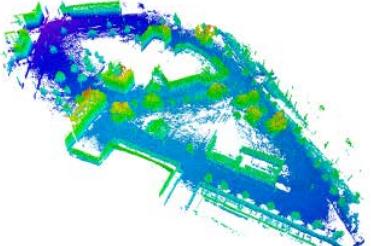
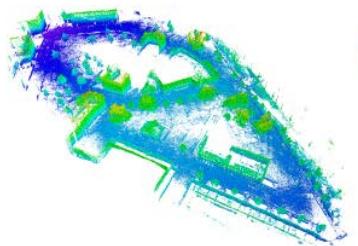
## [Paper 2] Result

### ● Computational Results

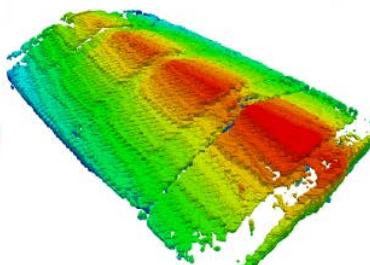
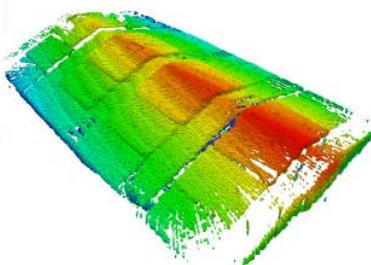
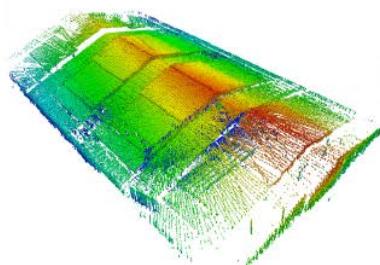
- Other datasets, 0.1m resolution



Freiburg-079 corridor dataset  
(43.7m x 182.0m x 3.3m)



Freiburg campus dataset  
(292m x 167m x 28m)



Spacebot Arena dataset  
(72.3m x 71.4m x 12.9m)

OctoMap

GP mapping

Their Method

## [Paper 2] Result

### ● Computational Results

- Computation times for mapping the four environments examined

Dataset	Size ( $m^3$ )	Scans	Points/Scan	Sampled Points/Scan	Method	Time (s)	Time/Scan (s)
Sim Structured Data	$10.0 \times 7.0 \times 2.0$	12	3500	1506	BCM-NP	6.57	0.55
					NBCM-P	0.44	0.04
					NBCM-P+	0.37	0.03
					OctoMap	0.20	0.02
FR-079	$43.8 \times 18.2 \times 3.3$	66	89445	7601	BCM-NP	724.10	10.97
					NBCM-P	10.96	0.17
					NBCM-P+	9.57	0.15
					OctoMap	6.71	0.10
FR Campus	$292.0 \times 167.0 \times 28.0$	81	247817	76009	BCM-NP	N/A	N/A
					NBCM-P	329.95	4.07
					NBCM-P+	294.62	3.64
					OctoMap	242.88	3.00
Spacebot Arena	$72.3 \times 71.4 \times 12.9$	8	296734	64950	BCM-NP	1189.42	148.68
					NBCM-P	33.06	4.13
					NBCM-P+	27.35	3.42
					OctoMap	33.65	4.21

## Summary

- **Paper 1 : Overlapping Hilbert Maps**

- Substantial time improvement over Hilbert maps
- Comparable accuracy to HM
- Still not real-time ready
- No uncertainty estimates

- **Paper 2: Bayesian Generalized Kernel Occupancy Maps**

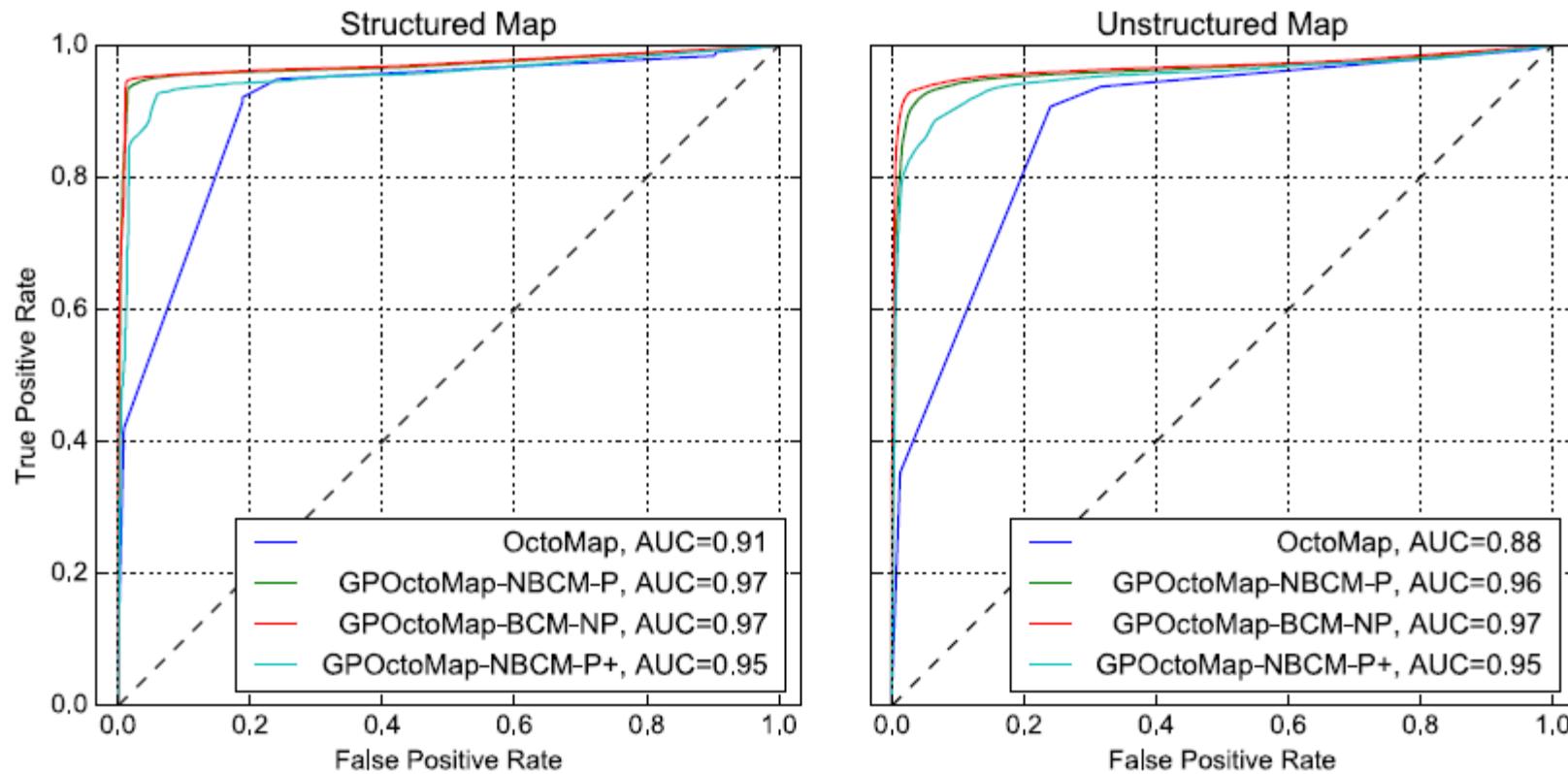
- Real-time viable
- Comparable accuracy to GPOM
- Provides uncertainty estimates
- BCM is unstable when mapping the same region

## Summary

- Applications of mobile robots warrant reliable planning and navigation, but sensors often give sparse and noisy readings. OctoMap can handle them. (T/F)
- Gaussian Process Occupancy Maps are available online. (T/F)

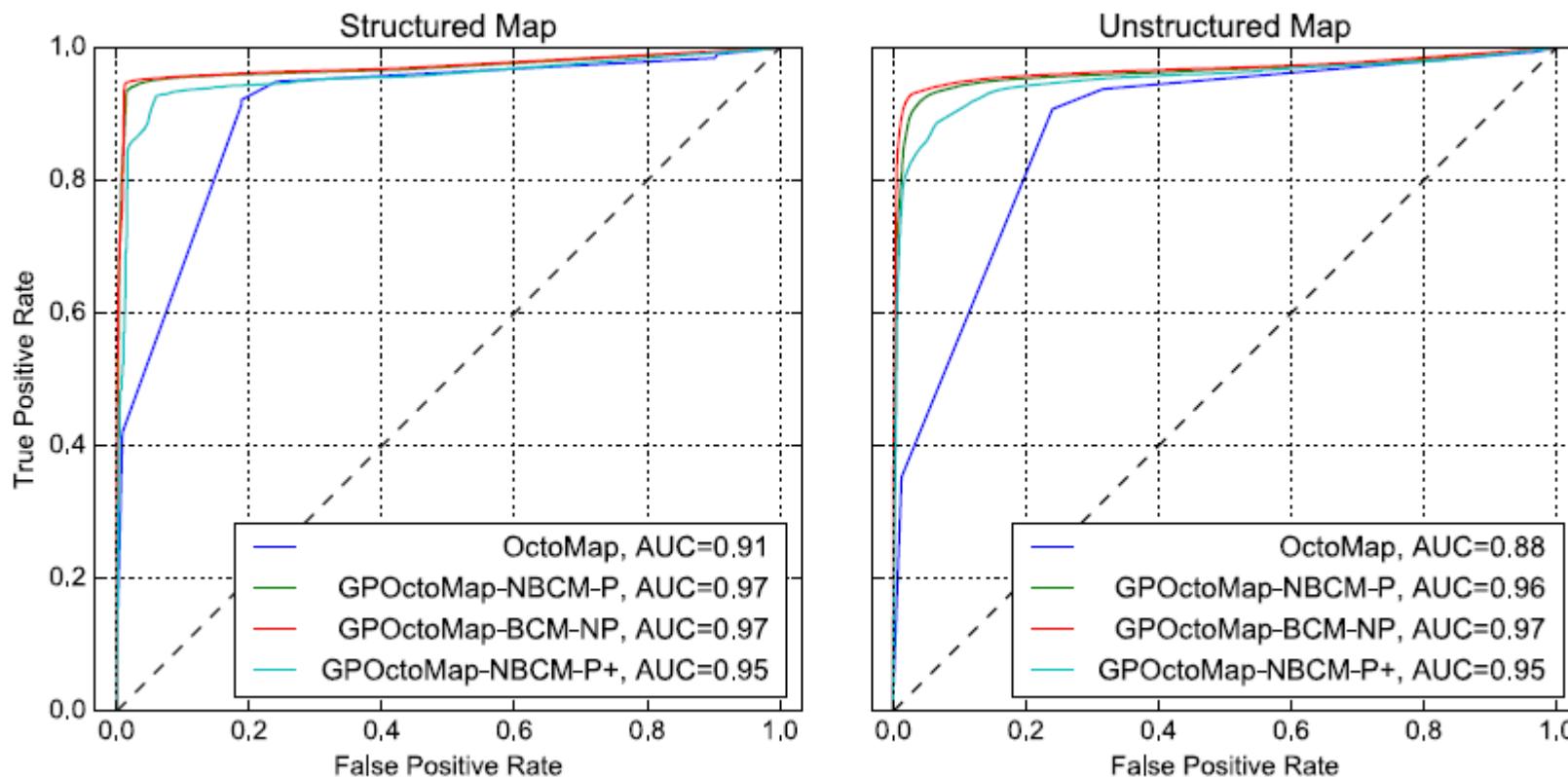
## [Paper 2] Result

- Computational Results



## [Paper 2] Result

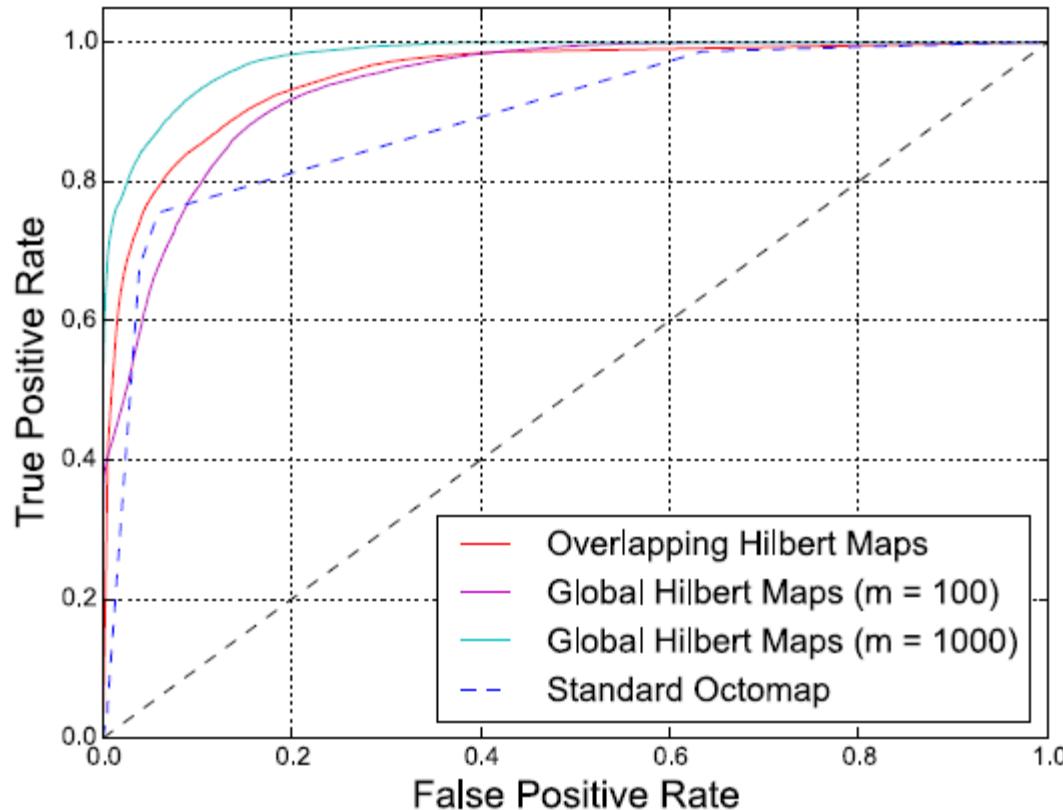
- Computational Results



## [Paper 1] Result

- Result graph

- Computation



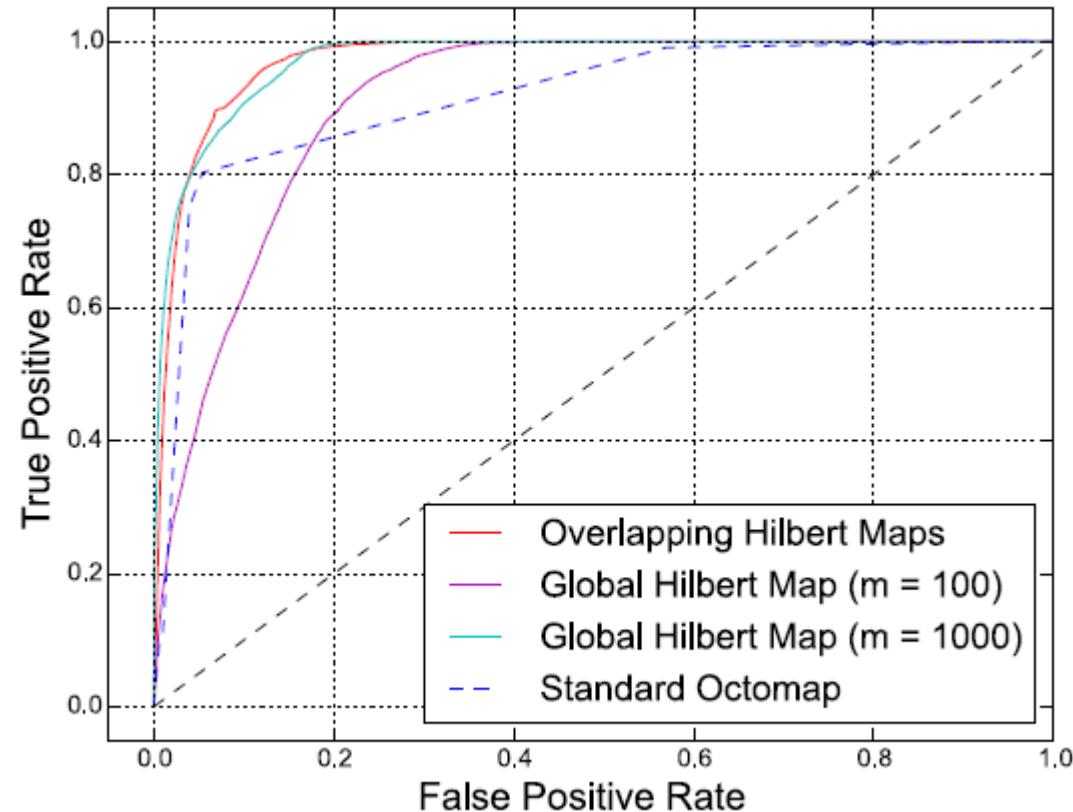
## [Paper 1] Result

### ● Result graph

- Computation

Method	AUC	Precision	Recall
OctoMap	0.92	0.320	0.097
Global Hilbert Map ( $m = 100$ )	0.91	0.792	0.108
Global Hilbert Map ( $m = 1000$ )	0.97	0.661	0.877
Overlapping Hilbert Maps	0.97	0.709	0.868

Method	AUC	Precision	Recall
OctoMap	0.89	0.418	0.042
Global Hilbert Map ( $m = 100$ )	0.94	0.999	0.248
Global Hilbert Map ( $m = 1000$ )	0.98	0.990	0.629
Overlapping Hilbert Maps	0.95	0.797	0.832



## [Paper 1] Result

- **Result**

- Computation

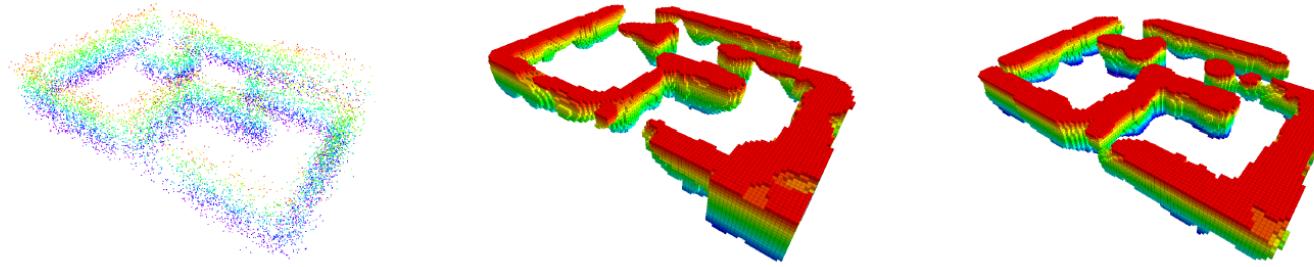


Fig. 8: Incrementally mapping the “structured” environment from Figure 2 when the range sensor is corrupted by noise. The first image (left) shows the raw sensor data. The second (center) shows the map produced using the Nyström method, as before. The rightmost image shows the same map produced using overlapping Hilbert maps with RKHS.