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# 로봇경로생성 기술 및 응용

## Robot Motion Planning and Applications

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Associate Professor

KAIST

<http://sglab.kaist.ac.kr>

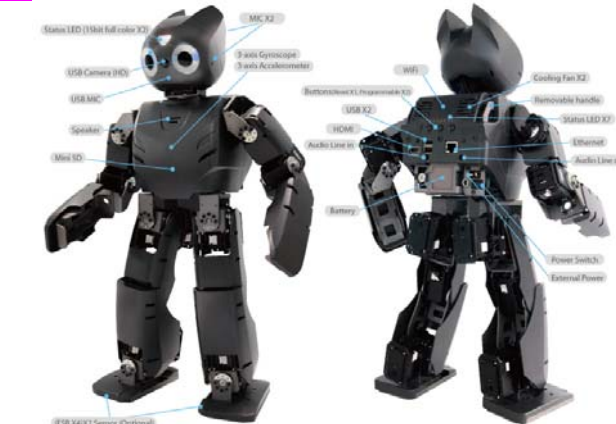
**KAIST**



# Real World Robots



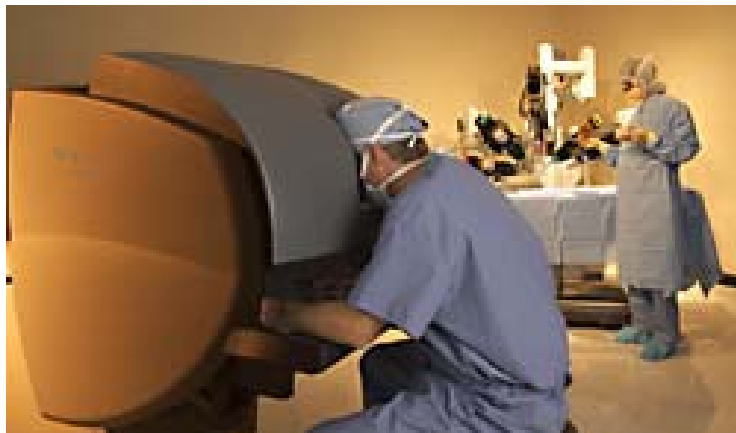
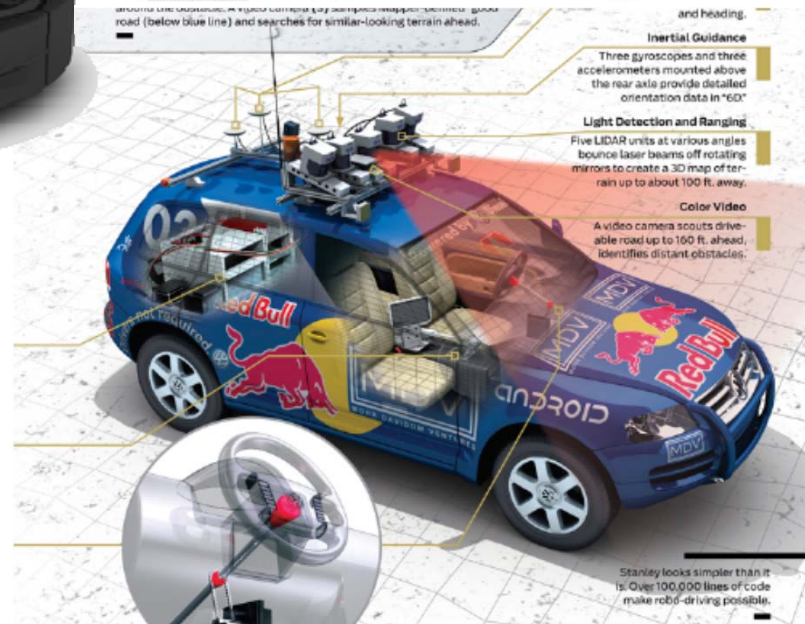
ASIMO



and heading. Inertial Guidance Three gyroscopes and three accelerometers mounted above the rear axle provide detailed orientation data in "6D".

Light Detection and Ranging Five LIDAR units at various angles bounce laser beams off rotating mirrors to create a 3D map of terrain up to about 100 ft. away.

Color Video A video camera scouts drivable road up to 160 ft. ahead, identifies distant obstacles.



Da Vinci

# Autonomous Robots

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- **Autonomous robots** that sense, plan, and act in real and/or virtual worlds
- Algorithms and systems for representing, capturing, planning, controlling, and rendering **motions of physical objects**
- **Applications:**
  - Manufacturing
  - Mobile robots
  - Computational biology
  - Computer-assisted surgery
  - Digital actors

# Goal of Motion Planning

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- Compute **motion strategies**, e.g.:
  - Geometric paths
  - Time-parameterized trajectories
  - Sequence of sensor-based motion commands
  - Aesthetic constraints
- Achieve **high-level goals**, e.g.:
  - Go to A without colliding with obstacles
  - Assemble product P
  - Build map of environment E
  - Find object O

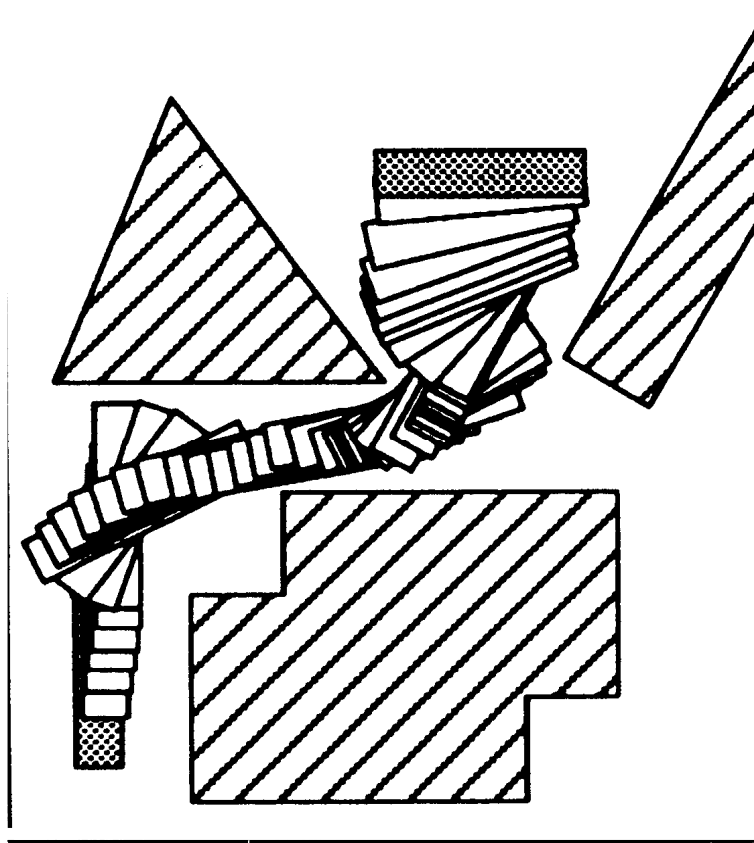
# Basic Motion Planning Problem

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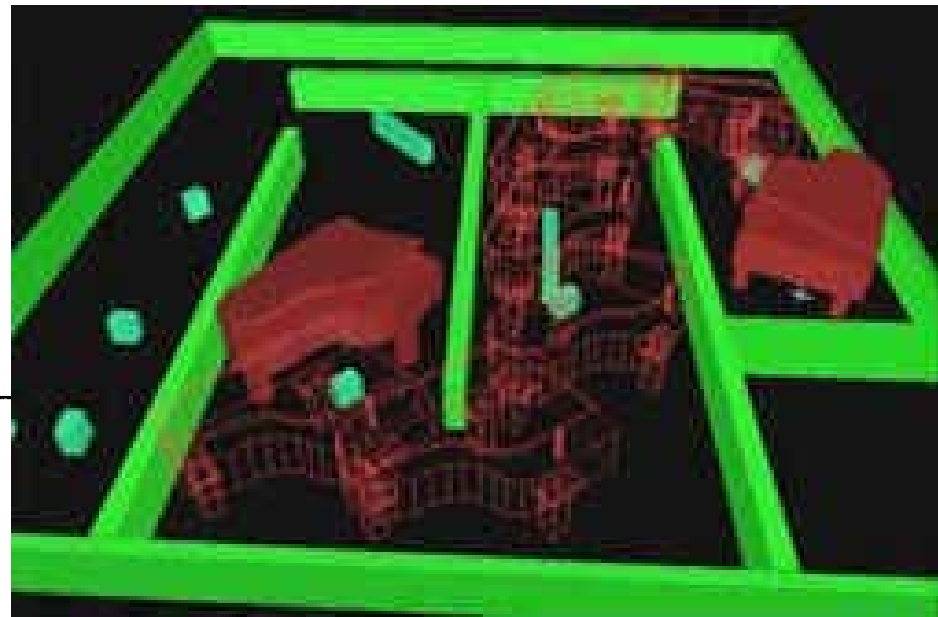
- **Statement:**
  - Compute a collision-free path for an object (the robot) among obstacles subject to CONSTRAINTS
- **Inputs:**
  - Geometry of robot and obstacles
  - Kinematics of robot (degrees of freedom)
  - Initial and goal robot configurations (placements)
- **Outputs:**
  - Continuous sequence of collision-free robot configurations connecting the initial and goal configurations

# Examples with Rigid Object

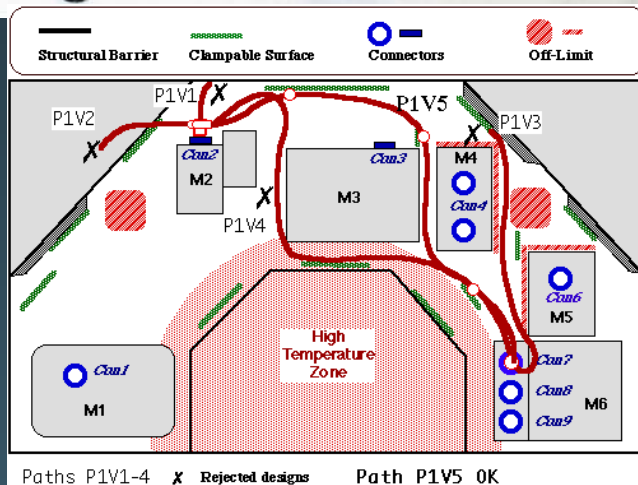


Piano-mover problem ←

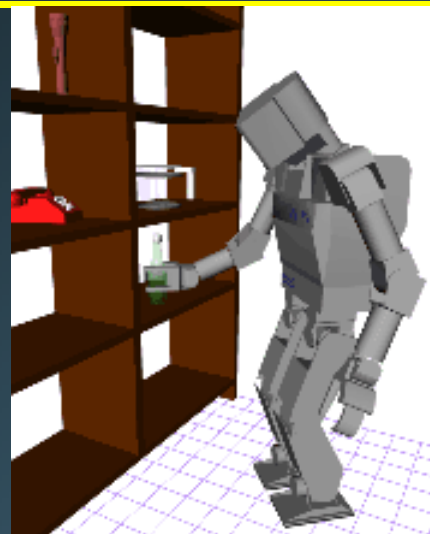
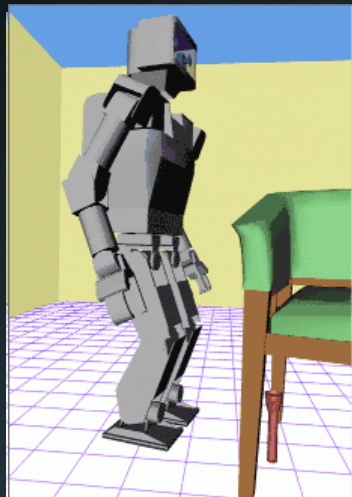
→ Ladder problem



# Cable Harness/ Pipe design



# Humanoid Robot



[Kuffner and Inoue, 2000] (U. Tokyo)





# DARPA Grand Challenge

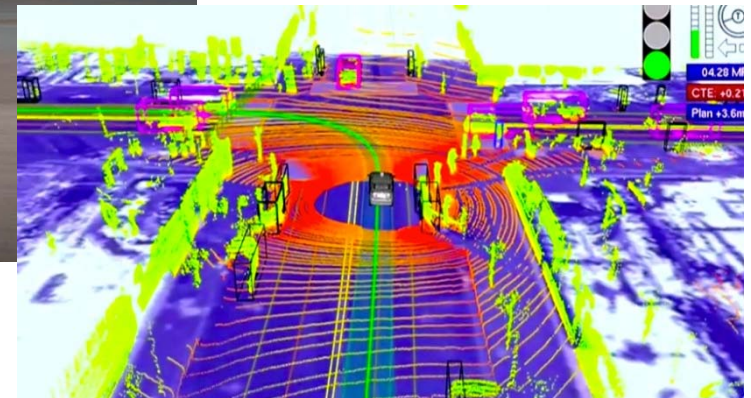


**Planning for a collision-free 132 mile path  
in a desert**

# Google Self-Driving Vehicles

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# Car is the next IT platform

WeeklyBiz ▾ [Weekly BIZ] 실리콘밸리는 '자동차 밸리'... 세계 1~8위 車 회사 모두 몰렸다  
 플로렌도셀몬트(캘리포니아)-최원석 기자 ws ▾

기사 100자평(0)

입력 : 2013.08.31 03:05

왜 실리콘밸리로 가나  
 자동차는 갈수록 전자제품화, 첨단 소프트웨어 기술 확보 필요

리브콜 받는 한국 모바일 부품 업체  
 스마트폰과 연결 시키는 작업 중 실력 뛰어난 한국 업체와 연구 돌입



중고차 아울렛

인 판매전, 중고차 아울렛

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▲ 구글-에를 등 실리콘밸리의 터넷대강 IT 업체들 사이로 자동차회사 연구소들이 속속 모여들고 있다. ①스탠퍼드대가 있는 플로렌도에 위치한 GM 연구소 ②셀몬트의 볼크스바겐 연구소 ③레드우드시에 있는 전기차 업체 테슬라의 전시장 ④실리콘밸리를 남북으로 관통하는 101 고속도로 위를 달리고 있는 구글 무인주행차 /실리콘밸리=최원석 기자

# Overview of This Tutorial

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- **4:30pm: Optimal path planning and its applications**
  - 윤성익, 전산과, KAIST
- **5:10pm: Data-driven planning for multi-contact poses of human avatars**
  - 이성희, CT, KAIST
- **5:40pm: High performance geometric computation for robot motion planning**
  - 김영준, 컴퓨터공학과, 이대
- **6:10pm: Path Planning and Execution for Real Worlds**
  - 심현철 (이웅희), 항공우주, KAIST

# Motion Planning Techniques

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- **Classical techniques**
  - Roadmap, cell decomposition, potential fields
- **Silhouette**
  - First complete general method that applies to spaces of any dimension and is singly exponential in # of dimensions [Canny, 87]
  - Slow

# Motion Planning Techniques

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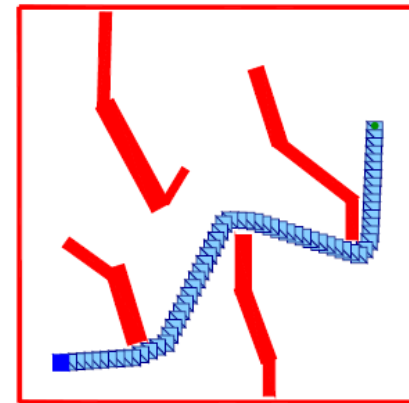
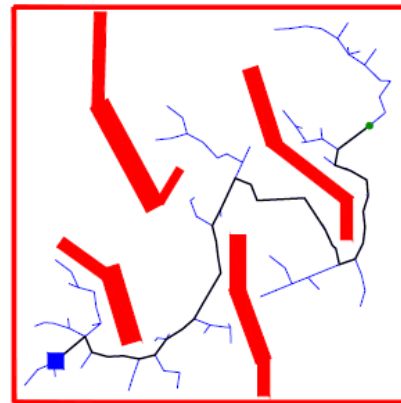
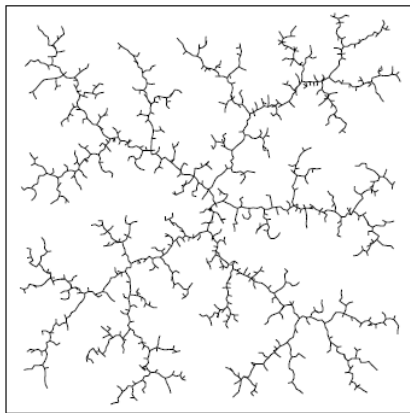
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- **Classical techniques**
- **Silhouette**
  
- **Sampling techniques w/ probabilistic completeness**
  - **Intuition: If there is a solution path, the algorithm will find it with a high probability**
  - **Probabilistic roadmaps**
  - **RRT techniques**

# Rapidly-exploring Random Trees (RRT) [LaValle 98]

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- Present an efficient randomized path planning algorithm for single-query problems
  - Converges quickly
  - Probabilistically complete
  - Works well in high-dimensional C-space

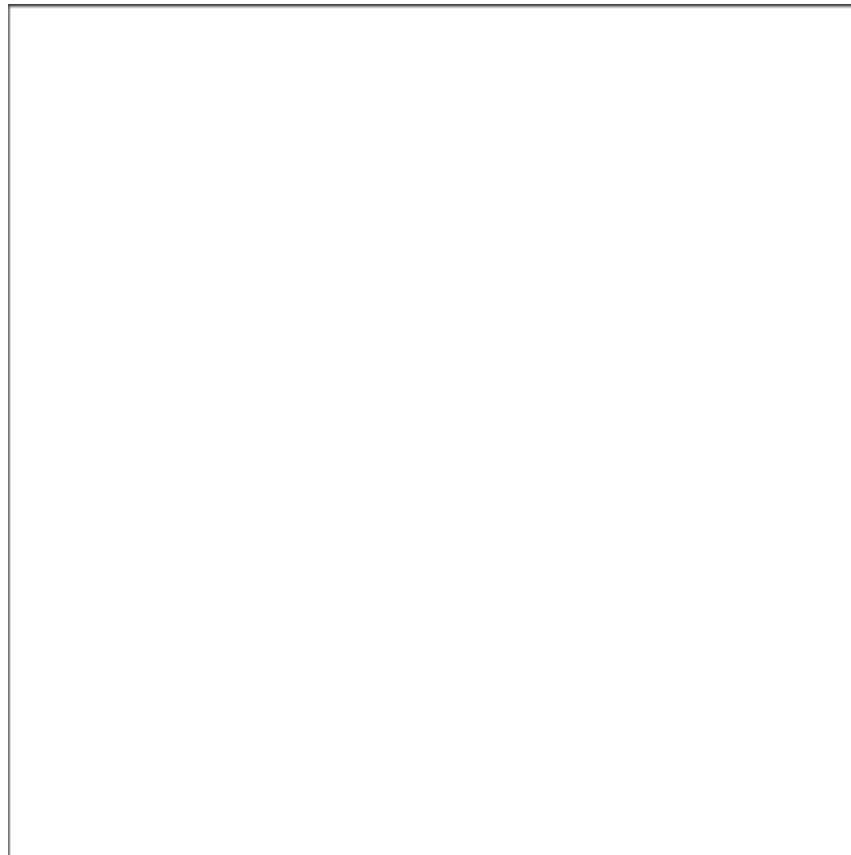


# Rapidly-Exploring Random Tree

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- A growing tree from an initial state



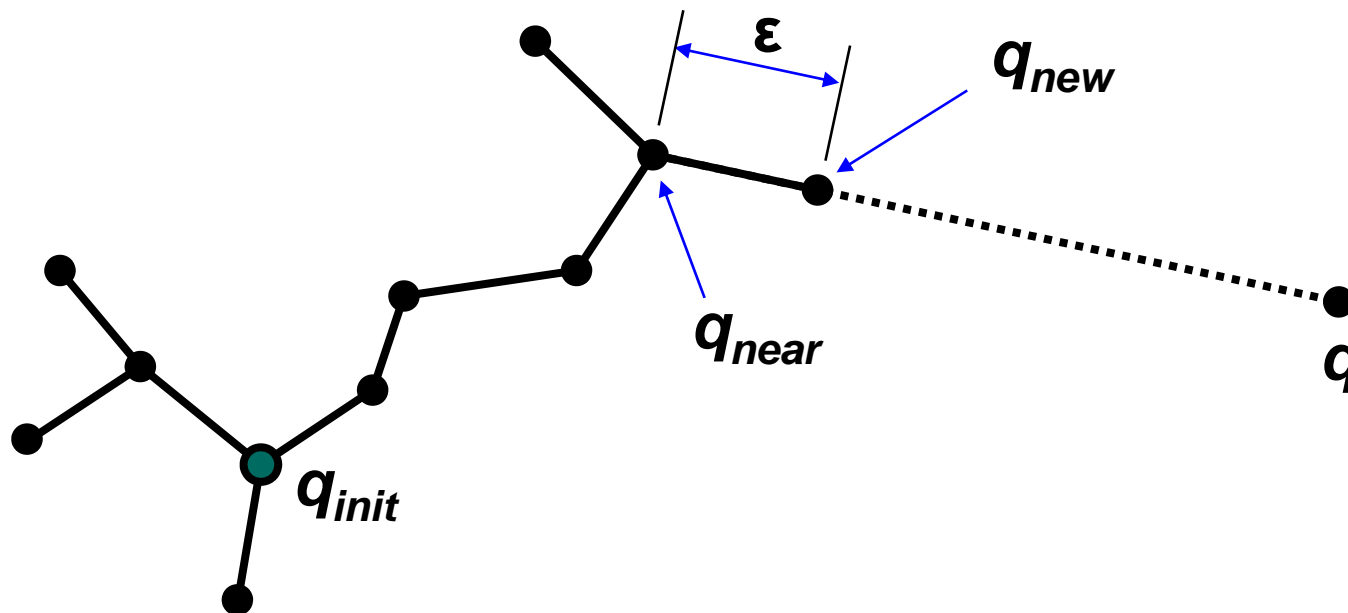


# RRT Construction Algorithm

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- Extend a new vertex in each iteration

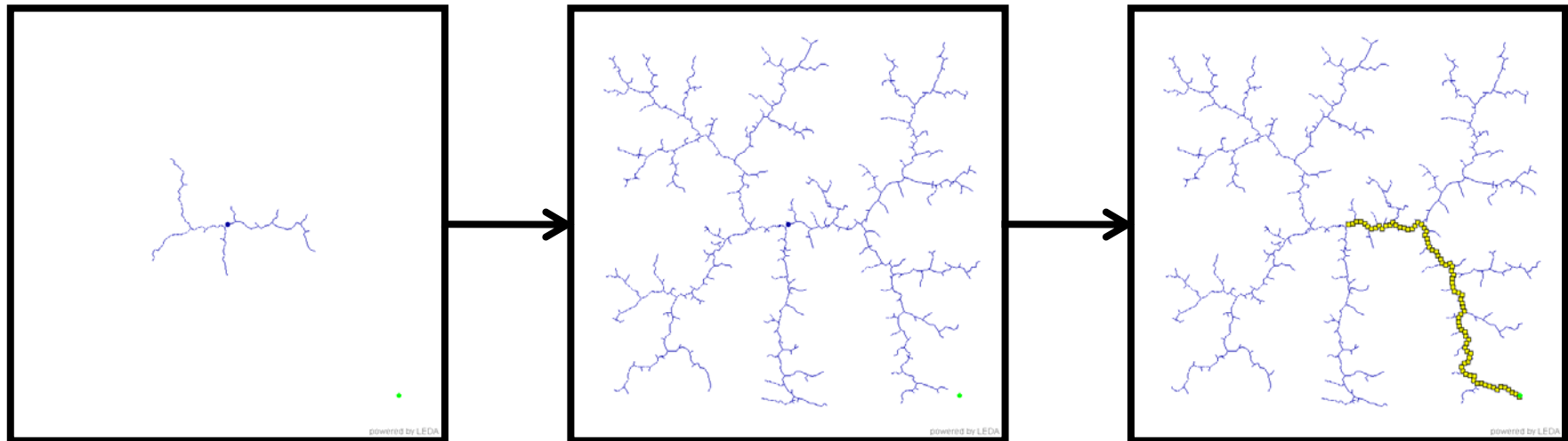


# Overview – Planning with RRT

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- **Extend RRT until a nearest vertex is close enough to the goal state**
  - Biased toward unexplored space
  - Can handle nonholonomic constraints and high degrees of freedom
- **Probabilistically complete, but does not converge**

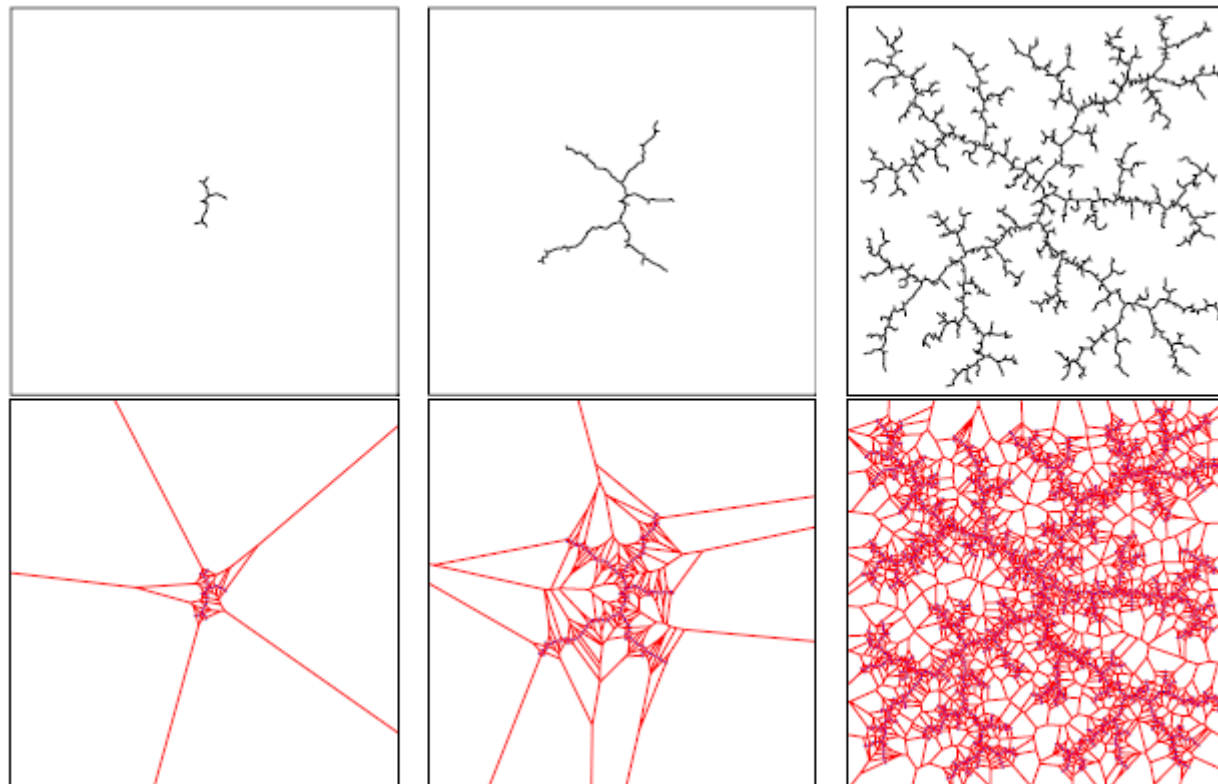


# Voronoi Region

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- An RRT is biased by large Voronoi regions to rapidly explore, before uniformly covering the space



# RRT Construction Algorithm

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```
BUILD_RRT( $q_{init}$ )
1   $\mathcal{T}.$ init( $q_{init}$ );
2  for  $k = 1$  to  $K$  do
3       $q_{rand} \leftarrow$  RANDOM_CONFIG();
4      EXTEND( $\mathcal{T}, q_{rand}$ );
5  Return  $\mathcal{T}$ 
```

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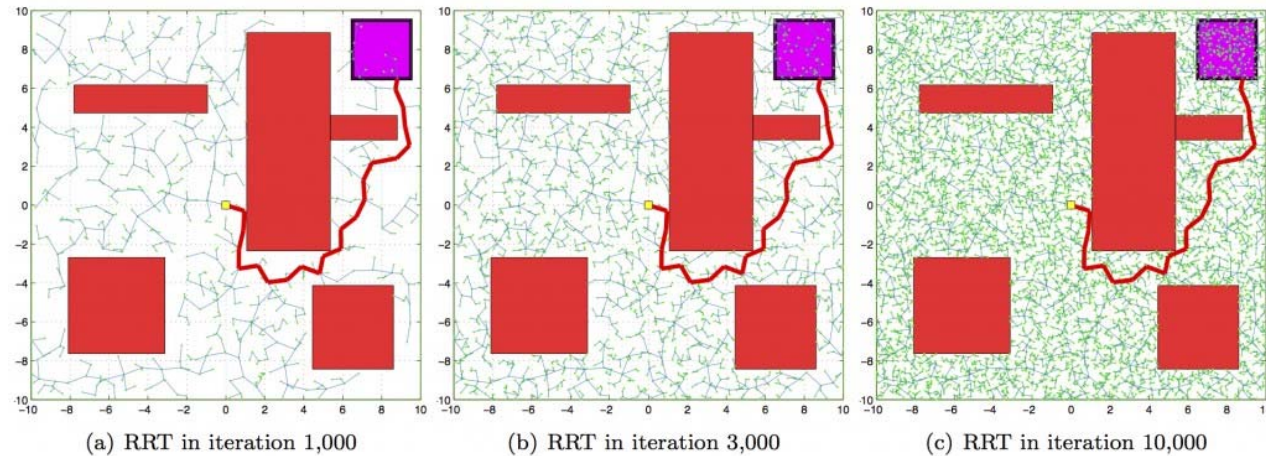
```
EXTEND( $\mathcal{T}, q$ )
1   $q_{near} \leftarrow$  NEAREST_NEIGHBOR( $q, \mathcal{T}$ );
2  if NEW_CONFIG( $q, q_{near}, q_{new}$ ) then
3       $\mathcal{T}.$ add_vertex( $q_{new}$ );
4       $\mathcal{T}.$ add_edge( $q_{near}, q_{new}$ );
5      if  $q_{new} = q$  then
6          Return Reached;
7      else
8          Return Advanced;
9  Return Trapped;
```

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# RRT\*

- RRT does not converge to the optimal solution

RRT



RRT\*

# RRT\*

- **Asymptotically optimal without a substantial computational overhead**

**Theorem [Karaman & Frazzoli, IJRR 2011]**

(i) The RRT\* algorithm is asymptotically optimal

$$\mathbb{P}\left(\left\{\lim_{n \rightarrow \infty} Y_n^{\text{RRT}^*} = c^*\right\}\right) = 1$$

(ii) RRT\* algorithm has no substantial computational overhead when compared to the RRT:

$$\lim_{n \rightarrow \infty} \mathbb{E} \left[ \frac{M_n^{\text{RRT}^*}}{M_n^{\text{RRT}}} \right] = \text{constant}$$

- $Y_n^{\text{RRT}^*}$  : cost of the best path in the RRT\*
- $c^*$  : cost of an optimal solution
- $M_n^{\text{RRT}}$  : # of steps executed by RRT at iteration n
- $M_n^{\text{RRT}^*}$  : # of steps executed by RRT\* at iteration n

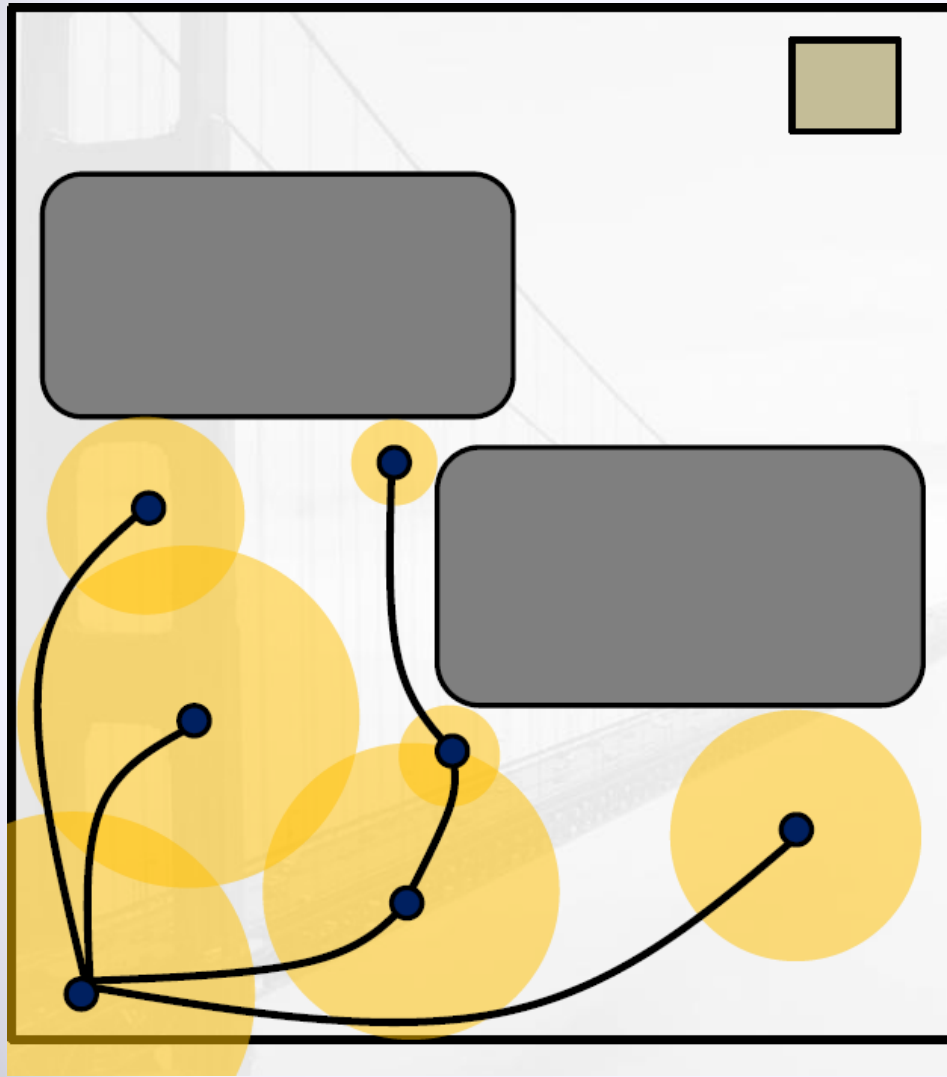
# Key Operation of RRT\*

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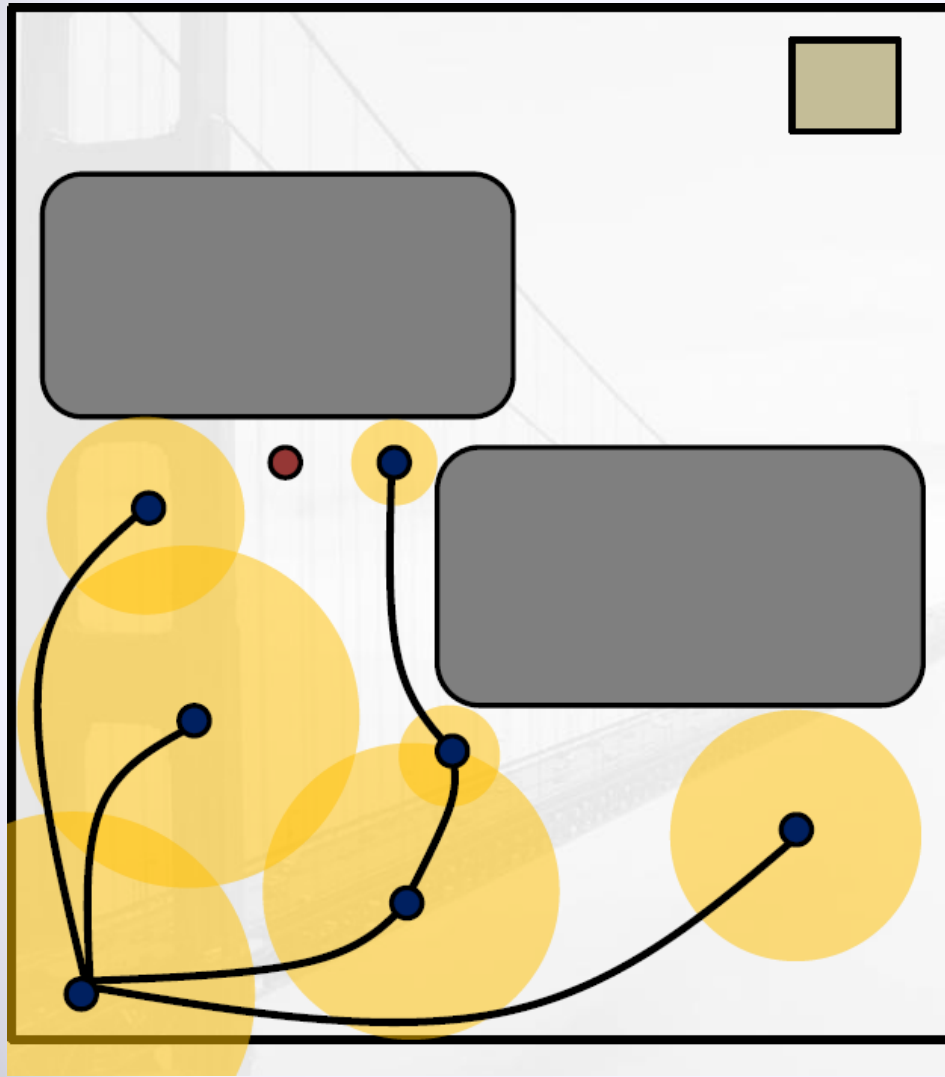
- **RRT**
  - Just connect a new node to its nearest neighbor node
- **RRT\* : refine the connection with re-wiring operation**
  - Given a ball, identify neighbor nodes to the new node
  - Refine the connection to have a lower cost

# Example: Re-Wiring Operation



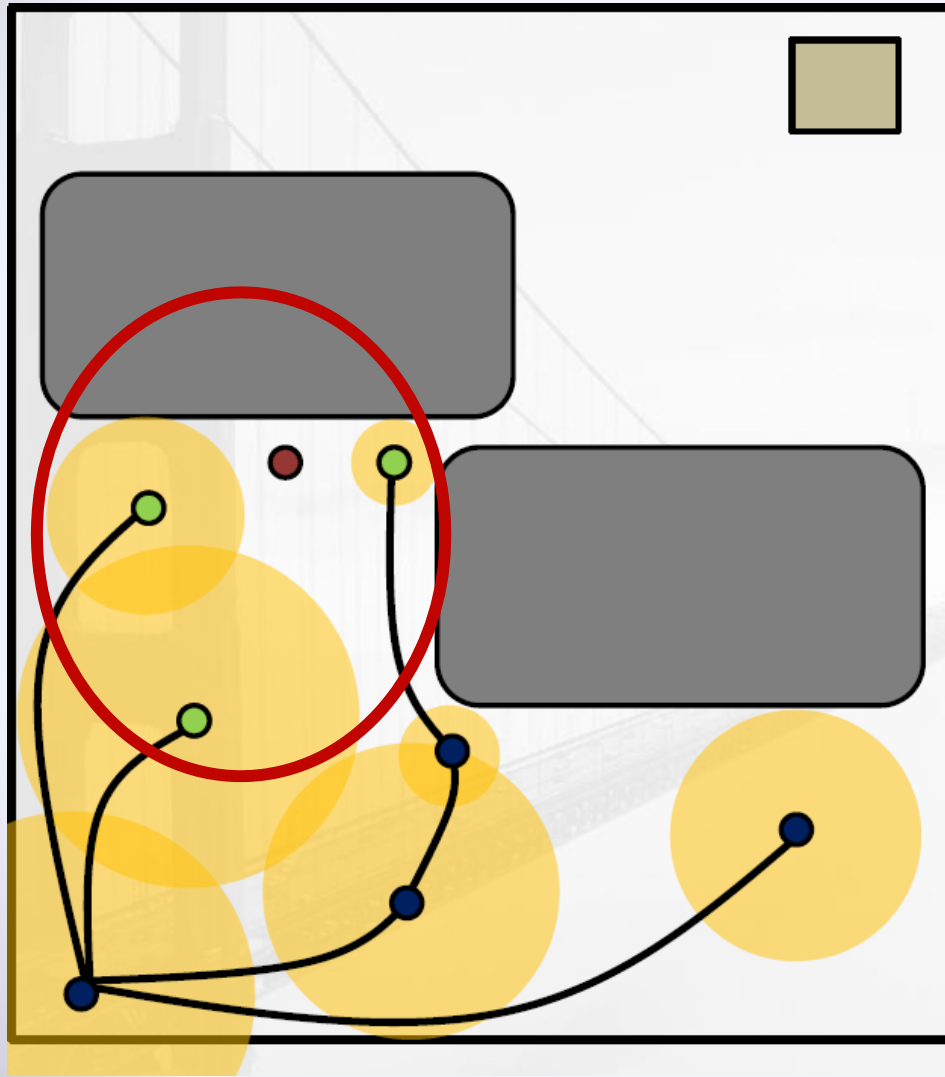


# Example: Re-Wiring Operation



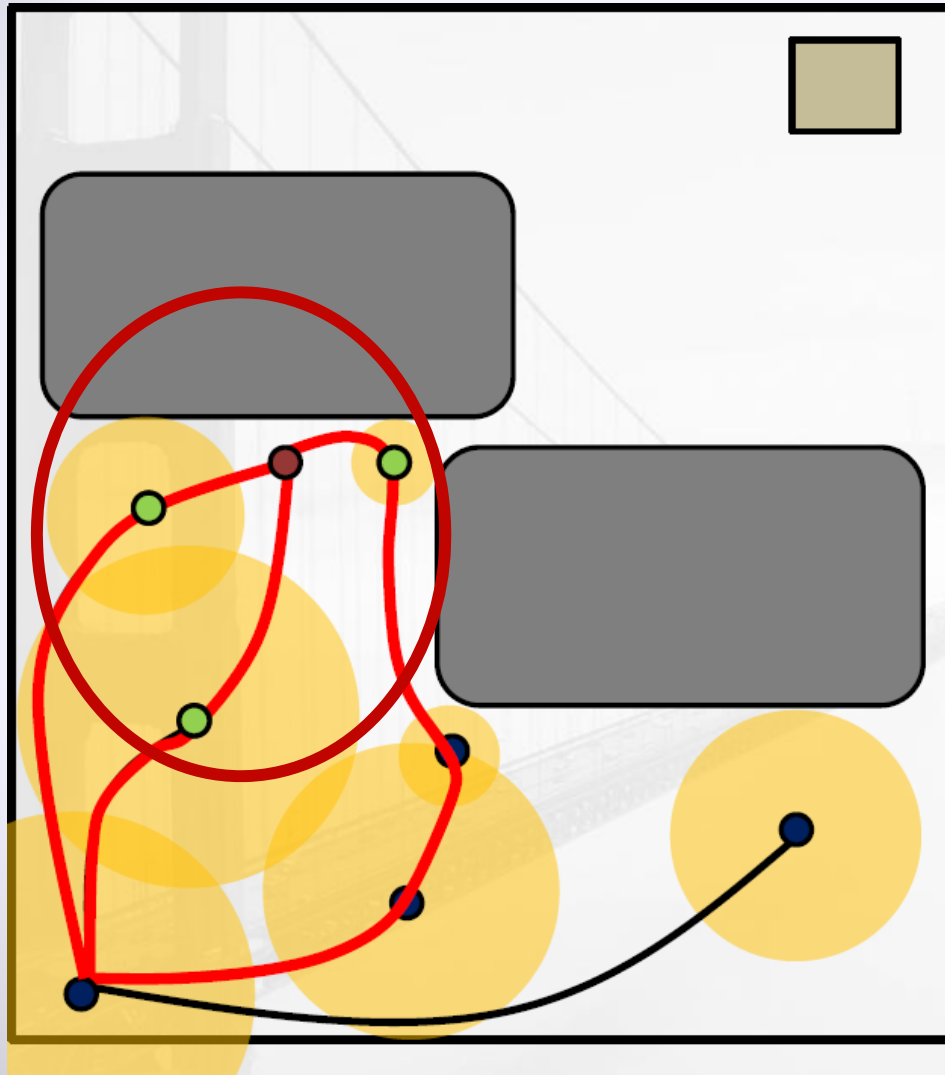
Generate a new sample

# Example: Re-Wiring Operation



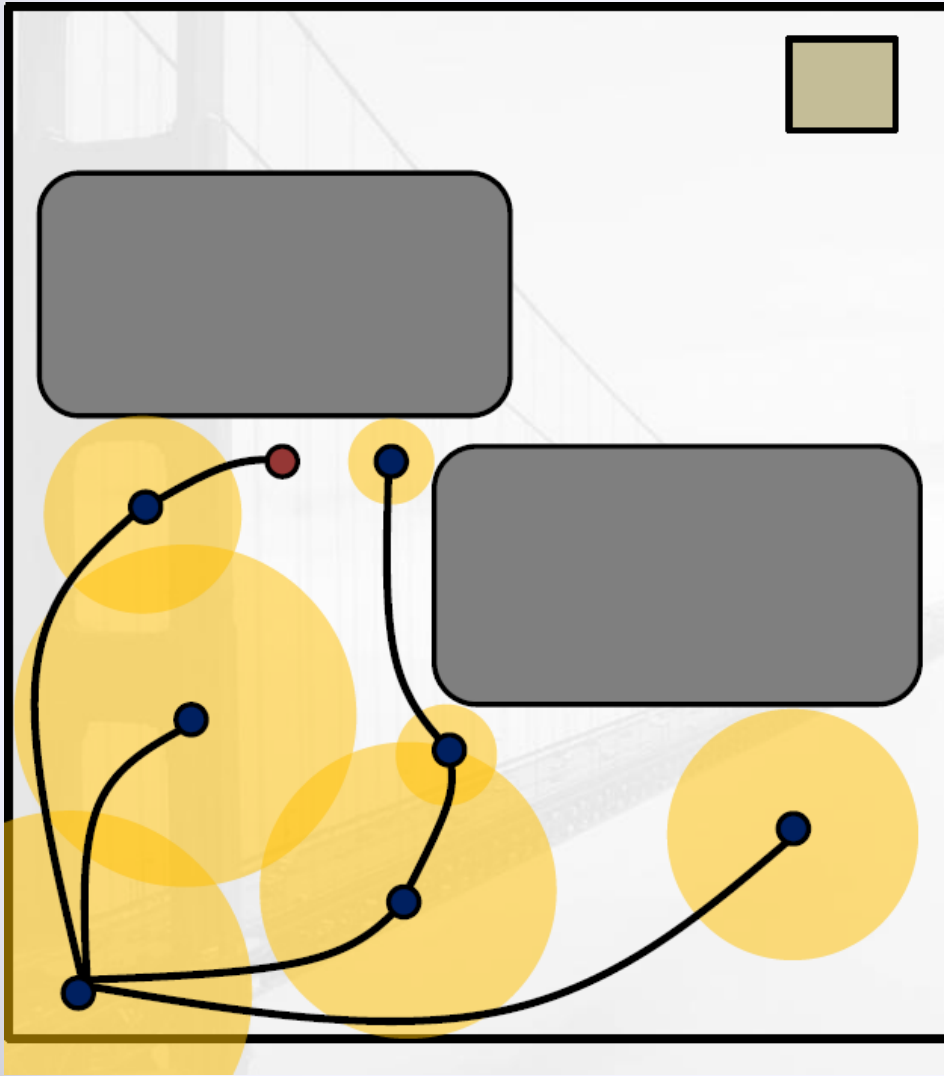
Identify nodes in a ball

# Example: Re-Wiring Operation

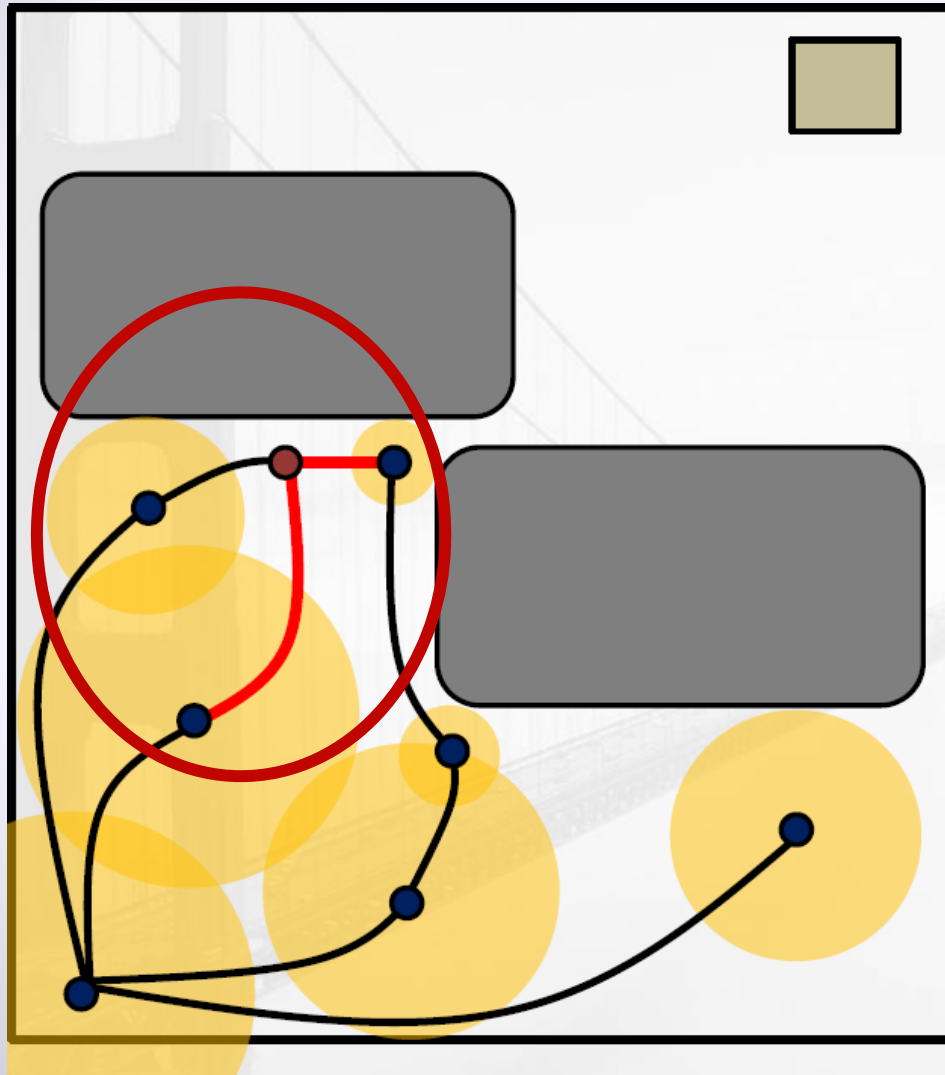


Identify which parent gives the lowest cost

# Example: Re-Wiring Operation

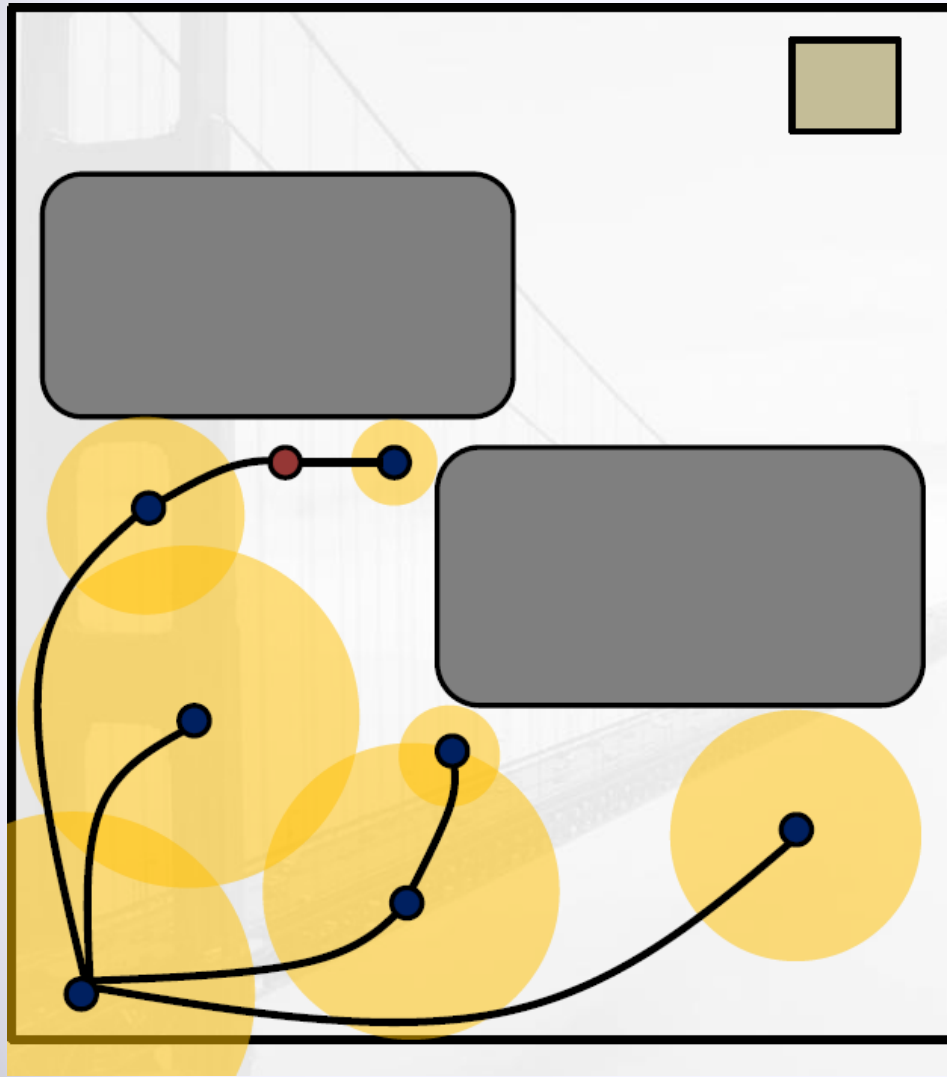


# Example: Re-Wiring Operation



Identify which child gives the lowest cost

# Example: Re-Wiring Operation



Video showing benefits  
with real robot

# Two Recent Works of Our Group

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- Handling narrow passages
- Improving low convergence to the optimal solution

# Two Recent Works of Our Group

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- **Narrow passages**
  - Identify narrow passage with a simple one-dimensional line test, and selectively explore such regions
  - Selective retraction-based RRT planner for various environments, Lee et al., T-RO 14
  - <http://sglab.kaist.ac.kr/SRRRT/T-RO.html>
- **Low convergence to the optimal solution**



# Retraction-based RRT

## [Zhang & Manocha 08]

- Retraction-based RRT technique **handling narrow passages**

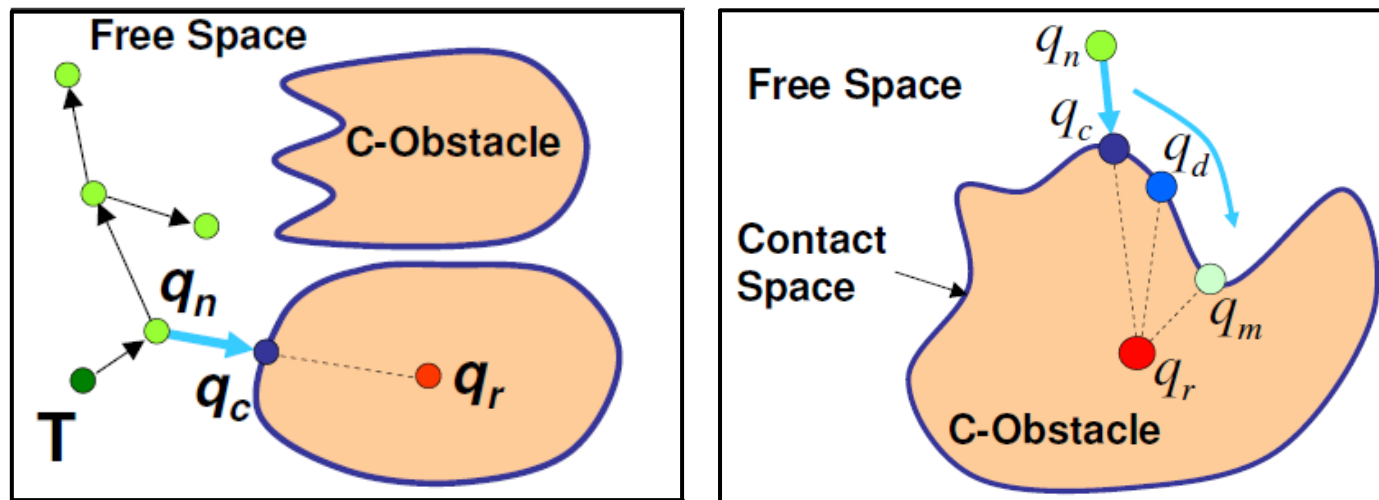
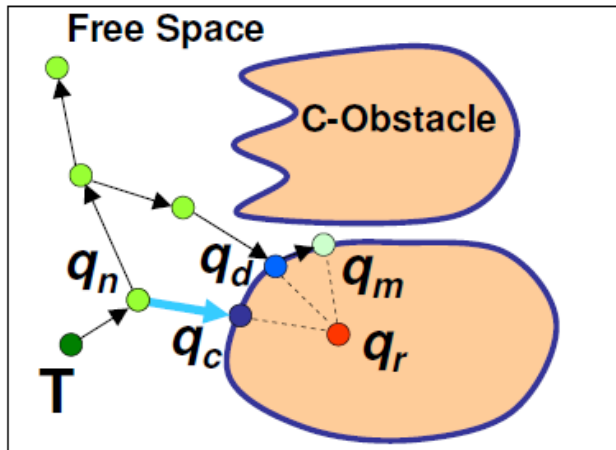


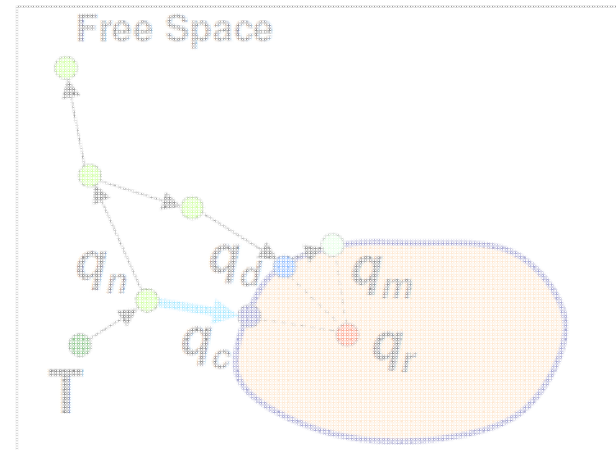
image from [Zhang & Manocha 08]

- General characteristic:**  
Generates more samples near the boundary of obstacles

# RRRT: Pros and Cons

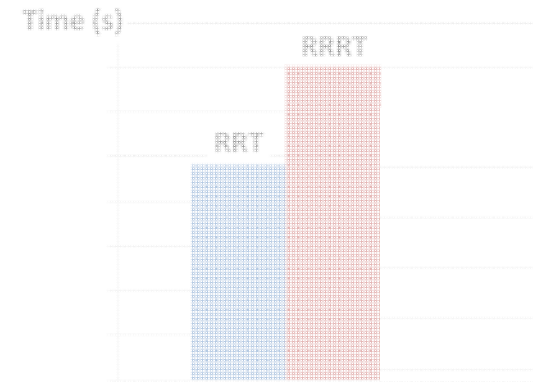
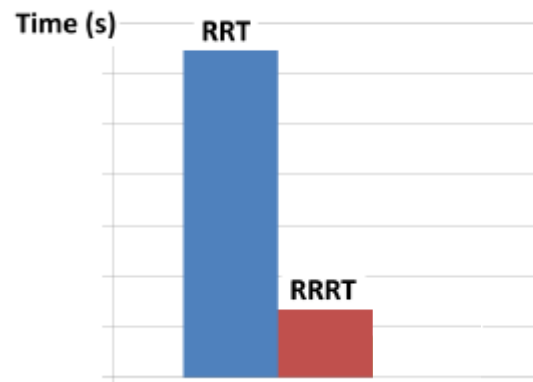


with narrow passages

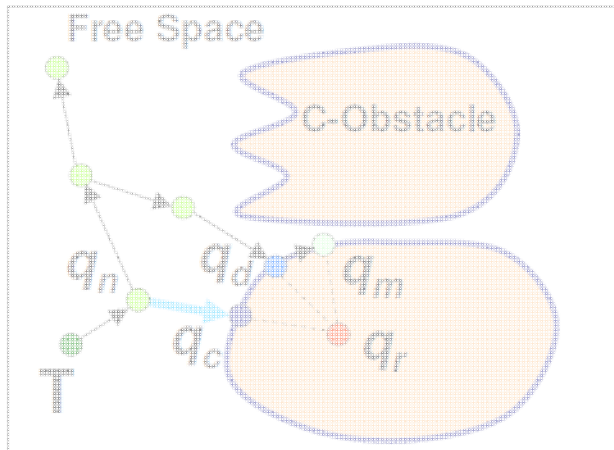


without narrow passages

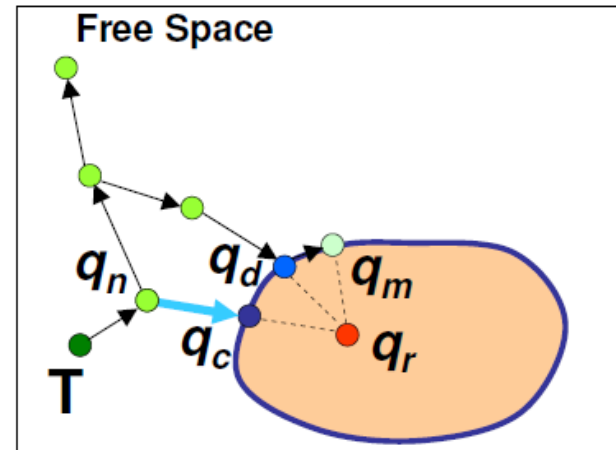
images from [Zhang & Manocha 08]



# RRRT: Pros and Cons

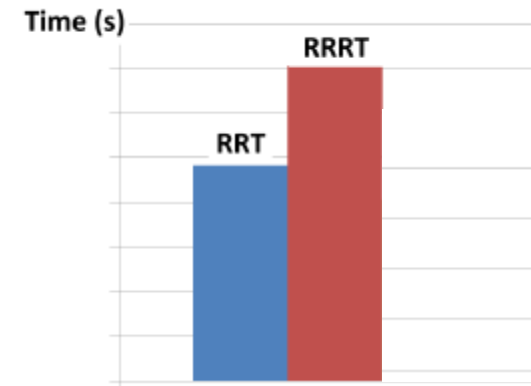
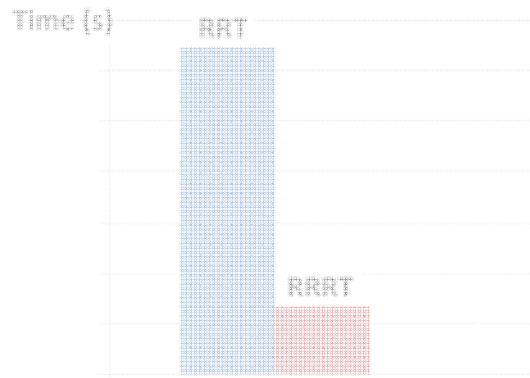


with narrow passages



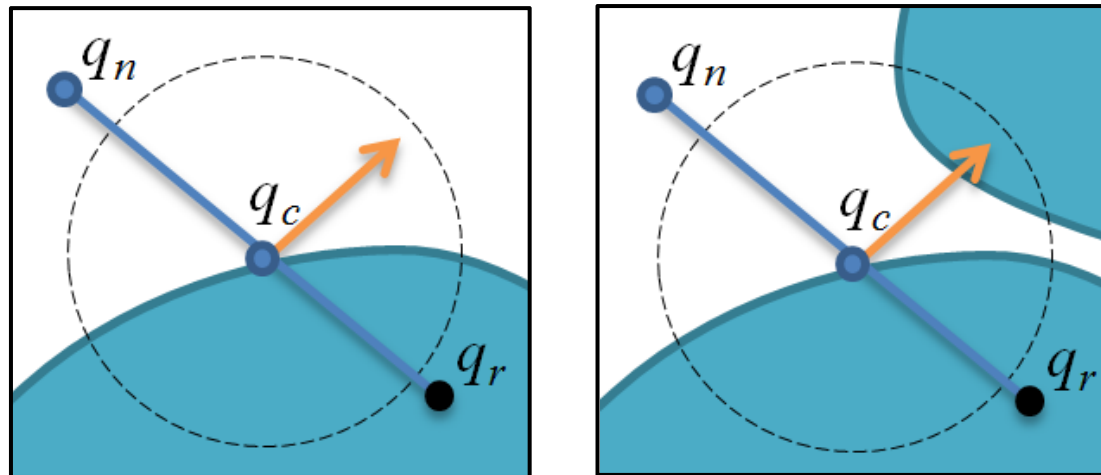
without narrow passages

images from [Zhang & Manocha 08]

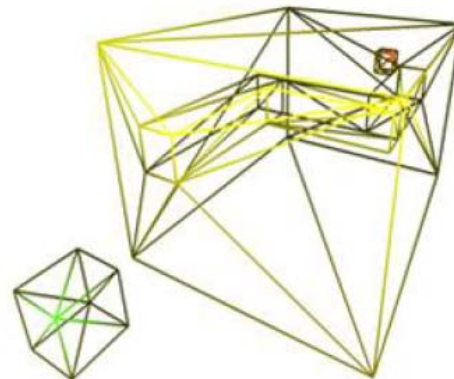
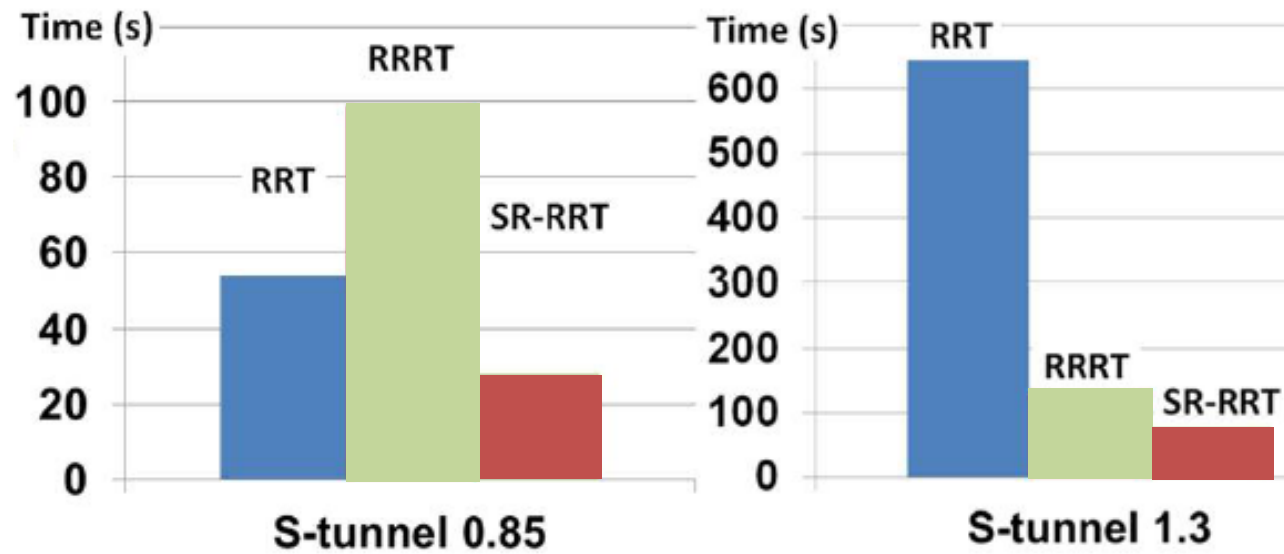


# Bridge line-test [Lee et al., T-RO 14]

- To identify narrow passage regions
- Bridge line-test
  1. Generate a random line
  2. Check whether the line meets any obstacle



# Results



Video

# Two Recent Works of Our Group

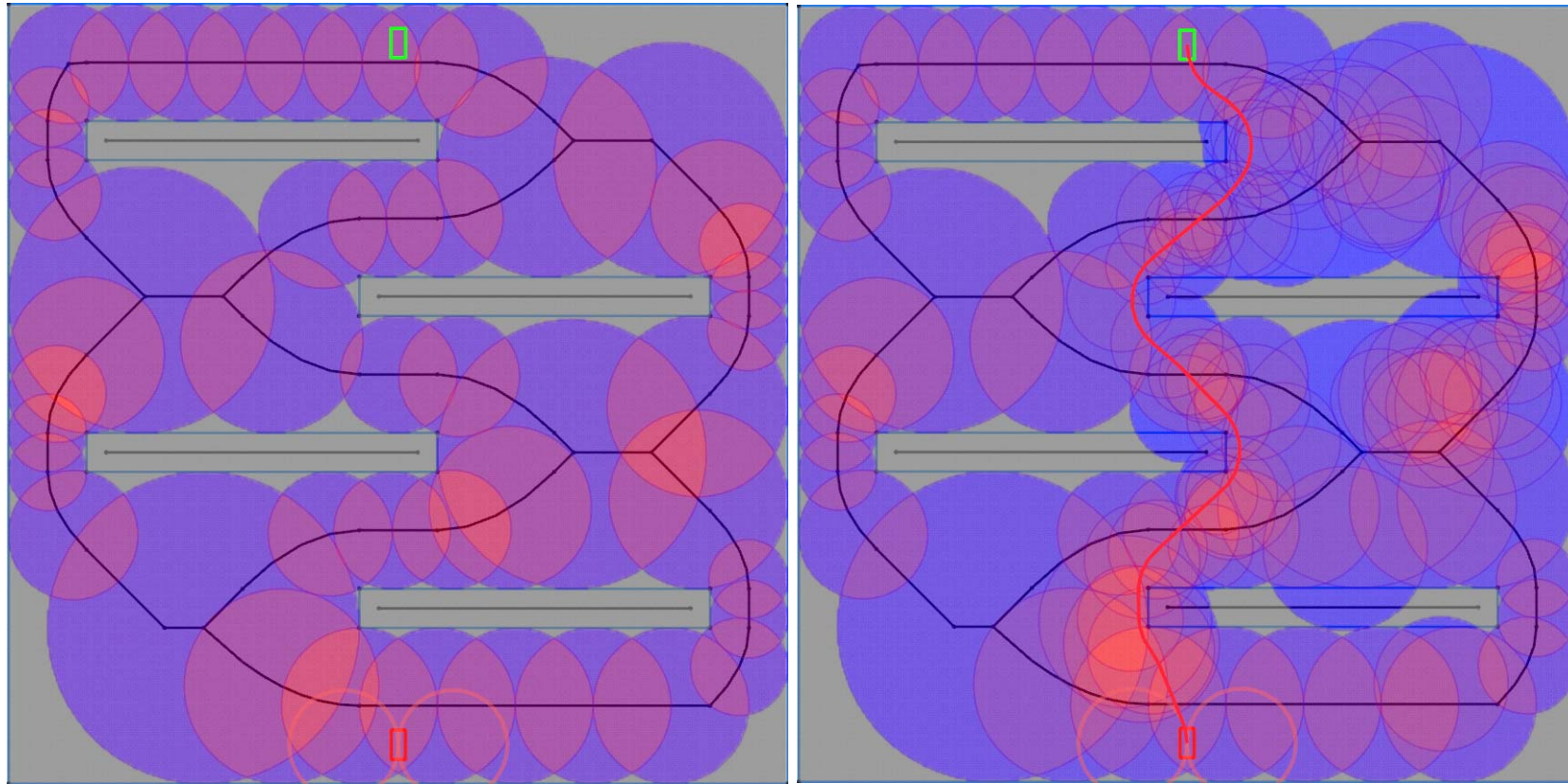
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- Handling narrow passages
- Improving low convergence to the optimal solution
  - Use the sampling cloud to indicate regions that lead to the optimal path
  - Cloud RRT\* : Sampling Cloud based RRT\* , Kim et al., ICRA 14
  - <http://sglab.kaist.ac.kr/CloudRRT/>

# Examples of Sampling Cloud

[Kim et al., ICRA 14]

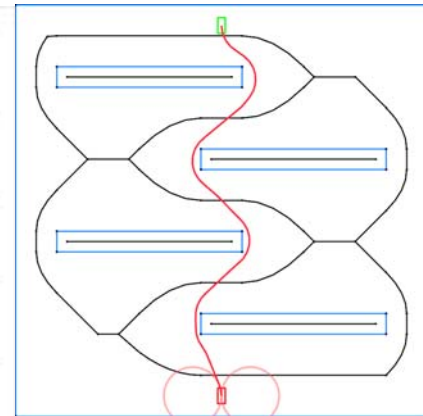
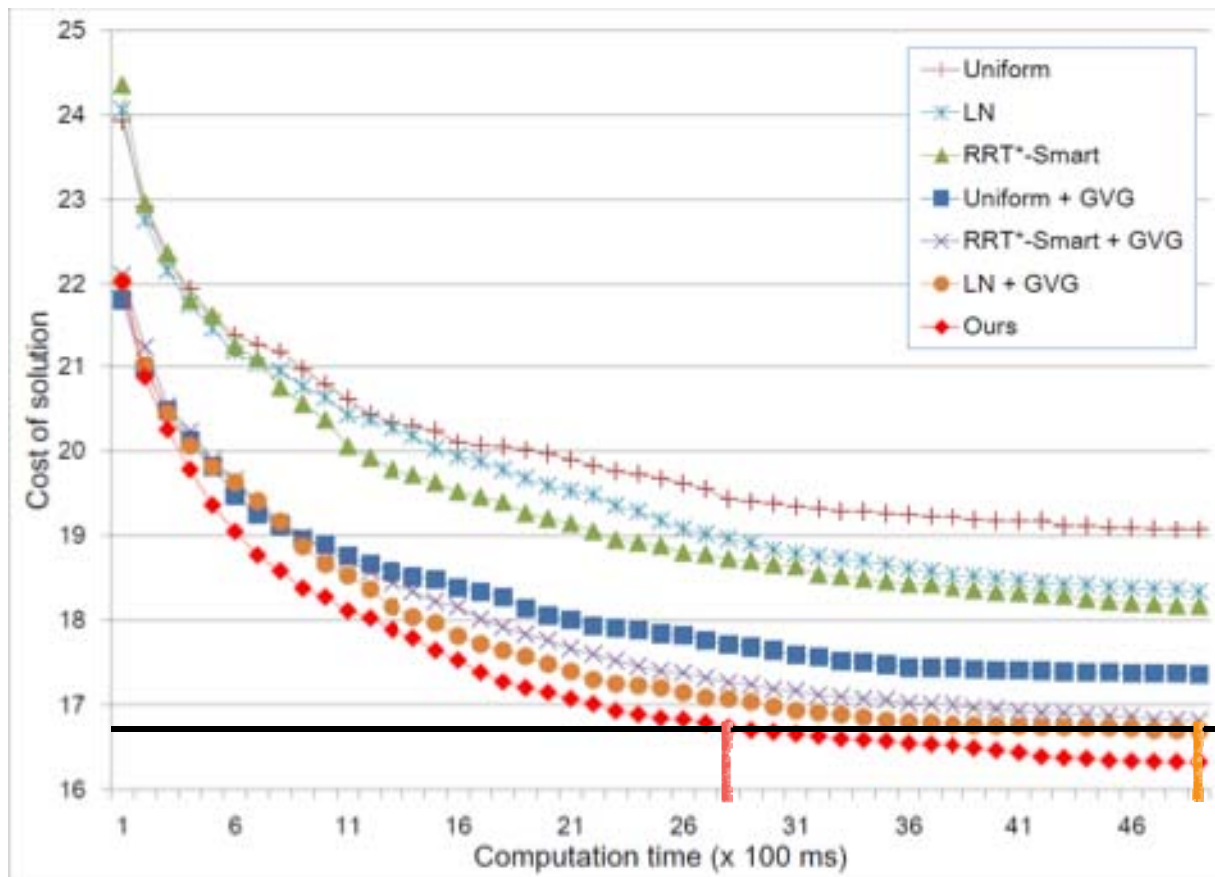


Initial state of sampling cloud

After updated several times

Video

# Results: 4 squares



**1.8X  
improvement**



# Conclusions

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- Explained the basic motion planning problem and its goal
- Covered basic sampling based planners
  - RRT
- Discussed an optimal RRT: RRT\*
- Briefly talked about two recent works
  - Handling narrow passages and low convergence

<http://sglab.kaist.ac.kr>

# Acknowledgements

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- **Collaborators**

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