
Multi-Resolution Method for Ray Tracing

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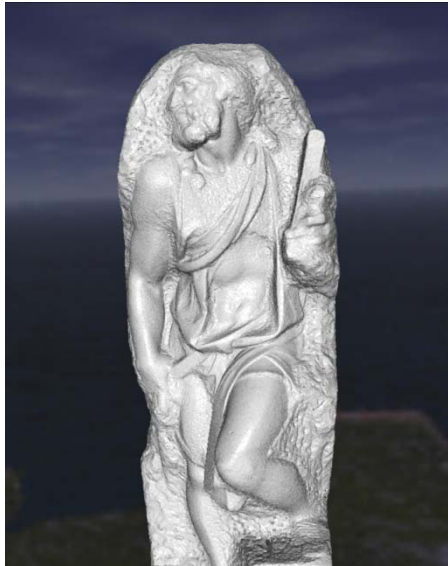
Course URL:
<http://jupiter.kaist.ac.kr/~sungeui/SGA/>

At the Previous Class

- **Studied LOD techniques for rasterization**

Goal

- **Perform an interactive ray tracing of massive models**
 - **Handles various kinds of polygonal meshes (e.g., scanned data and CAD)**



**St. Matthew
372M triangles**



**Double eagle tanker
82M triangles**



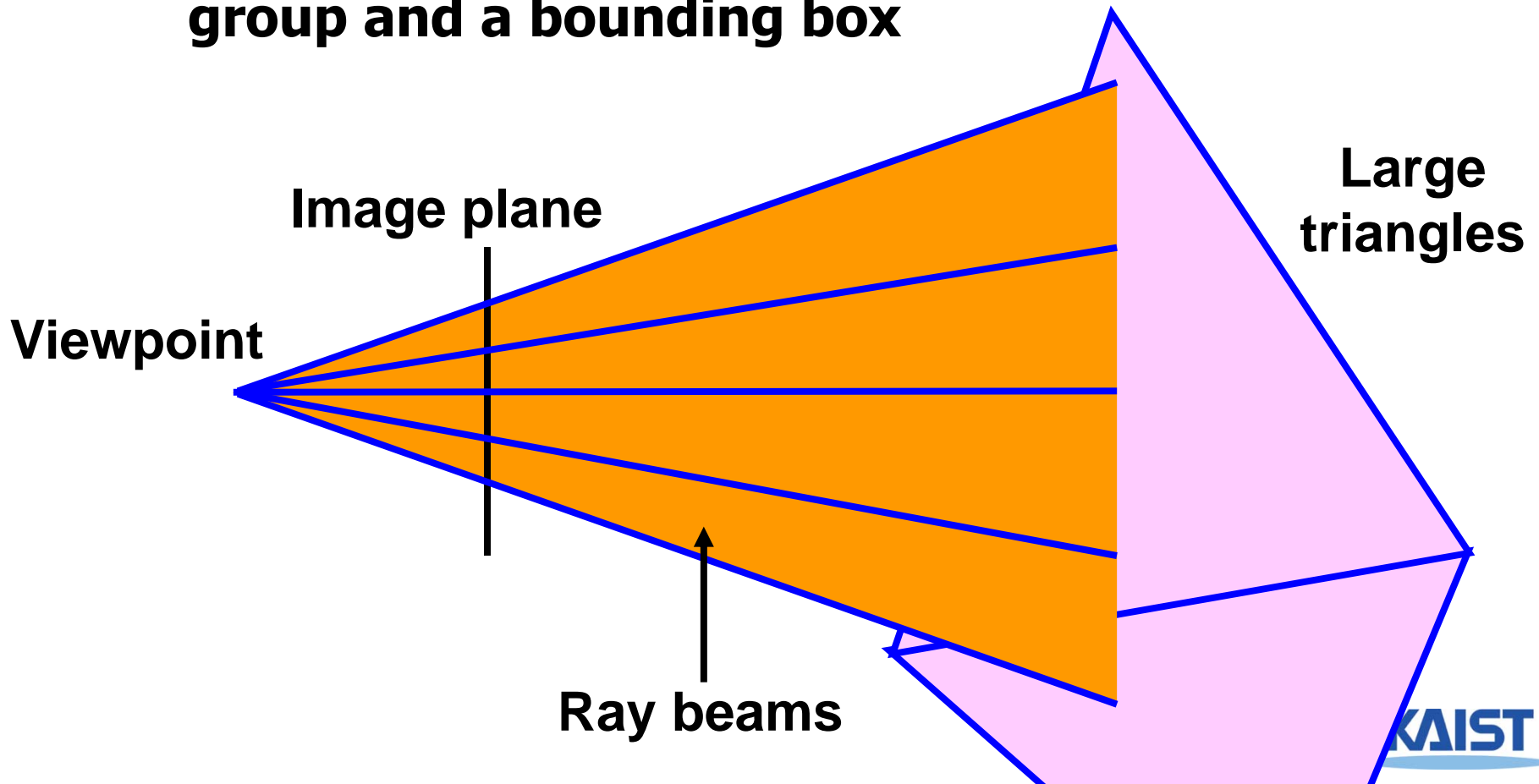
Forest model (32M)

Recent Advances for Interactive Ray Tracing

- **Hardware improvements**
 - Exponential growth of computation power
 - Multi-core architectures
- **Algorithmic improvements**
 - Efficient ray coherence techniques [**Wald et al. 01, Reshetov et al. 05**]

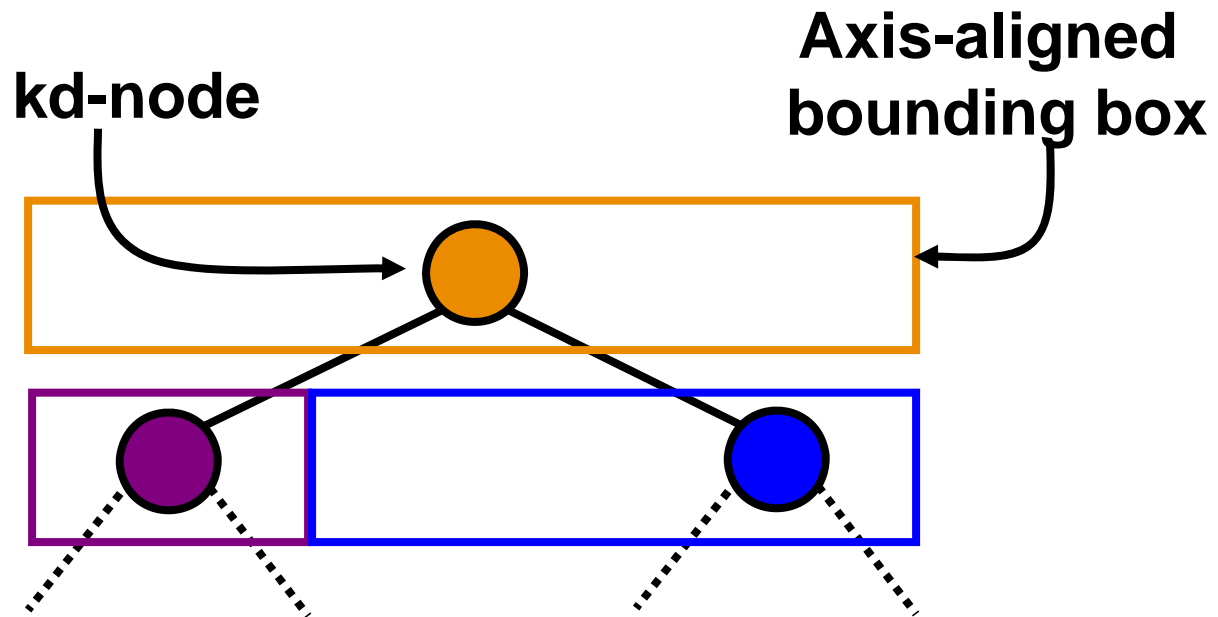
Ray Coherence Techniques

- **Models with large primitives**
 - **Group rays and test intersections between the group and a bounding box**



Hierarchical Acceleration Data Structures

- **kd-trees for interactive ray tracing [Wald 04]**
 - **Simplicity and efficiency**
 - **Used for efficient object culling**

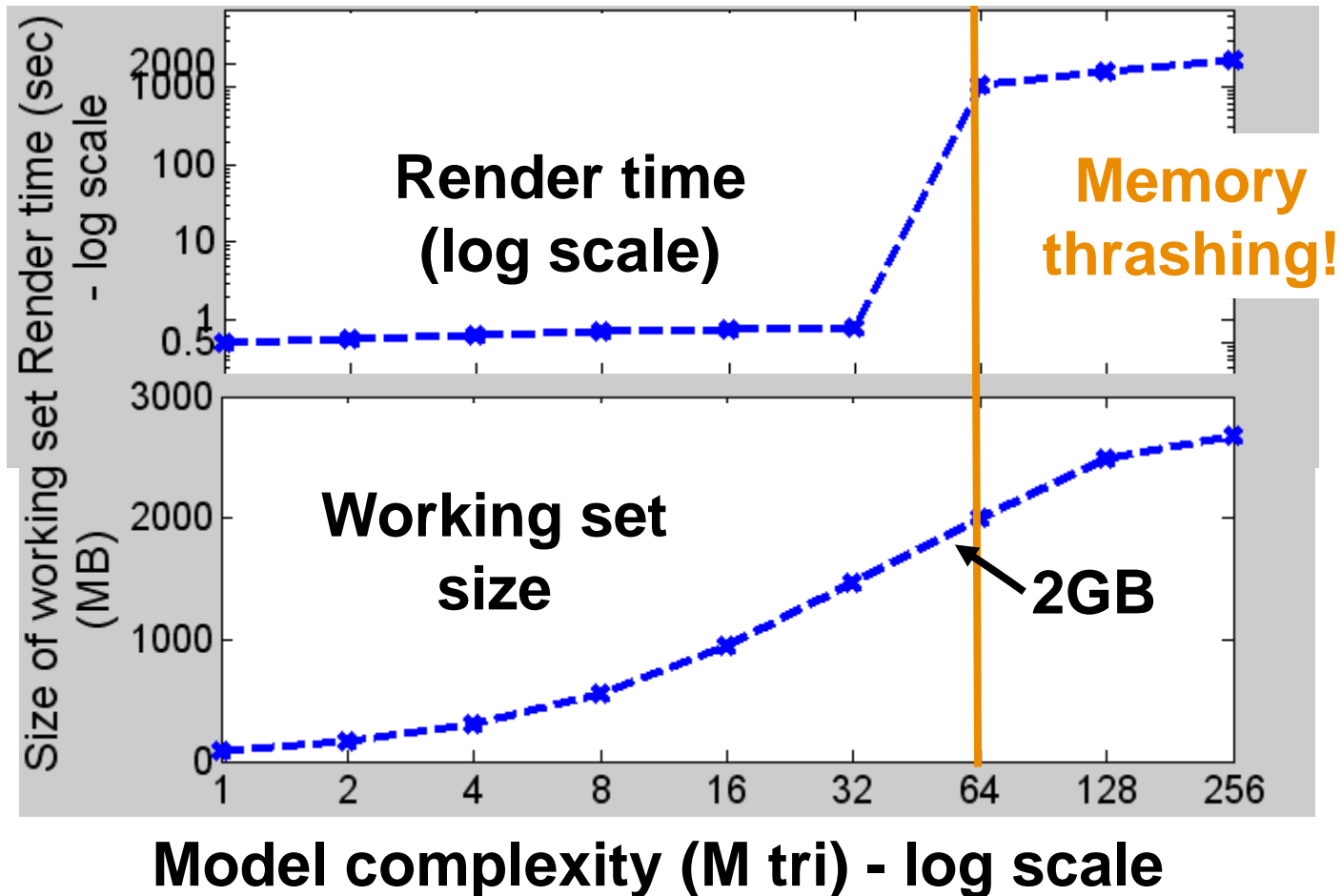


Ray Tracing of Massive Models

- **Logarithmic asymptotic behavior**
 - **Very useful for dealing with massive models**
 - **Due to the hierarchical data structures**
 - **Observed only in in-core cases**

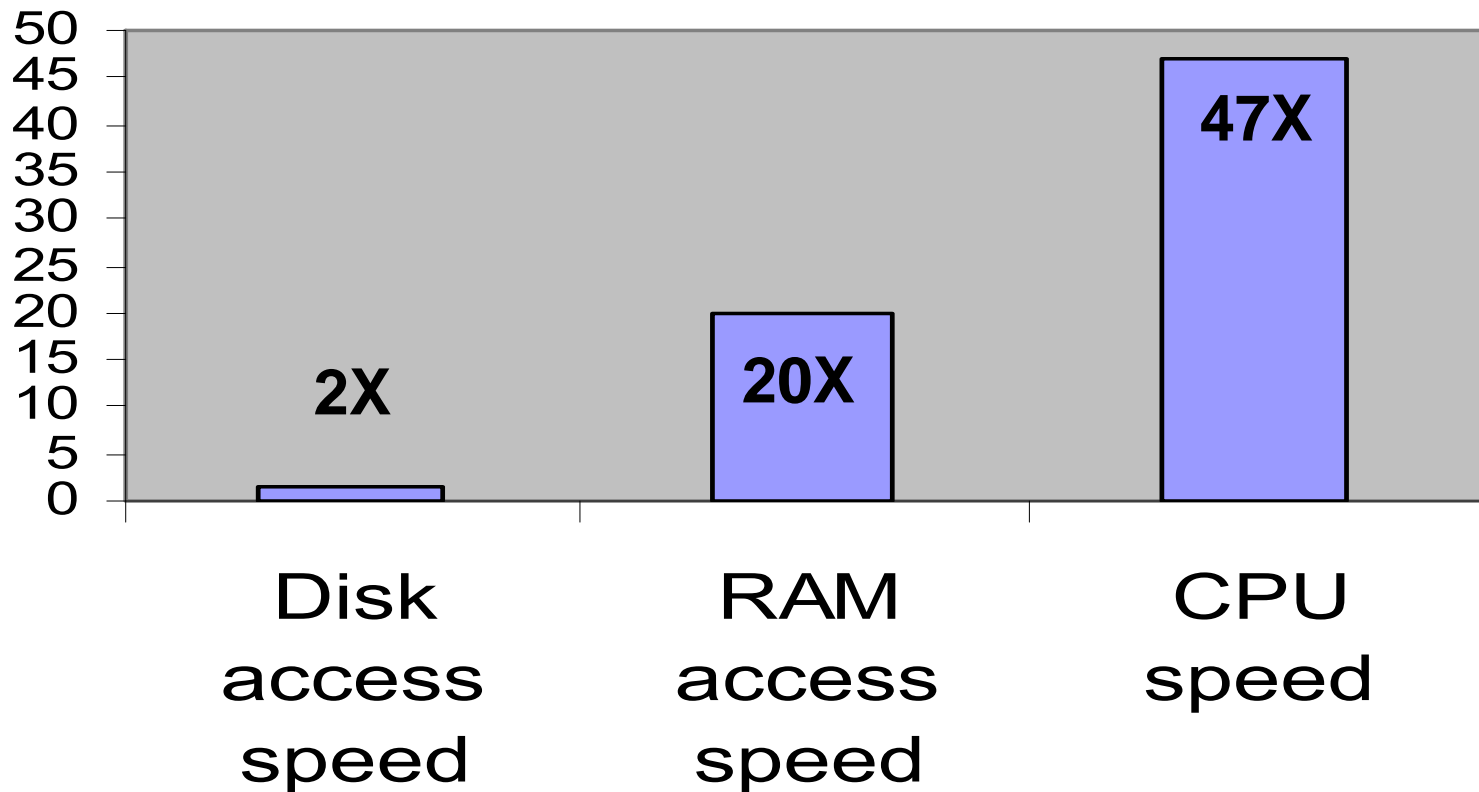
Performance of Ray Tracing with Different Model Complexity

- Measured with 2GB main memory



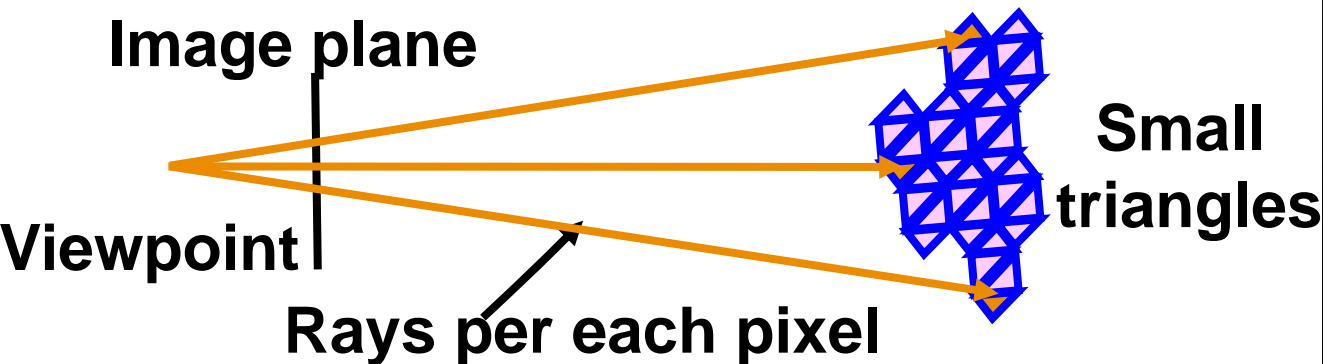
Low Growth Rate of Data Access Time

Growth rate
during 1993 – 2004



Inefficient Memory Accesses and Temporal Aliasing

- **St. Matthew (256M triangles)**
 - Around 100M visible triangles
- **1K by 1K image resolution**
 - 1M primary rays
 - Hundreds of triangle per pixel
 - Each triangle likely in different area of memory



Example of Aliasing



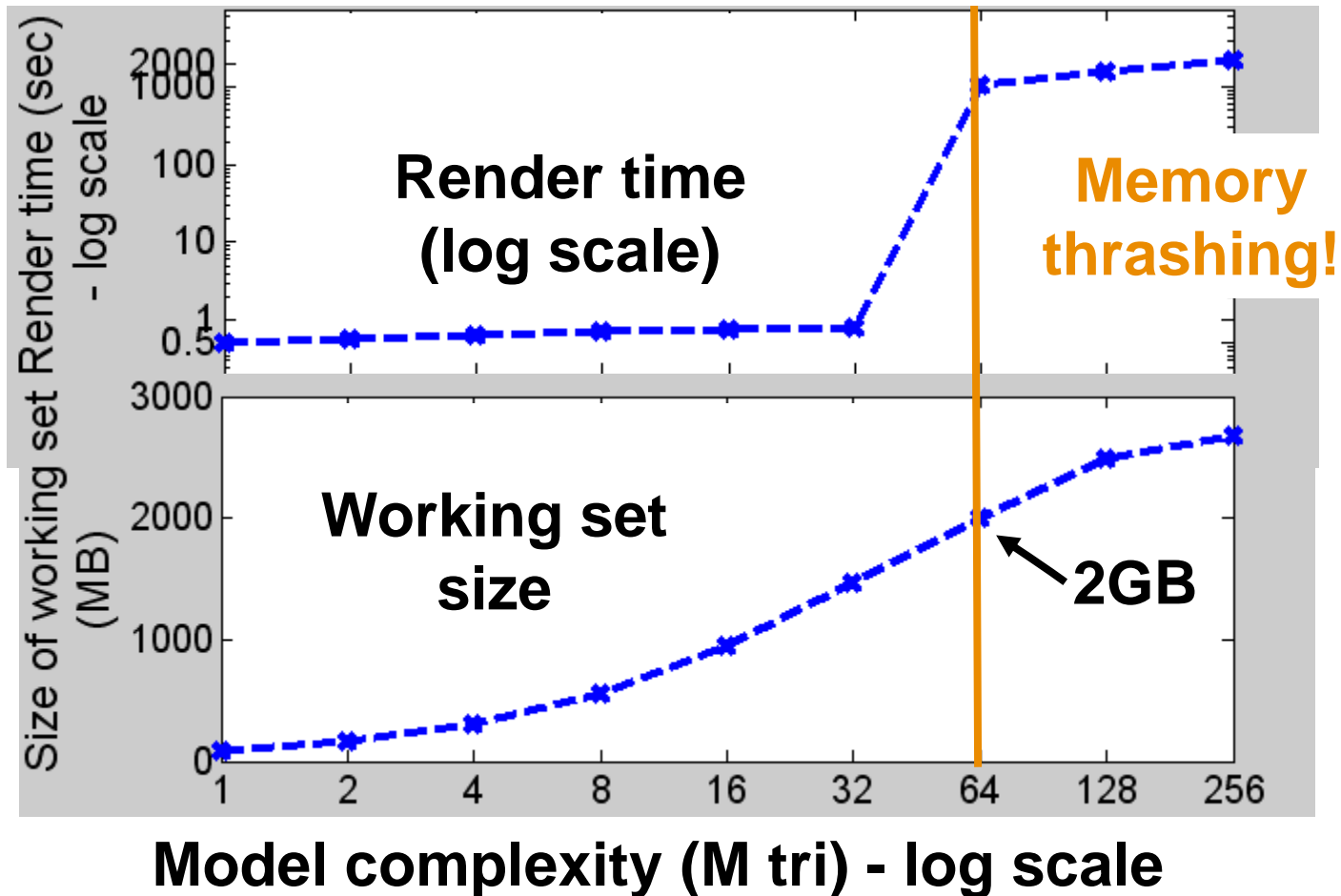
Due to the under-sampling

LOD-based Ray Tracing

- **Propose an LOD (level-of-detail)-based ray tracing of massive models**
 - **R-LOD, a novel LOD representation for Ray tracing**
 - **Efficient LOD error metric for primary and secondary rays**
 - **Integrate ray and cache coherent techniques**

Performance of Ray Tracing with Different Model Complexity

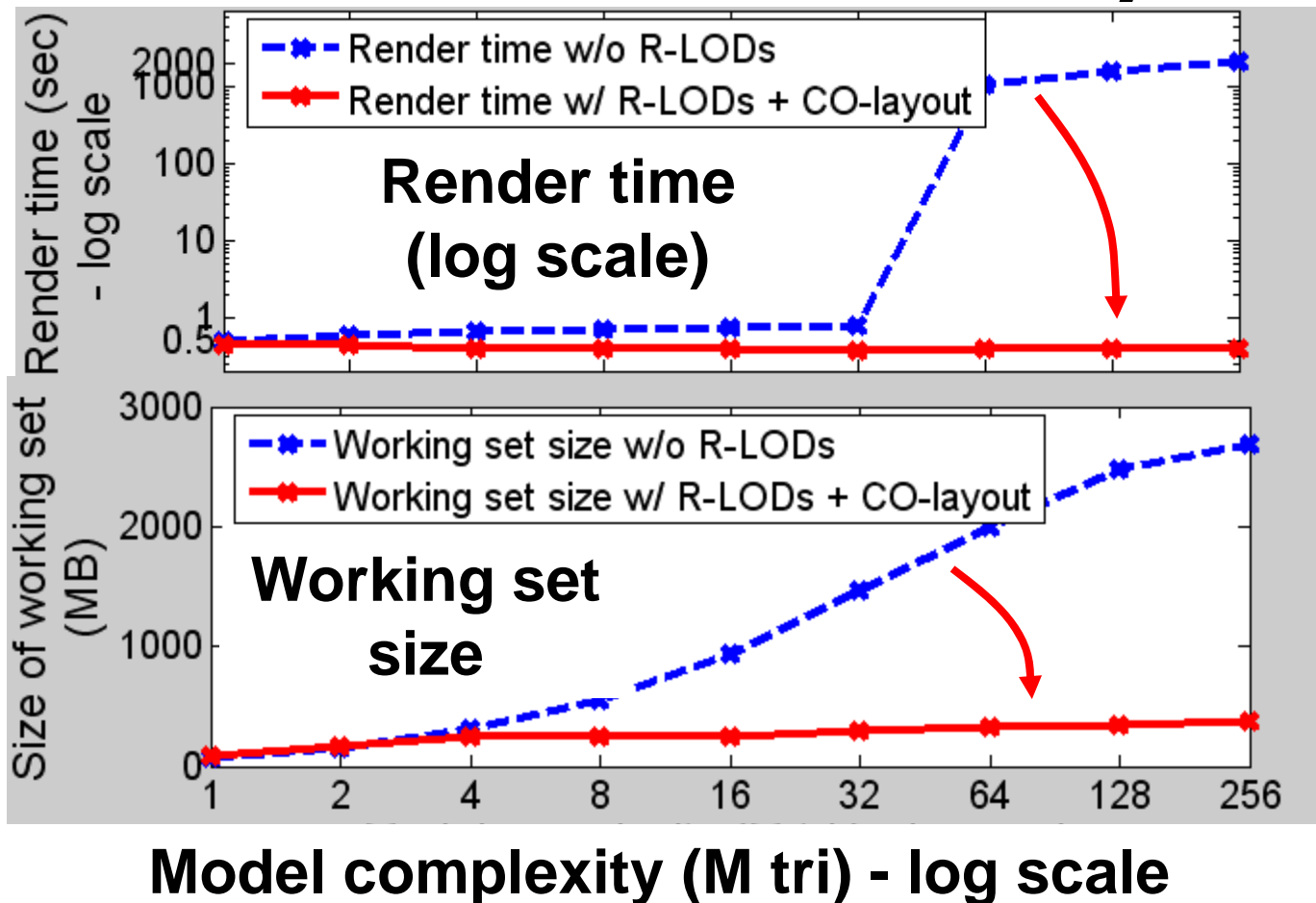
- Measured with 2GB main memory



Performance of LOD-based Ray Tracing

Achieved up to three order of magnitude speedup!

- Measured with 2GB main memory



Real-time Captured Video – St. Matthew Model



St. Matthew

128 Million triangles

Dual Xeon processors
with Hyper-Threading

Resolution: 512x512

**512 by 512 and 2x2 super-sampling,
4 pixels of LOD error in image space**

Related Work

- **Interactive ray tracing**
- **LOD and out-of-core techniques**
- **LOD-based ray tracing**

Interactive Ray Tracing

- **Ray coherences**
 - [Heckbert and Hanrahan 84, Wald et al. 01, Reshetov et al. 05]
- **Parallel computing**
 - [Parker et al. 99, DeMarle et al. 04, Dietrich et al. 05]
- **Hardware acceleration**
 - [Purcell et al. 02, Schmittler et al. 04, Woop et al. 05]
- **Large dataset**
 - [Pharr et al. 97, Wald et al. 04]

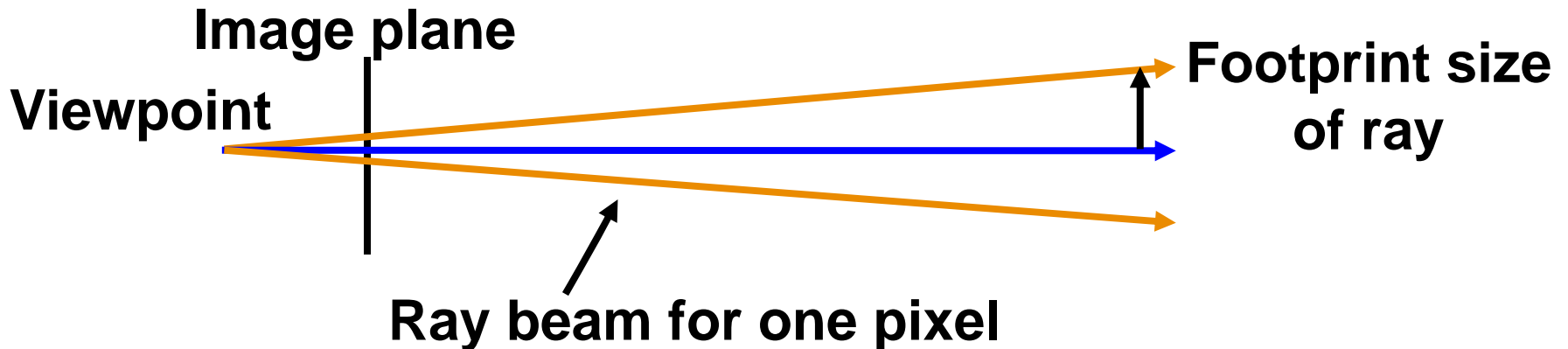
LOD and Out-of-Core Techniques

- **Widely researched**
 - LOD book [Luebke et al. 02]
 - Out-core algorithm course [Chiang et al. 03]
- **LOD algorithms combined with out-of-core techniques**
 - Points clouds [Rusinkiewicz and Levoy 00]
 - Regular meshes [Hwa et al. 04, Losasso and Hoppe 04]
 - General meshes [Lindstrom 03, Cignoni et al. 04, Yoon et al. 04, Gobbetti and Marton 05]

**Not clear whether LOD techniques
for rasterization is applicable to ray tracing**

LOD-based Ray Tracing

- **Ray differentials [Igehy 99]**
 - **Subdivision meshes [Christensen et al. 03, Stoll et al. 06]**
 - **Point clouds [Wand and Straßer 03]**



Outline

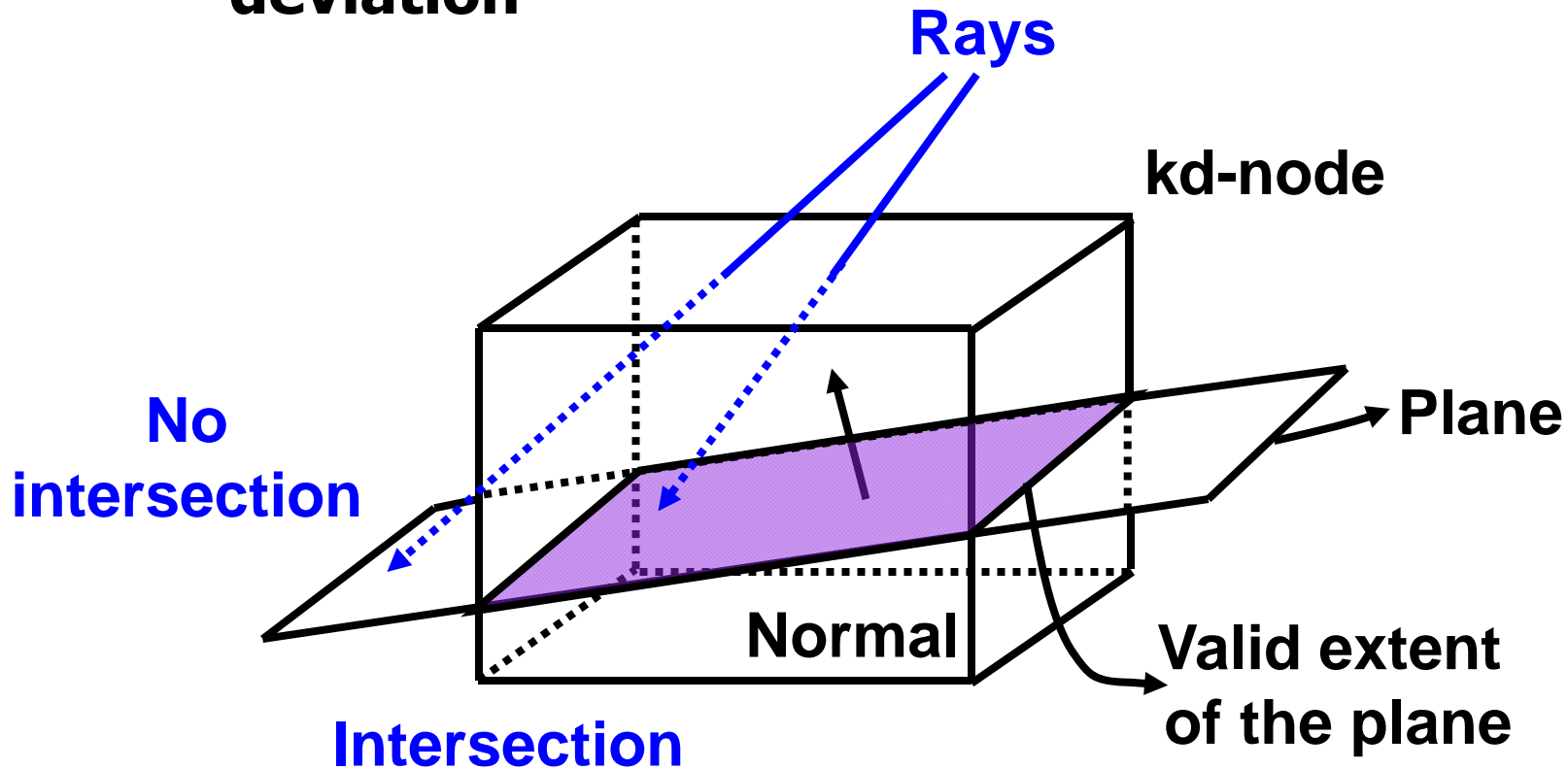
- **R-LODs for ray tracing**
- **Results**

Outline

- **R-LODs for ray tracing**
- Results

R-LOD Representation

- **Tightly integrated with kd-nodes**
 - **A plane, material attributes, and surface deviation**



Properties of R-LODs

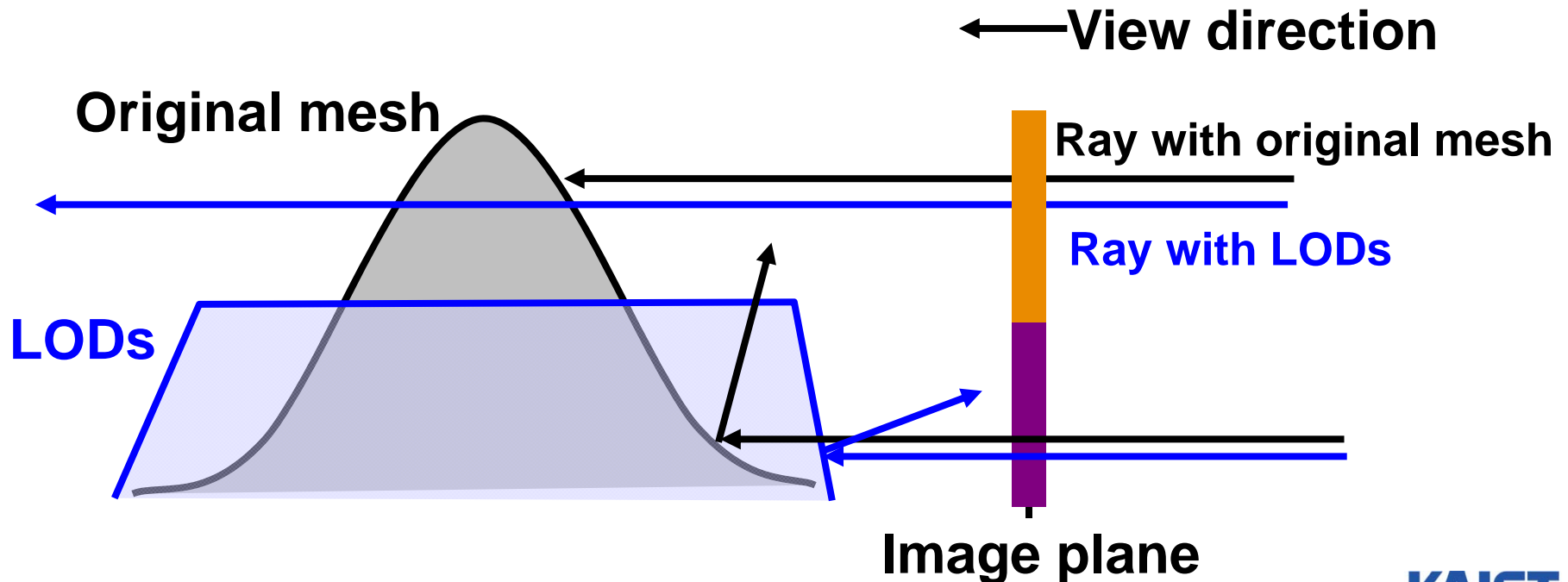
- **Compact and efficient LOD representation**
 - Add only 4 bytes to (8 bytes) kd-node
- **Drastic simplification**
 - Useful for performance improvement
- **Error-controllable LOD rendering**
 - Error is measured in a screen-space in terms of **pixels-of-error (PoE)**
 - Provides interactive rendering framework

Two Main Design Criteria for LOD Metric

- **Controllability of visual errors**
- **Efficiency**
 - **Performed per ray (not per object)**
 - **More than tens of million times evaluation**

Visual Artifacts

- **Visibility difference** **Surface deviation**
- **Illumination difference** **Projected area**
- **Path difference for secondary rays** **Curvature difference**



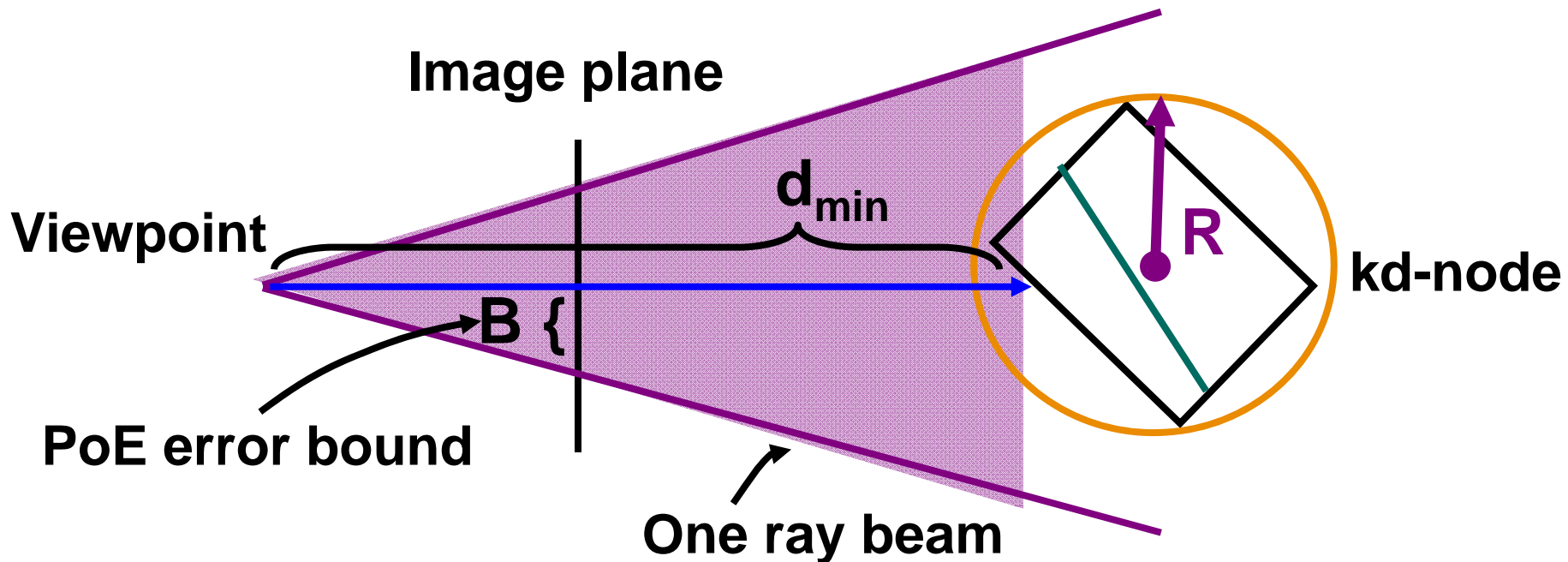
R-LOD Error Metric

- **Consider two factors**
 - **Projected screen-space area of a kd-node**
 - **Surface deviation**

Conservative Projection Method

- Measures the screen-space area affected by using an R-LOD

$$\text{LOD metric: } C(B) d_{\min} > R \quad ?$$



R-LODs with Different PoE Values



PoE: Original

1.85

5

10

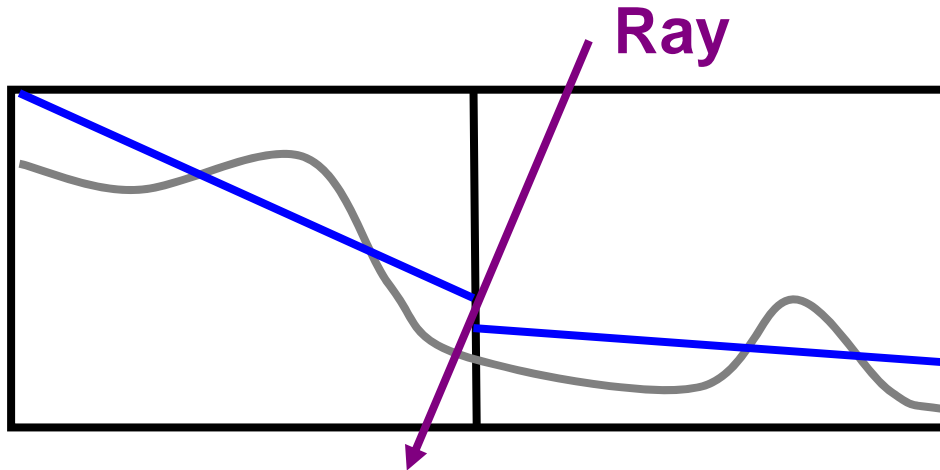
(512x512, no anti-aliasing)

LOD Metric for Secondary Rays

- **Applicable to any linear transformation**
 - Shadow
 - Planar reflection

- **Not applicable to non-linear transformation**
 - Refraction
 - Uses more general, but expensive ray differentials [Igehy 99]

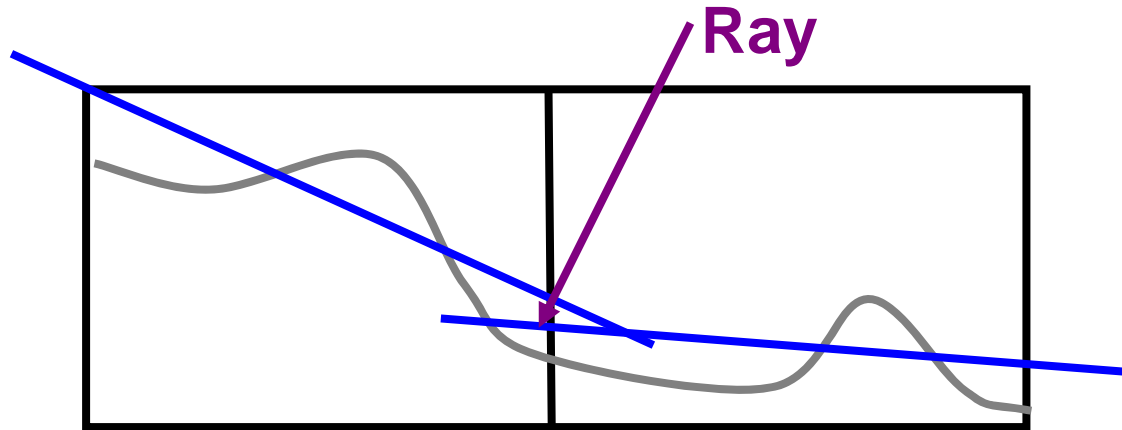
C^0 Discontinuity between R-LODs



- **Possible solutions**

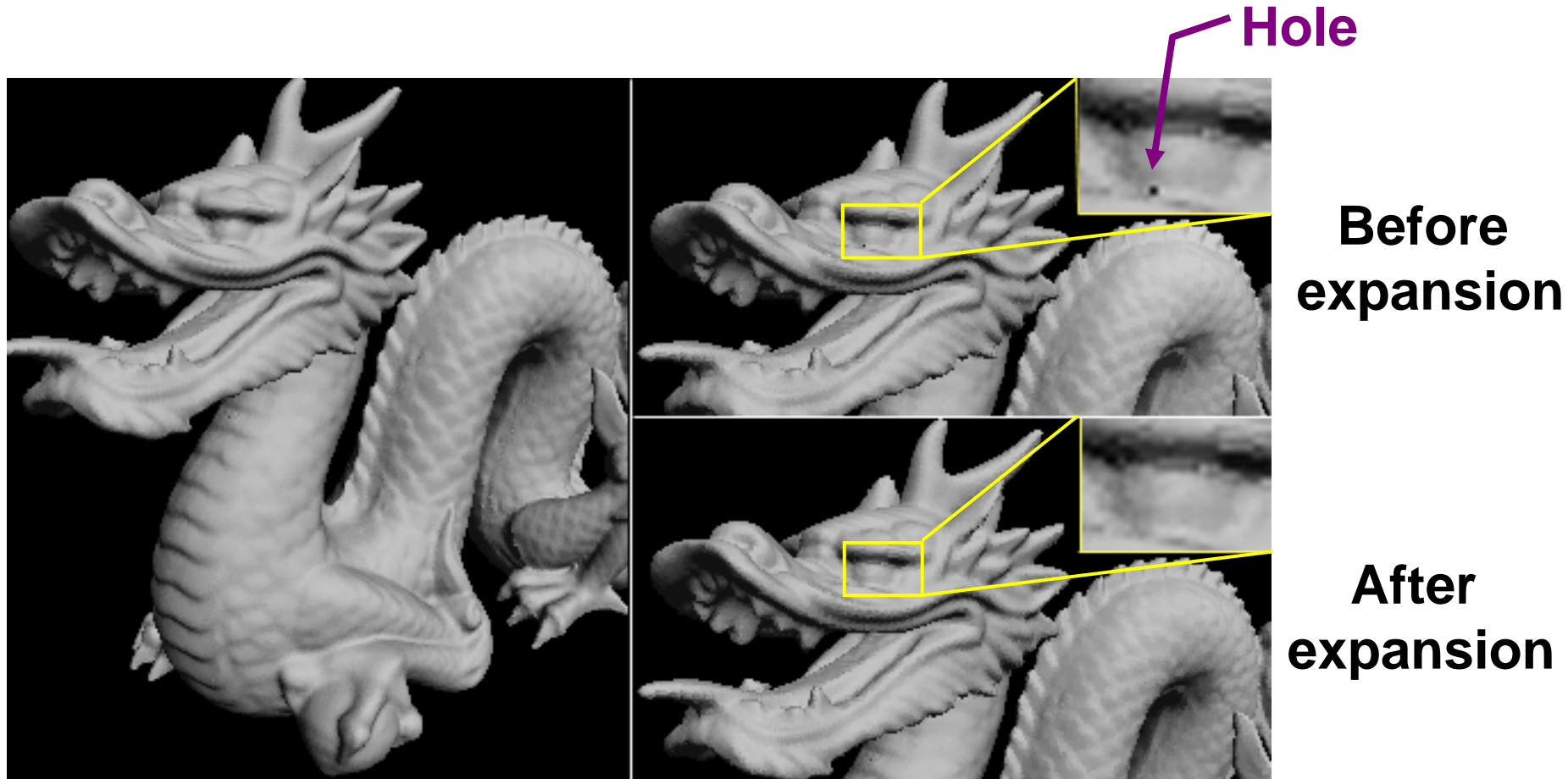
- **Posing dependencies [Lindstrom 03, Hwa et al. 04, Yoon et al. 04, Cignoni et al. 05]**
- **Implicit surfaces [Wald and Seidel 05]**

Expansion of R-LODs



- **Expansion of the extent of the plane**
 - Inspired by hole-free point clouds rendering [Kalaiah and Varshney 03]
 - A function of the surface deviation (20% of the surface deviation)

Impact of Expansions of R-LODs

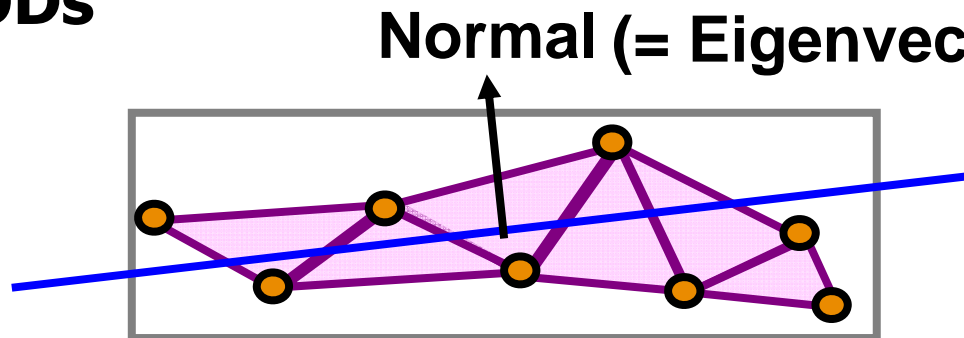


Original model

**PoE = 5
at 512 by 512**

R-LOD Construction

- **Principal component analysis (PCA)**
 - **Compute the covariance matrix for the plane of R-LODs**



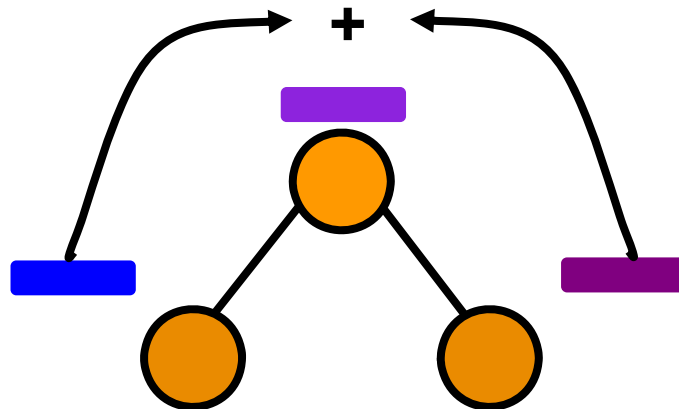
- **Hierarchical PCA computation**
 - **Has linear time complexity**
 - **Accesses the original data only one time with virtually no memory overhead**

Hierarchical PCA Computation with Linear Time Complexity

$$\sigma_{xy} = \sum_{k=1}^n (x_k - \mu_x)(y_k - \mu_x),$$

where x_k , y_k are x, y coordinates of kth points

$$\sigma_{xy} = \sum_{k=1}^n x_k y_k - \frac{2}{n} \sum_{k=1}^n x_k \sum_{k=1}^n y_k + \frac{2}{n^2} \sum_{k=1}^n x_k \sum_{k=1}^n y_k$$



Utilizing Coherence

- **Ray coherence**
 - Using LOD improve the utilization of SIMD traversal/intersection
- **Cache coherence**
 - Use cache-oblivious layouts of bounding volume hierarchies [Yoon and Manocha 06]
 - 10% ~ 60% performance improvement

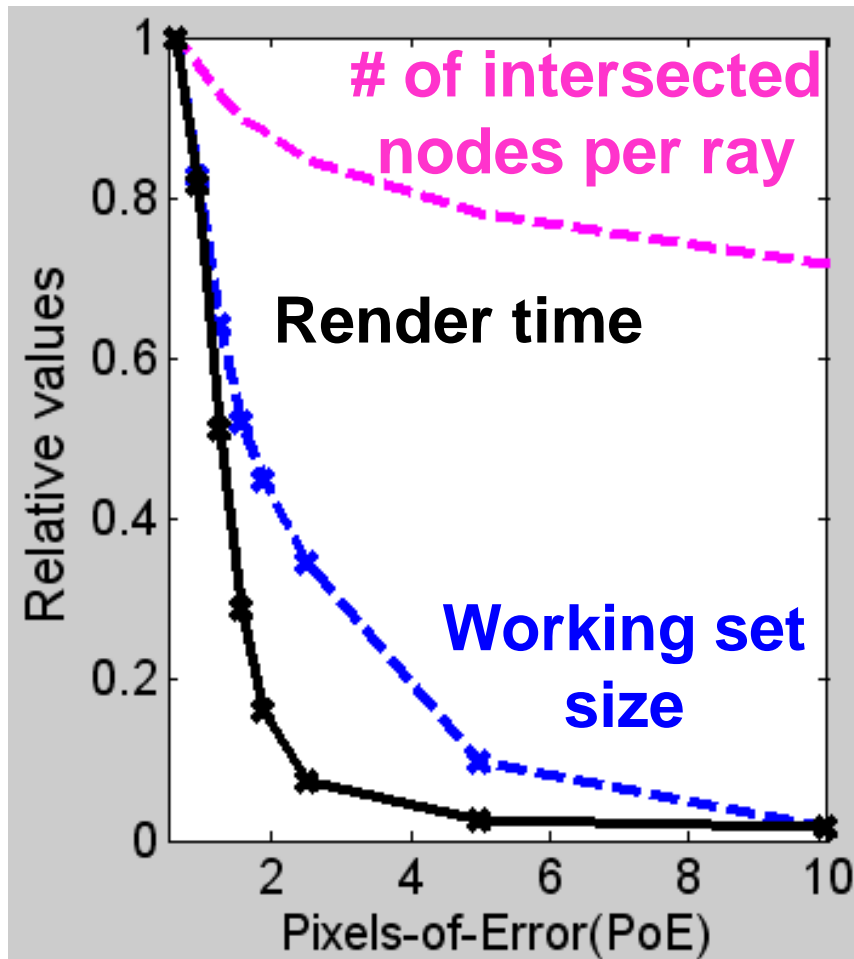
Outline

- R-LODs for ray tracing
- **Results**

Implementation

- **Uses common optimized kd-tree construction methods**
 - **Based on surface-area heuristic [MacDonald and Booth 90, Havran 00]**
- **Out-of-core computation**
 - **Decompose an input model into a set of clusters [Yoon et al. 04]**


Impact of R-LODs



10X speedup



PoE = 0
(No LOD)

PoE = 2.5 

Real-time Captured Video – St. Matthew Model

512 x 512, 2 x 2 anti-aliasing, PoE = 4



St. Matthew
with reflection &
shadows

128 Million triangles

Dual Xeon processors
with Hyper-Threading

Resolution: 512x512

Pros and Cons

- **Limitations**

- **Does not handle advanced materials such as BRDF**
- **No guarantee there is no holes**

- **Advantages**

- **Simplicity**
- **Interactivity**
- **Efficiency**

Conclusion

- **LOD-based ray tracing method**
 - **R-LOD representation**
 - **Efficient LOD error metric**
 - **Hierarchical LOD construction method with a linear time complexity**
 - **Reduce the working set size**

Ongoing and Future Work

- **Investigate an efficient use of implicit surfaces**
- **Allow approximate visibility**
- **Extend to global illumination**

At the Next Class

- **Will discuss cache-coherent layouts**